

FPA Modelling and Concepts at CSIRO

Focal Plane Array Workshop
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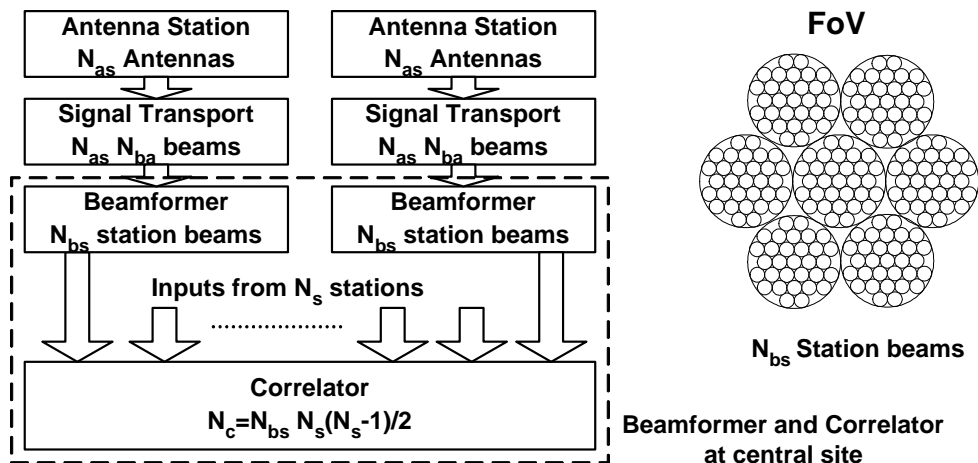
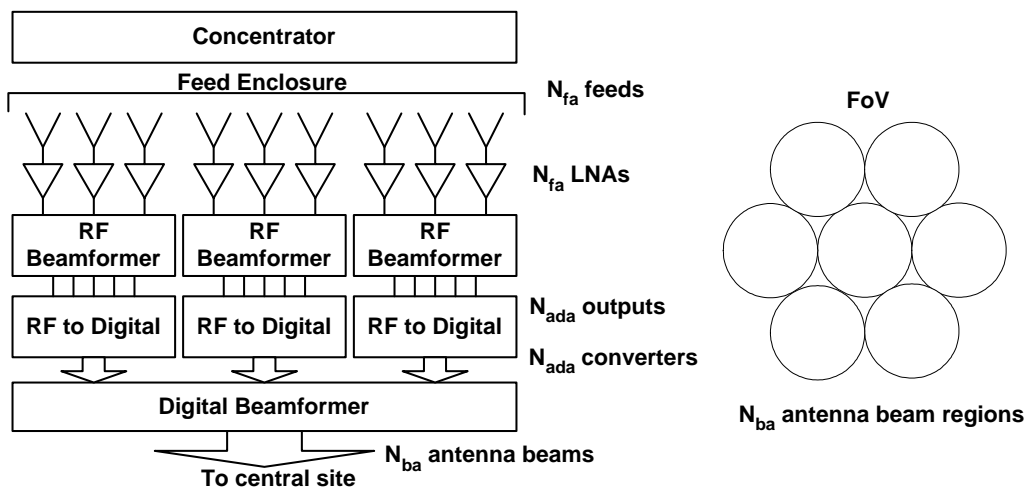


- Aim
- SKA goals and antenna concept of current focus
- Antenna-related modelling requirements; NTD, xNTD and beyond
 - Some topics of interest
 - FPA design for NTD
 - FPA size vs FoV and f/D
 - FPA system modelling
 - FPA concepts for enhanced performance eg frequency range
- Summary

- **Sensitivity**
 - $A_e / T_{\text{sys}} = 20000 \text{ m}^2 \text{ K}^{-1}$
- **Frequency range**
 - 0.5GHz – 25GHz
- **Survey speed**
 - $\text{FoV} (A_e / T_{\text{sys}})^2 \text{ BW} = 4.6 \times 10^{15} \text{ m}^4 \text{ K}^{-2} \text{ Hz}$ at 0.7GHz

eg FoV = 100 square degrees BW = 400MHz

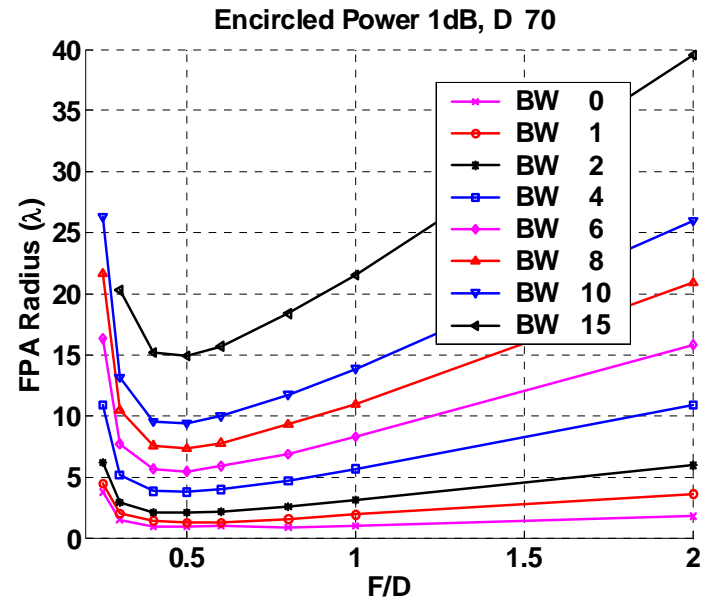
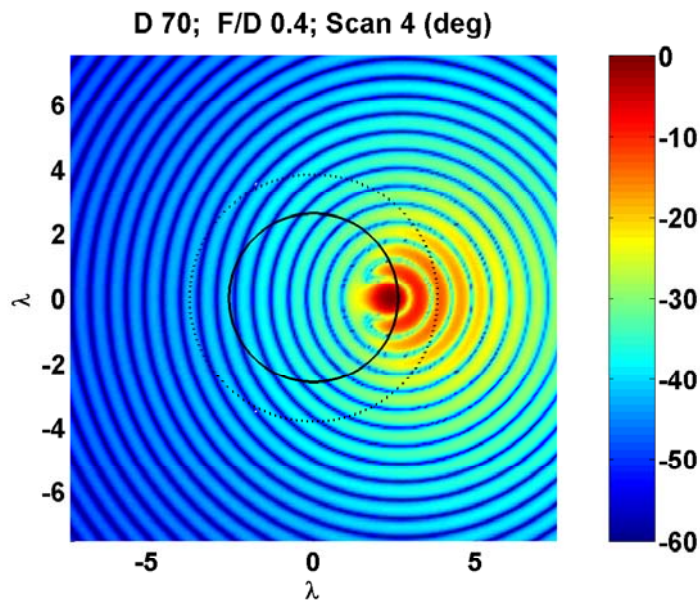
SKA general form with FPA antennas



