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#### Master Astronomy and Astrophysics - 5214RAAS6Y



#### Radio Astronomy Lecture 2

#### The Science of Radio Astronomy: Extragalactic

#### Lecturer: Michael Wise (wise@astron.nl)

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## Outline

- Radio Astronomy for Extragalactic Science
- Nearby Galaxies, Astrometry, SNR, GRBs, Mapping HI, Dynamics, Star Formation, FIR-Radio Correlation Magnetic Fields, Lensing
- Radio Galaxies, AGN, Jets, Quasars, Black Hole Growth, Feedback, Gas Flows, and Radio Source Evolution
- Groups and Clusters, Feedback, Relics, Halos, Shocks and Turbulence
- Cosmic Microwave Background, S-Z Effect, EoR, Cosmology and Large-scale Structure

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## Extragalactic Science

How do galaxies form and evolve? What part do black holes play? How do black holes form and grow? What governs large-scale structure growth? What is dark matter and where is it? What were the early phases of the universe?

## ⇒ Gives us the big picture





#### ⇒ Probes a wide range of physics

- Dark Ages (spin decoupling)
- Epoch of Reionization (highly redshifted 21 cm lines)
- Early Structure Formation (high z RG)
- Large Scale Structure Evolution (diffuse emission)
- Evolution of Dark Matter & Dark Energy (Clusters)
- Energy Feedback into the Intracluster Medium (AGN)
- Black Hole Formation and Growth (AGN, jets)
- Particle Acceleration (AGN, cluster merger/accretions shocks)
- Star Formation and Galaxy Evolution (distant starburst galaxies)
- Formation of Magnetic Fields (nearby galaxies)
- Source populations (large, all-sky surveys)

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#### Why Synthesis Imaging? ⇒ Resolution

Angular resolution can be tuned by the observer by selecting baselines (but trade sensitivity to emission on different scales)

Reduce source "confusion" problem Match resolutions at other wavelengths Extremely accurate absolute astrometry High angular resolution (10<sup>-3</sup> arcsec)



Bright radio AGN Cygnus A at a variety of frequencies and angular resolutions from VLA to VLBI baselines

Carilli & Harris (1996)





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Apparent superluminal motion in quasar 3C279 is shown as mosaic of five VLBA radio images made over seven years at 22 GHz with resolution of 0.001 arcseconds



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#### Why Synthesis Imaging? ⇒ Dynamic Range

High dynamic range achieved via deconvolution and self-calibration (1,000,000:1 in some cases!)

High sensitivity via long exposures

Resolve diffuse emission in the presence of bright sources

Detect faint sources and resolve "confusion" limitations



VLA 330 MHz image of the galaxy M87, showing details of the large-scale, radio-emitting "bubbles" believed to be powered by the central black hole

Owen, Eilek, & Kassim (1999)





#### Why Synthesis Imaging? ⇒ Dynamic Range

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WSRT 1.4 GHz image of the Perseus cluster showing details of the large-scale, radio halo exposed at a dynamic range of 1,000,000:1

de Bruyn & Brentjens (2010)

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## Beating Confusion



**Telescope beam** 

Un-resolved sources in beam limit achievable sensitivity Function of resolution, frequency, and source density

![](_page_8_Picture_6.jpeg)

# Beating Confusion

"RMS" confusion:  $\sigma_{c} \approx 0.2 \ v^{-0.7} \ \theta^{2}$  where

 $\sigma$  is in mJy/beam  $\nu$  is in GHz  $\theta$  is in arcmin

![](_page_9_Figure_3.jpeg)

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NVSS (45 arcsec) grayscale under GBT (12 arcmin) contours

DDO 154

NGC 3198

NGC 2976

HOIL

NGC 7793

IC 2574

#### NGC 3621

NGC 4214

NGC 2366

NGC 3521

NGC 2841

# Nearby Galaxies

NGC 4826 (M64)

NGC 5194 (M51)

NGC 925

NGC 628 (M74)

NGC 3031 (M 81)

NGC 4449

M81 DWB

![](_page_10_Picture_8.jpeg)