- **FPAAs with all-digital beamforming in paraboloidal reflectors**
 - reduce signal-transport and correlator costs
 - correct for reflector effects eg aberrations and cross polarization
 - RFI mitigation
 - contiguous FoV
 - technologies possibly with broader application

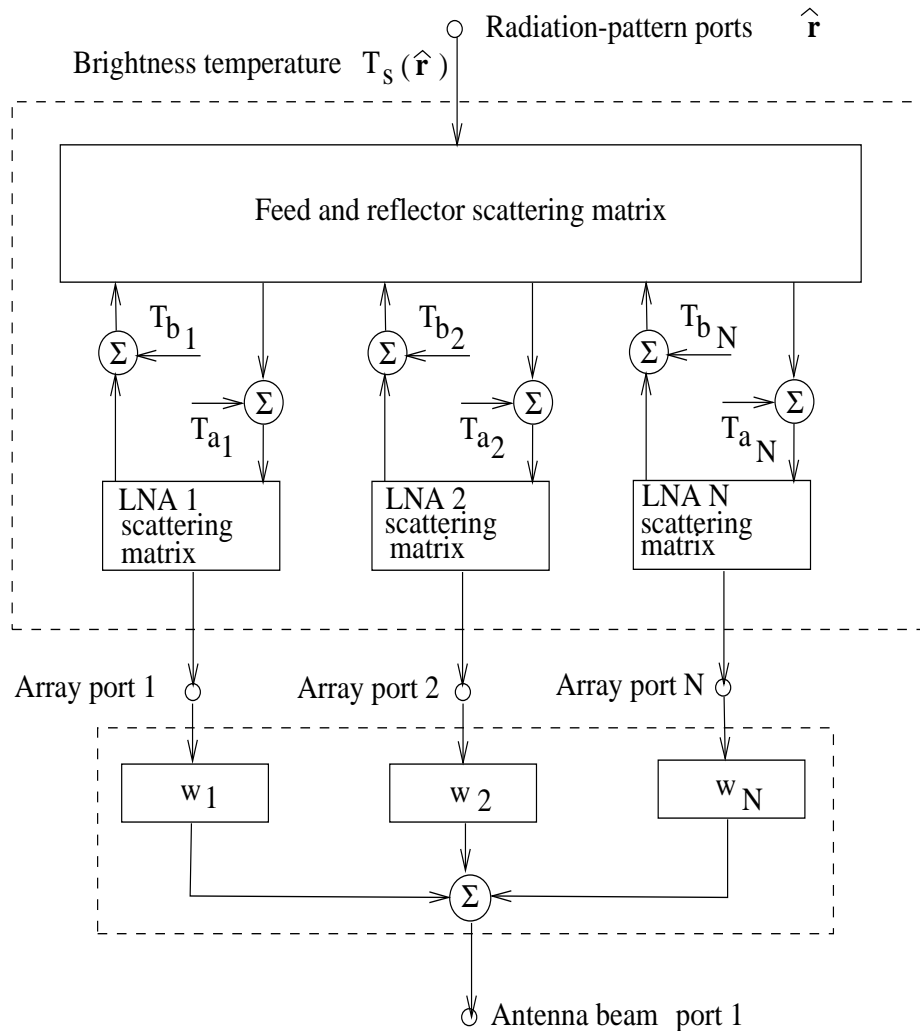
- **NTD**
 - FPA design with Vivaldi or similar element, collaboration with ASTRON and U. Mass.
 - Reflector-FPA interaction
 - System model, including antenna, LNAs, digitizers and beamformer
 - Preliminary investigation of possible trades and optimum design
 - Verification
- **xNTD and beyond**
 - Low-cost reflector options
 - Optimum design studies; antenna/LNA/conversion/beamforming
 - Investigate other FPA elements and configurations
 - increase frequency range
 - decrease cost
 - other performance enhancements
 - Modelling capability enabling such

FPA size for specified A_e and f/D



- D.B. Hayman, T.S. Bird, K.P. Esselle and P. Hall, 2005 IEEE AP-S Symposium.

Sensitivity (Ae/Tsys) modelling



$$\frac{A_e(\hat{\mathbf{r}})}{T_{\text{sys}}} = \frac{|\phi^t \mathbf{w}|^2}{\bar{\mathbf{w}}^t \mathbf{M} \mathbf{w}}$$

$$\phi_i = \mathbf{S}_i(\hat{\mathbf{r}}) \cdot \hat{\mathbf{p}}$$

$$M_{i,j} = \frac{1}{\lambda^2} \iint d\Omega \bar{\mathbf{S}}_i(\hat{\mathbf{r}}) \cdot \mathbf{S}_j(\hat{\mathbf{r}}) T_s(\hat{\mathbf{r}}) + \sum_p \bar{\mathbf{S}}_{i,a_p} \mathbf{S}_{j,a_p} \mathbf{T}_{a_p} + \sum_p \bar{\mathbf{S}}_{i,b_p} \mathbf{S}_{j,b_p} \mathbf{T}_{b_p} + 2\Re \sum_p \bar{\mathbf{S}}_{i,a_p} \mathbf{S}_{j,b_p} \mathbf{T}_{a_p,b_p}$$

- Jan Peter Peeters Weem “Broad band antenna arrays and noise coupling for radioastronomy”, PhD thesis, U. Colorado, 2001.
 - Directly radiating arrays
 - Role of Tx-mode reflection coefficient

- Maximum A_e (conjugate match)

$$w = \bar{\phi}$$

- Maximum A_e/T_{sys} (Bird and Hayman, URSI GA, 1996)

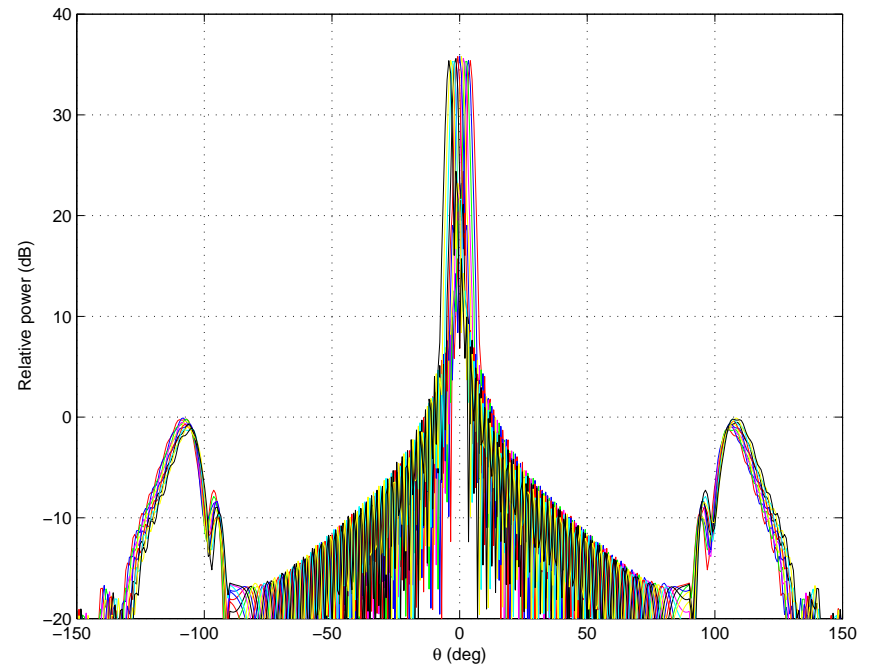
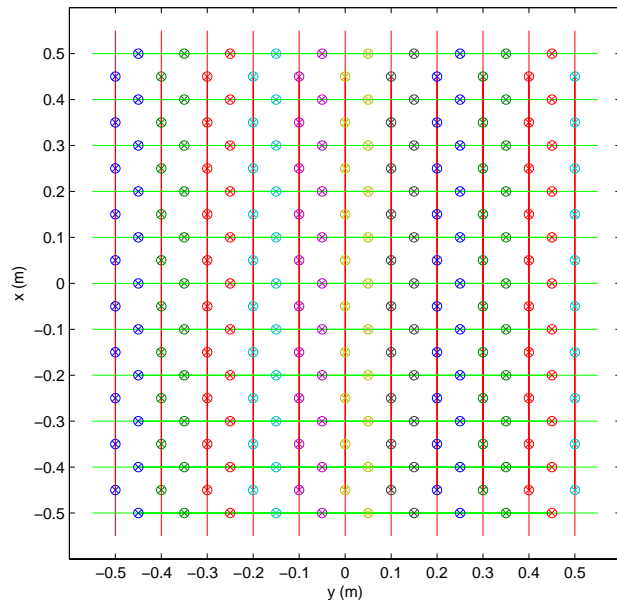
$$w = M^{-1} \bar{\phi}$$

- Maximum A_e/T_{sys} subject to upper bounds on co- and cross-polar sidelobes

- Successive Projections (Poulton, Electron. Lett. 1986) approach is possible, perhaps including quantization or dynamic-range constraints as additional sets

- Requirements from image formation studies

Illustration - wire-grid over groundplane



- MoM solution for scattering matrix of array
- 14m-reflector $f/D=0.4$ at 0.7GHz and zenith
- Ground and sky noise temperature models