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NGC 3627 (M66)

![](_page_10_Picture_10.jpeg)

## Radio Astrometry

![](_page_11_Picture_1.jpeg)

![](_page_11_Figure_2.jpeg)

Brunthaler et al. (2000)

![](_page_11_Figure_4.jpeg)

- VLBA astrometry of H<sub>2</sub>O masers in M33
- Angular rotation + proper motion
- Distribution of dark matter in the Local Group
- History and fate of Local Group galaxies
- Distribution of dark matter in nearby galaxies

![](_page_11_Picture_11.jpeg)

![](_page_11_Picture_12.jpeg)

## Supernova Remnants

![](_page_12_Figure_1.jpeg)

Radio monitoring of the supernova remnant from SN 1993J located in M81, a spiral galaxy in the constellation Ursa Major, from May 1993 to Feb 2000.

![](_page_12_Picture_3.jpeg)

![](_page_12_Picture_5.jpeg)

### Gamma-ray bursts ⇒ Most luminous explosions in the universe Each burst may emit up to ~10<sup>54</sup> erg

![](_page_13_Figure_1.jpeg)

A GRB detected by <u>BATSE</u>, the Burst And Transient Source Experiment, on-board the Compton Gamma-Ray Observatory (CGRO) Spatial distribution of GRBs detected by **<u>BATSE</u>** 

![](_page_13_Figure_4.jpeg)

Distribution implies extragalactic origin Confirmed using host galaxy emission lines

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# Gamma-ray bursts

#### Principal GRB Models

- Collapse of a rotating massive star
- Neutron Star Neutron Star Mergers
- Black Hole Neutron Star (He star) Mergers
- Black Hole Neutron Star Mergers
- Black Hole White Dwarf Mergers

#### Science Drivers

- Stellar Collapse, Black Holes
- Jet and Fireball Physics
- UHE cosmic ray acceleration , v
- Gravitational radiation
- Early universe, star formation, reionization

![](_page_14_Figure_13.jpeg)

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![](_page_14_Picture_14.jpeg)

![](_page_15_Figure_0.jpeg)

## Gamma-ray bursts

#### Synchrotron Afterglow Spectrum $\nu^{1/3}$ -(p-1)/2 -2 Slow cooling -3 F<sub>v</sub>(Jy) -4 -5 ν<sup>-p/2</sup> -6 -7 -8 -9 10 12 16 18 8 14 v(Hz)-1 ,-1/2 Fast cooling $\nu^{1/3}$ -2 -3 F<sub>v</sub>(Jy) v<sup>-p/2</sup> -5 -12/7 -6 -7 20 8 10 12 14 16 18 v(Hz)Sari, Piran, and Narayan (1998)

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#### **Radio Emission from Forward Shock**

![](_page_16_Figure_3.jpeg)

- 50% of all bursts show radio afterglows
- Radio positions accurate to 0.01"
- Good for location in host galaxy (galaxy size 1-3")
- No simple power law decline
- Can monitor the source for years
- Prompt, short-lived radio flares have been detected
- Beginning of afterglows show strong ISM scintillation

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## Starburst Galaxies

- Starburst galaxies have star-formation intensities of I-100 M<sub>☉</sub> yr<sup>-1</sup> kpc<sup>-2</sup> (x10<sup>3</sup> Milky Way)
- Starbursts often are stimulated by galaxy mergers or close passages
- Radio emission is thermal emission from HII regions ("super star clusters") or nonthermal emission from supernova remnants
- Correlated with Far-Infrared emission
- Starbursts younger than a few Myr are dominated by thermal radio emission

![](_page_17_Picture_6.jpeg)

Image of starburst galaxy M82 (D  $\sim$  3 Mpc) showing the stellar disk of the galaxy, which harbors its active star formation, and a perpendicular supergalactic wind of ionized gas powered by the starburst (HST+WIYN).