Illustration – A_e/T_{sys}

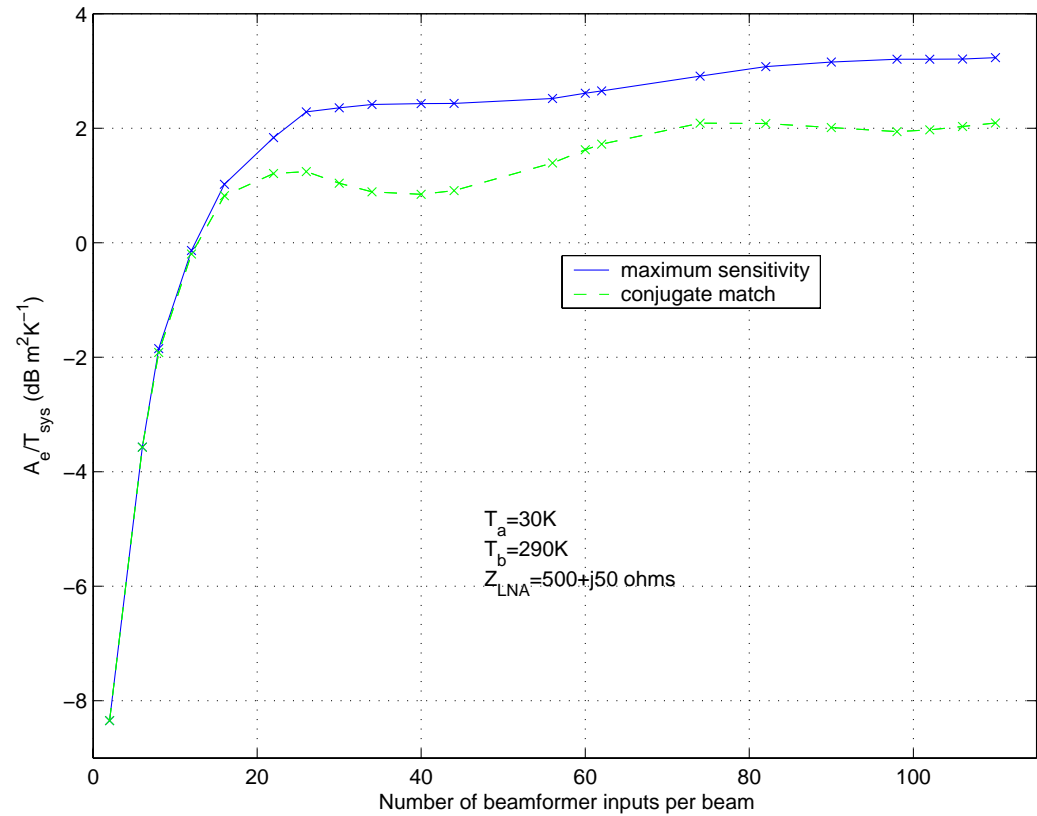
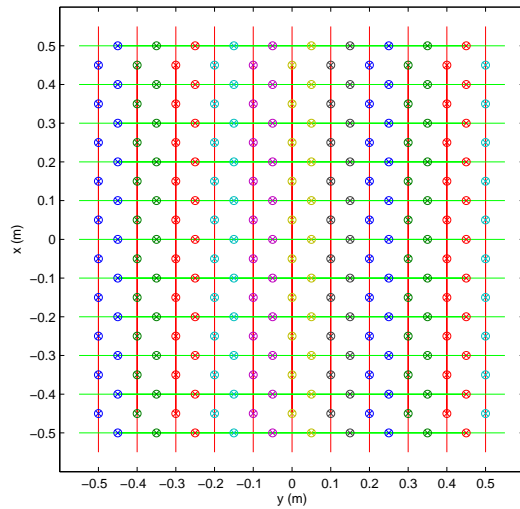


Illustration – T_{sys} and A_e

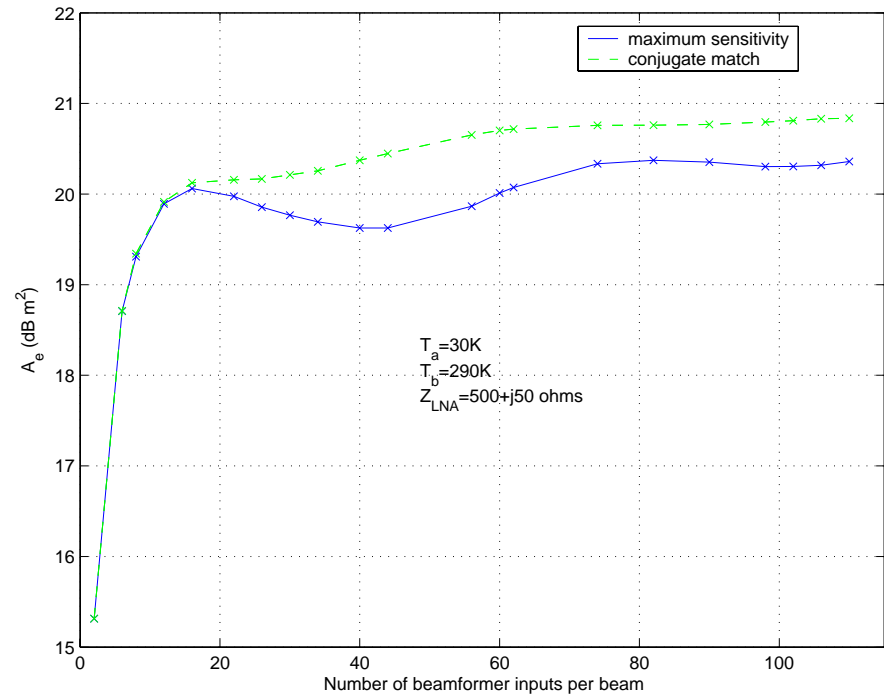
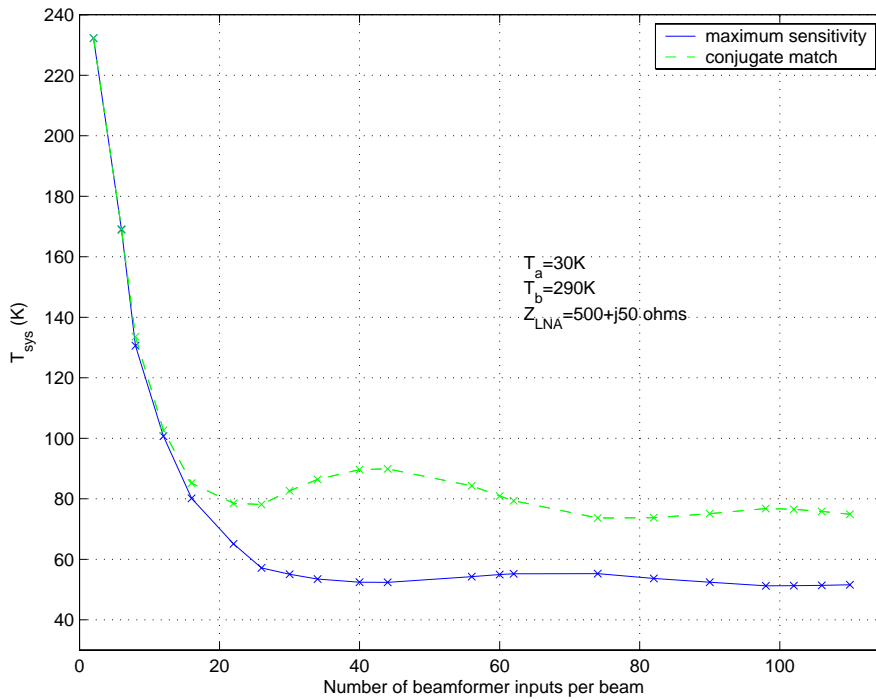