![](_page_17_Picture_10.jpeg)

# Typical Spectrum (M82)

![](_page_18_Figure_1.jpeg)

# LFIR - LRadio Correlation

![](_page_19_Figure_1.jpeg)

Gordon et al. (2004)

**M8** 

- Driven by star formation of massive stars
- Form in dusty giant molecular clouds; nearly all their luminosity emerges in FIR
- SNR accelerate free electrons which escape into the galaxy and emit synchrotron
- Assume starburst history, adopt IMF:

SFR  $(M_{\odot} \text{ yr}^{-1}) = 4.5 \times 10^{-44} \text{ L}_{FIR} \text{ (ergs s}^{-1})$ 

• Can use radio to measure SFR at high z!

![](_page_19_Figure_9.jpeg)

![](_page_19_Picture_10.jpeg)

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### Merger Induced Starbursts ⇒ Nearest Merger - The "Antennae"

#### WFPC2 with CO overlay

#### VLA 5 GHz image

![](_page_20_Figure_3.jpeg)

Whitmore et al. (1999); Wilson et al. (2000)

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5 mJy ~ 30,000 O7-equivalent stars

![](_page_20_Picture_7.jpeg)

## HI Galaxy Structure Studies

![](_page_21_Picture_1.jpeg)

All-sky image of the HI column density in the Milky Way - from the Dwingeloo- Leiden survey

HI from the Milky Way

![](_page_21_Figure_4.jpeg)

Oort, Kerr & Westerhout (1958)

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- HI comprises 5-10% mass in the Milky Way
- HI traces the "warm" interstellar medium
- Organized into diffuse clouds of gas and dust

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- Traces structure and kinematics
- Traces streams and high velocity clouds
- Traces accretion and mergers
- Probe of dark matter
- Evolution of gas content with redshift

# Why Neutral Hydrogen (HI) ?

- Hydrogen most common element in the universe ⇒ present "everywhere"!
- Narrow spectral line ( for T ~ 100 K, Δv ~ 1 km/s )
- Systemic shifts are always much larger

2 (VEL)\*

- Doppler effect  $\Rightarrow$  kinematics!
- Optically thin

![](_page_22_Figure_6.jpeg)

Every channel is one plane of the cube

( (RA) →

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m (DEC)

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## 21-cm line of Neutral Hydrogen

- The ground state of HI can undergo a hyperfine transition
- Spin of electron reverses (higher energy state when the spins are parallel)
- Difference corresponds to  $E = 6 \times 10^{-6} \text{ eV}$ )

![](_page_23_Figure_4.jpeg)

Population of the two states is determined primarily by collisions between atoms  $\Rightarrow T_s$  equal to the kinetic temperature

![](_page_23_Picture_6.jpeg)

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### HI Detected in Emission

![](_page_24_Figure_1.jpeg)

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### HI Detected in Absorption

![](_page_25_Figure_1.jpeg)

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### HI Detected in Absorption

![](_page_26_Figure_1.jpeg)

### Examples of HI studies

![](_page_27_Picture_1.jpeg)

- Galactic studies , high velocity clouds, satellites of the Milky Way.....
- Nearby galaxies and gas accretion
- Dark matter studies
- Interacting systems (including the stream in our own Galaxy)
- Effects of dense cluster IGM on cluster member galaxies (e.g. stripping etc.)
- Gas and Active Galactic Nuclei (AGN) ⇒ HI absorption tracing circumnuclear gas outflows
- Intervening HI => neutral hydrogen located between us and a radio source

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### Interacting systems

#### VLA C+D-array observations of NGC 4038/9 - "The Antennae"

![](_page_28_Picture_2.jpeg)

![](_page_28_Picture_3.jpeg)

![](_page_28_Picture_5.jpeg)

### Dark matter studies

#### HI much more extended than the stars

 $M \approx RV^2$ 

M = mass R = distance from centerV = velcocity at R

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![](_page_29_Picture_5.jpeg)

NGC 2915 Meurer et al.(2002)

![](_page_29_Picture_6.jpeg)

## Gravitational Lensing

Gravitational lensing is the deflection of light by mass along the line of sight to the background source.