Illustration – T_b effect on T_{sys}

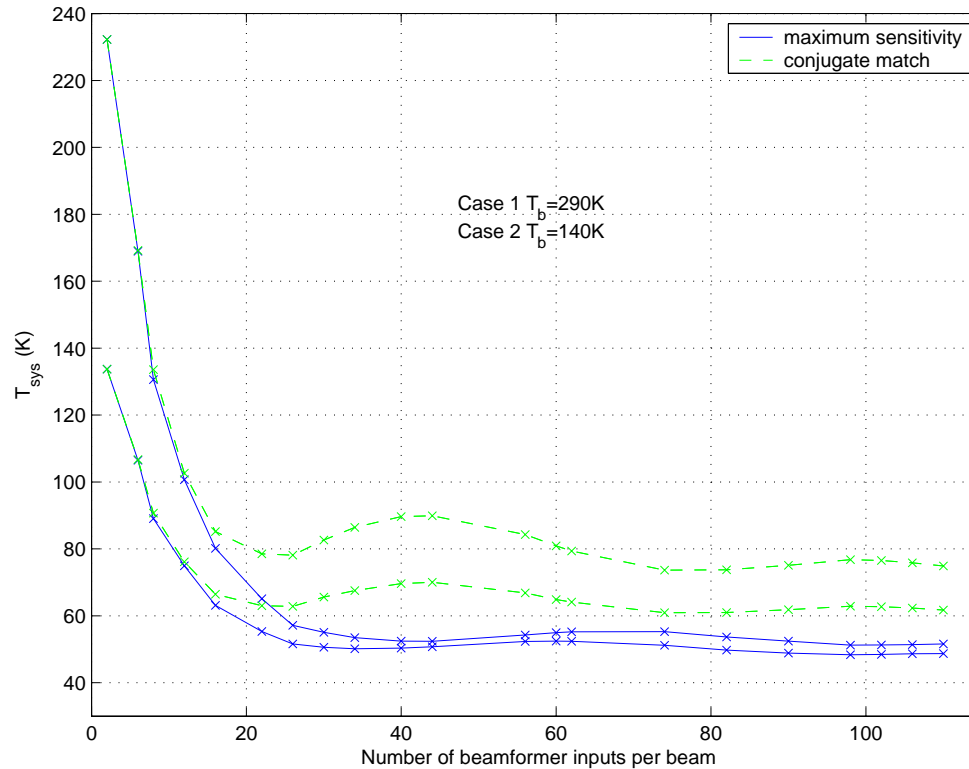


Illustration – Tx-mode reflection coefficient

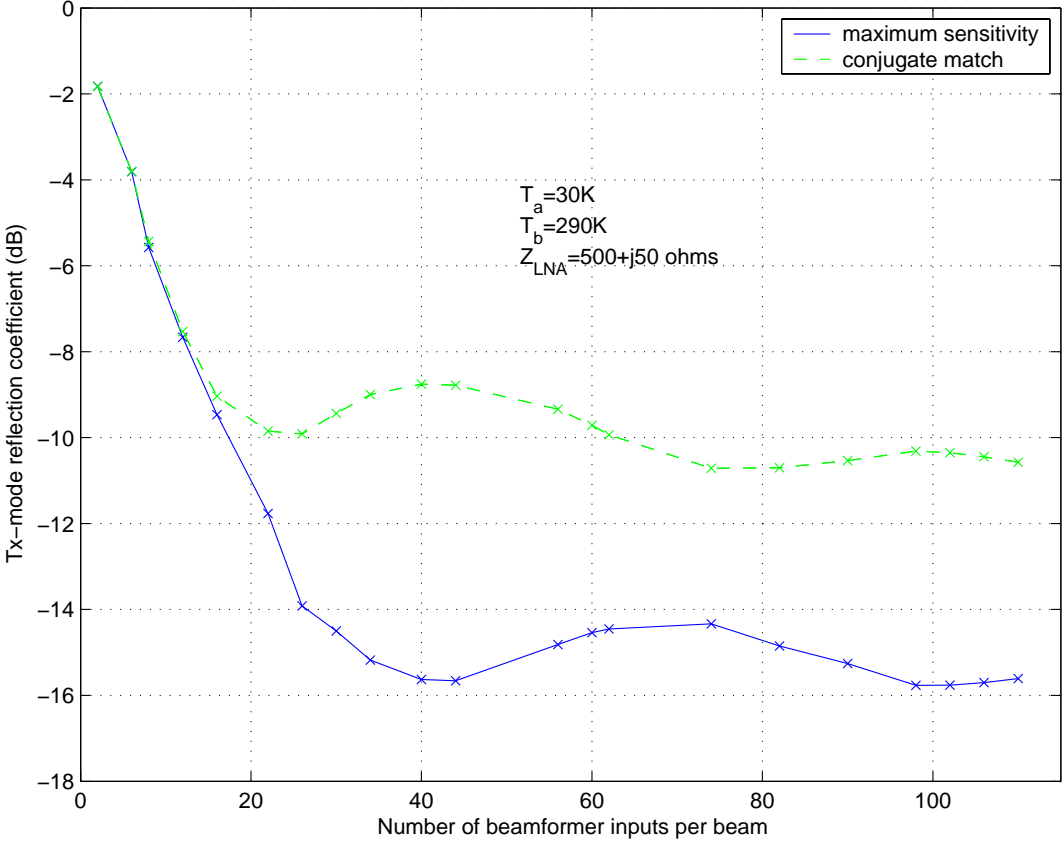
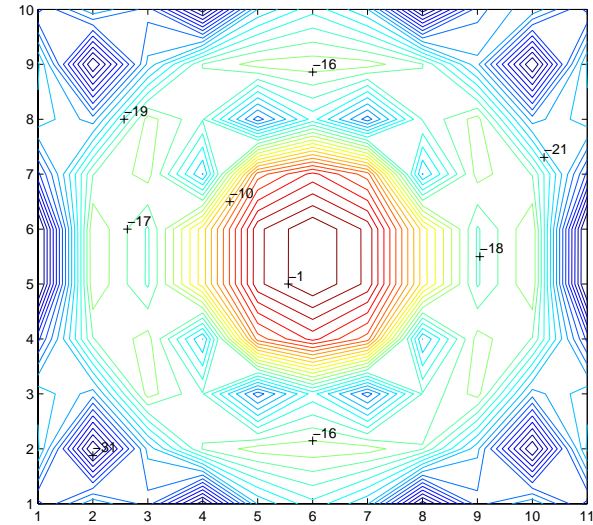
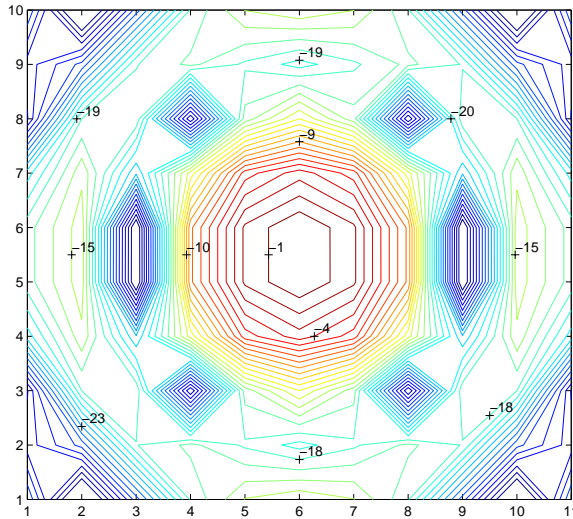


Illustration - weights



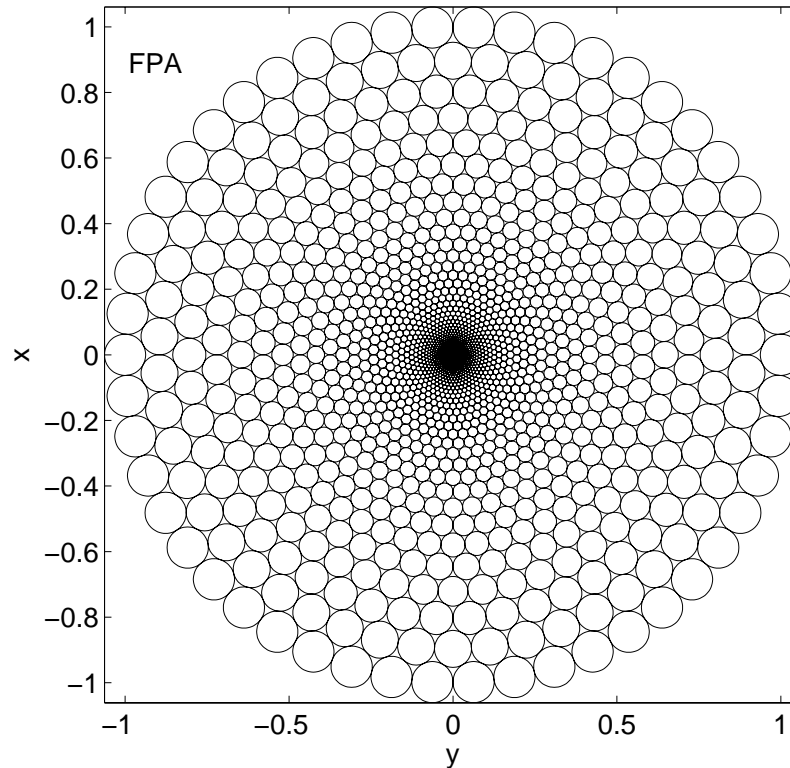
- Max Ae/Tsys (left) and conjugate match (right)

- **Other FPA configurations (increased frequency range or reduced antenna cost)**
 - Other elements (eg published work on rabbit ear in radar application)
 - Fractal/nested structures
 - Conductivity switching
 - Directive self-complementary structures
 - 3-dimensional digital beamforming
 - Foveated focal-plane array
- **Development of EM modelling capability**
 - Flexible boundary element method
 - Interactions with other structures, eg reflector and supports, via Green's-function approach or scattering-matrix with free-space modes eg SWE
 - Implementation in grid/cluster computing

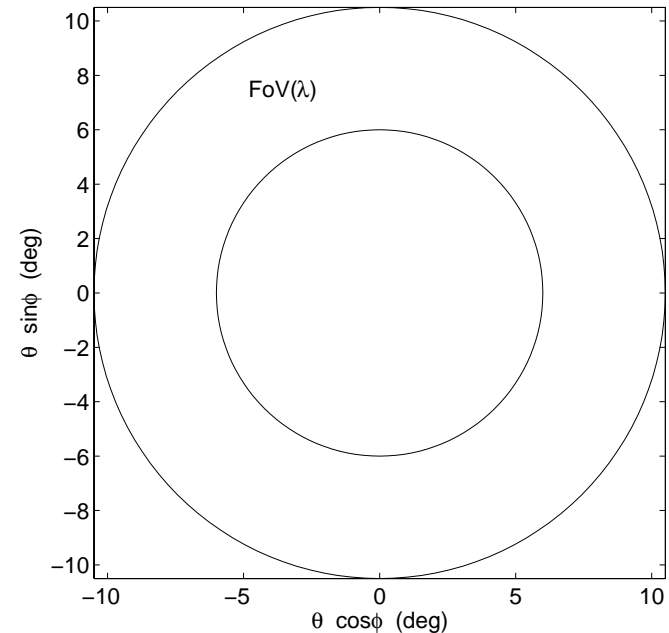
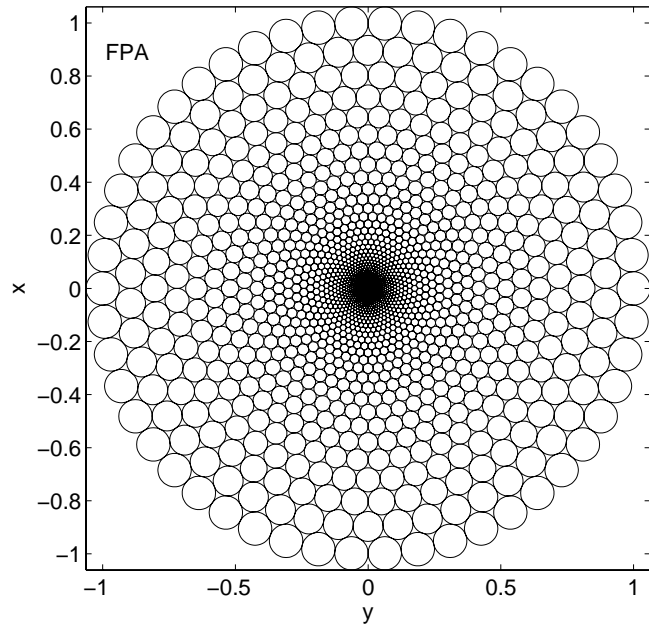
Other FPA configurations – increased frequency range