![](_page_30_Figure_2.jpeg)

#### Can be used to:

i) Study the mass distribution of the lens -- test galaxy formation and models for dark matter.

ii) Study the high redshift Universe as a cosmic telescope.

iii) Measure the cosmological parameters through the lensing statistics.

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![](_page_30_Picture_7.jpeg)

## Mass Structure of Galaxies

![](_page_31_Picture_1.jpeg)

![](_page_31_Picture_2.jpeg)

![](_page_31_Picture_4.jpeg)

# The Magnified Universe

![](_page_32_Figure_1.jpeg)

VLA imaging of CO (2-1) molecular gas at 0.3 arcsec resolution.

Lens modelling detects a rotating disk of gas around a z = 4.12 quasar.

![](_page_32_Picture_4.jpeg)

![](_page_32_Picture_5.jpeg)

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(Riechers et al. 2008)

8.5 kpc

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## Radio Galaxies

![](_page_33_Picture_1.jpeg)

![](_page_33_Picture_2.jpeg)

## AGN Terminology

- Supermassive Black Hole (SMBH)
- Active Galactic Nucleus (AGN)
  - Technically any accreting SMBH, but generally used for low-luminosity (or similarly low-accretion rate)
- Quasar short for quasi-stellar radio source
  - Usually luminous AGN (>1043-44 erg/s), regardless of radio emission (a better name is quasi-stellar object or QSO)
- Standard Review Papers
  - Canonical Paradigm: Antonucci 1993 (Radio-quiet AGN); Urry & Padovani 1995 (Radio-loud AGN)
  - More Recently: Ho et al. (2008); Antonucci (2011); Elitzur (2012)
  - Also see Boroson & Green (1992); Elvis (2000); Richards et al. (2011)

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## The Radio Galaxy Zoo

#### **\***Radio Galaxies

- Strong extended radio emission but rather weak nucleus. Can display either narrow optical emission lines (NLRG) or broad optical emission lines (BLRG)
- **\***Radio Loud Quasars
  - Strong extended radio emission and a strong/ variable nucleus showing broad optical emission lines

#### **\*Blazars**

Strong and variable emission across the whole spectrum; no emission lines; highly polarized, nonthermally dominated

![](_page_35_Picture_9.jpeg)

## Faranoff-Riley Type I & II

![](_page_36_Figure_1.jpeg)

⇒ FR-I : low power systems that are bright in the center and then fade off at the edges, i.e., "edge darkened". Look like smoke-stacks.

![](_page_36_Picture_5.jpeg)

## Faranoff-Riley Type I & II

![](_page_37_Picture_1.jpeg)

![](_page_37_Picture_2.jpeg)

⇒ FR-II : high power systems that brighten at the edges (edge-brightened). Often look like directed "explosions".

![](_page_37_Picture_4.jpeg)

![](_page_37_Picture_6.jpeg)

### AGN Unification Schemes

![](_page_38_Picture_1.jpeg)

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## Jet Propagation

M87 Chandra X-Ray

![](_page_39_Picture_2.jpeg)

![](_page_39_Picture_3.jpeg)

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## Jet Propagation

![](_page_40_Figure_1.jpeg)

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### Radio Source Diagnostics

![](_page_41_Figure_1.jpeg)

![](_page_41_Picture_2.jpeg)

Wise et al. (2013)

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- Spectral index maps over broad frequency range
- Determine spectral ageing of e- population
- Determine jet and lobe particle content
- Constrain strength and topology of B fields

![](_page_41_Picture_9.jpeg)

### Radio Galaxies: Outburst Lifecycle

![](_page_42_Figure_1.jpeg)

 Hydra A at 4500 MHz (inset) shows an FR-I morphology on scales of <1.5' (100 kpc)</li>

![](_page_42_Figure_3.jpeg)

New 74 and 330 MHz data show Hydra A is
> 8' (530 kpc) in extent with large outer
lobes surrounding the high frequency source

• Outer lobes have important implications for the radio source lifecycle and energy budget

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# Clusters of Galaxies

![](_page_43_Picture_1.jpeg)

![](_page_43_Picture_3.jpeg)