- SKA goals
 - $A_e / T_{\text{sys}} = 20000 \text{ m}^2 \text{ K}^{-1}$
 - 0.5GHz – 25GHz
 - $\text{FoV} (A_e / T_{\text{sys}})^2 \text{ BW} = 4.6 \times 10^{15} \text{ m}^4 \text{ K}^{-2} \text{ Hz}$ at 0.7GHz
- The data rate into the correlator is proportional to $(\text{FoV}/\lambda^2) \text{ BW}$
- One approach: keep BW constant and let FoV vary as λ^2

Foveated FPA

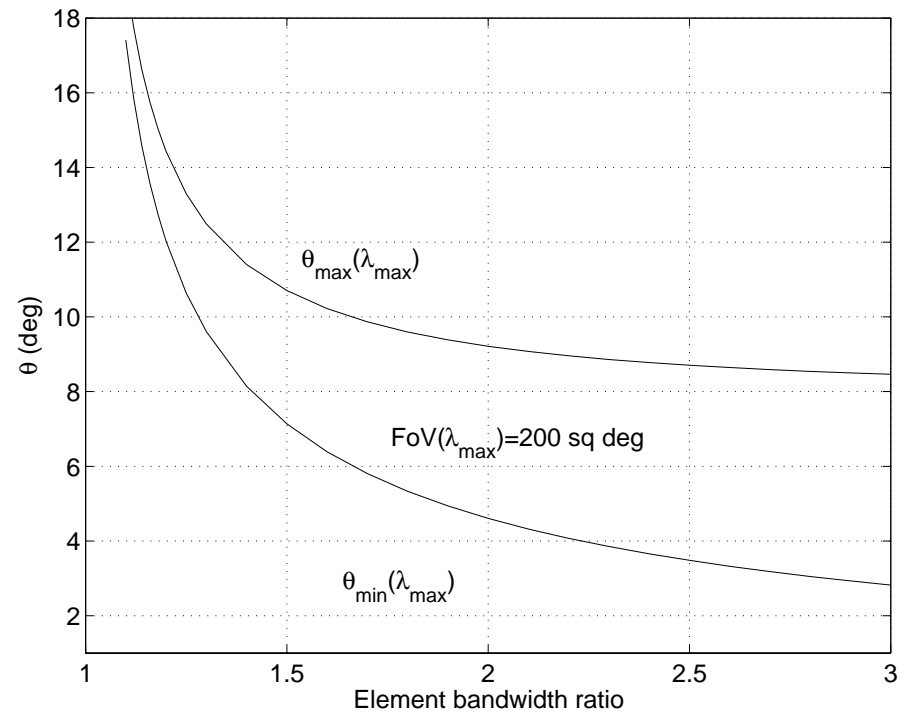
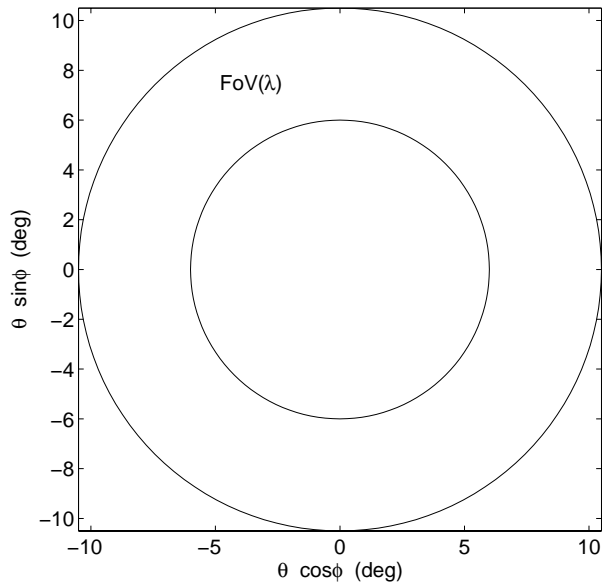


- Geometry periodic in $\log(x+jy)$
- Suited to the aberration behaviour of focussing reflectors
- Various element types possible

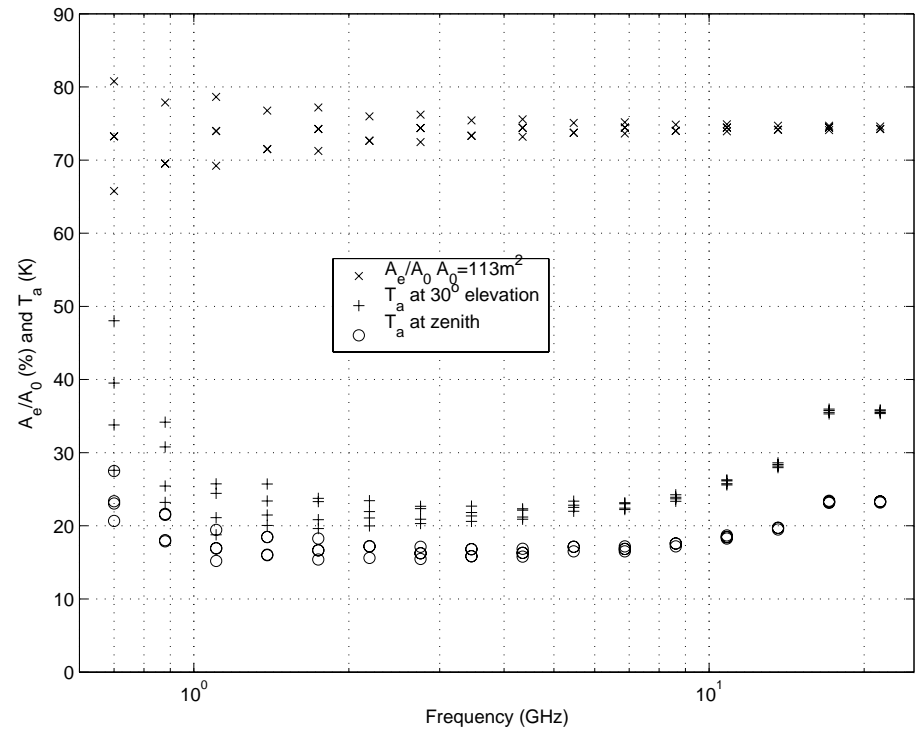
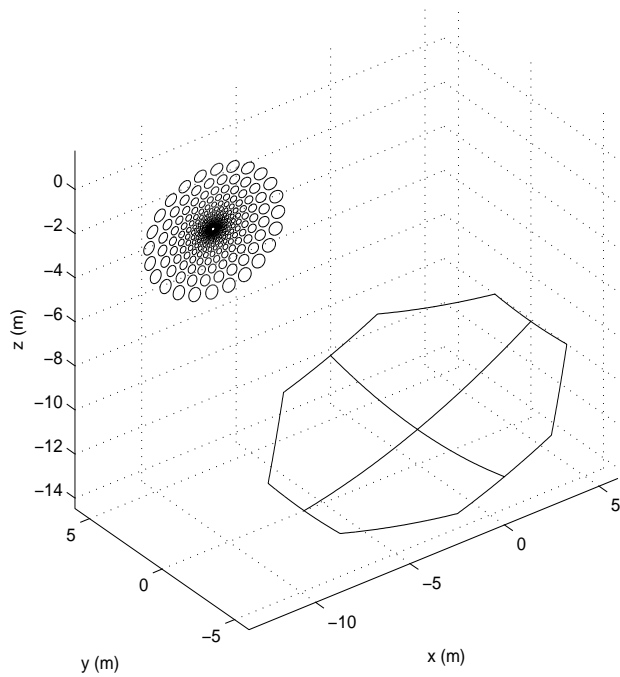


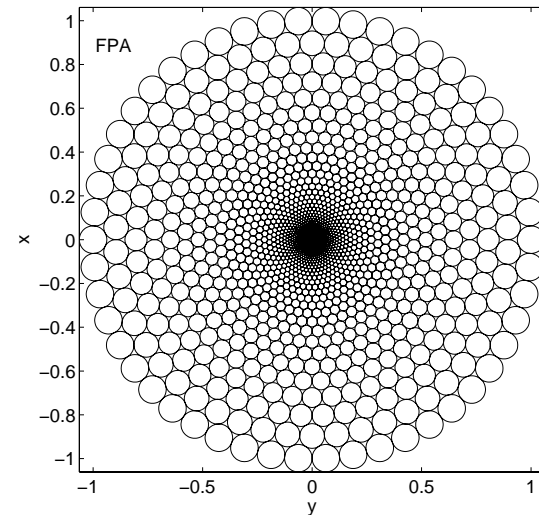
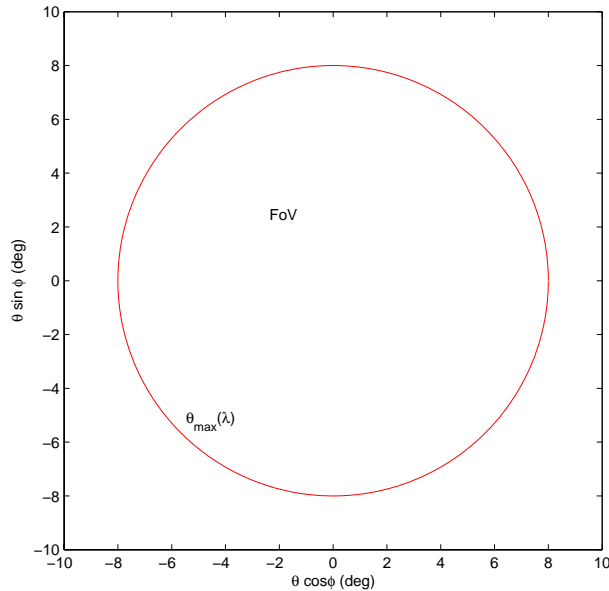
- All elements have same BW ratio, centre frequency increasing towards array centre
- Prolonged tracking still possible

Form 1 cont



Example with offset-fed reflector





- All elements have common lowest frequency, BW increasing towards array centre
- Still reduction in number of elements and beamformer inputs at lowest frequency, compared to non-foveated geometry

- Outline of antenna-related modelling of interest for NTD, xNTD and beyond
 - FPA antenna design for NTD and beyond
 - System modelling important for determining significance of antenna, LNA, digitizer and beamformer properties and optimum design
 - Interested in other elements and FPA configurations to get from NTD to SKA

For more information, see www.csiro.au or contact:

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