![](_page_44_Picture_0.jpeg)

z=20

z=0

z=10 z=5

z=50

z=1

Galaxy Cluster

Millennium Simulation Springel, Frenk & White (2006)

### Evidence for AGN Feedback

![](_page_45_Figure_1.jpeg)

![](_page_45_Picture_2.jpeg)

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#### Cluster-scale AGN Outbursts

 $M \sim 1.3$  shock

 $E = 10^{62} \text{ erg}$ 

Wise et al. (2013) McNamara et al. (2009, 2011) Gitti et al. (2007) McNamara et al. (2005) MS0735.6+7421 (z=0.216)

Radio plasma

Displaced X-ray gas

1' = 200 kpc .

Optical, Radio, X-ray

## The Feedback Sequence

![](_page_47_Figure_1.jpeg)

What produces the observed scatter? How do we extend this to high z?

![](_page_47_Figure_3.jpeg)

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# Lradio as proxy for Pcavity

![](_page_48_Figure_1.jpeg)

Bîrzan et al. (2008)

![](_page_48_Figure_3.jpeg)

- 24 cavity systems from Chandra Archive
- Low to moderate redshift (0.0035 < z < 0.545)

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- VLA data: 330 MHz, 1.4, 4.5, and 8.5 GHz
- Combine X-ray + Radio
- Depends on source extent

#### Calibrate at low-z $\Rightarrow$ Extrapolate to high z

## Trace History of AGN Output

Hydra A

Low frequency  $\Rightarrow$  integrated history t > 200 Myr

High frequency  $\Rightarrow$  recent activity  $t \sim 50 \text{ Myr}$ 

> Diffuse emission Steep spectrum

Traces integrated AGN output

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![](_page_49_Picture_8.jpeg)

Wise et al. (2007)

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0.5-7.0 keV

**330 MHz** 

**1.4 GHz** 

### AGN Duty Cycle and SMBH Growth

![](_page_50_Figure_1.jpeg)

![](_page_50_Figure_2.jpeg)

Blanton et al. (2007)

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![](_page_50_Figure_4.jpeg)

Clarke et al. (2007)

- Multiple cavities detected in X-ray maps
- Imply multiple AGN outbursts over ~200 Myr
- Limits on rate of BH growth:

$$\Delta M_{BH} = (1 - \epsilon) M_{ac}$$

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 $M_{acc} = \frac{E_{cav}}{cc^2}$ 

# Driving Shocks into ICM

![](_page_51_Picture_1.jpeg)

 Chandra X-ray emission detects shock front surrounding low frequency radio contours

 Expanding radio lobes drive the shock over last ~1.4x10<sup>8</sup> yr

 Total energy input significantly exceeds requirements to offset Xray cooling in cluster

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![](_page_51_Picture_7.jpeg)

## Driving Shocks into ICM

X-ray Temperature

Residuals + VLA

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![](_page_52_Picture_3.jpeg)

#### Hercules A

- Second most powerful AGN outburst known (E<sub>tot</sub> > 10<sup>61</sup> erg)
- Synchrotron power on par with Cygnus A, FRII-like
- Radio morphology is jet-dominated, no hotspots, FRI-like
- Spherical, M~1.6 shock surrounding the cavities

# Merger Calorimetry

![](_page_53_Figure_1.jpeg)

Several clusters display large regions of diffuse synchrotron:

- 'Halos' & 'relics' associated with merging clusters
- Radio emission is generally steep spectrum
- •RADIO RELICS: cluster outskirts, elongated morphology, polarized at the ~30% level
- RADIO HALOS: centrally located, regular structure similar to the X-ray morphology, unpolarized
- Location, morphology, spectral properties, etc... can be used to understand merger geometry and energetics

![](_page_53_Picture_10.jpeg)

# Sunyaev-Zel'dovitch Effect

![](_page_54_Figure_1.jpeg)

- Temperature shift proportional to gas pressure,
- CMB photon energies boosted by  $\sim kT_e/(m_ec^2)$
- kTe ~ 10 keV,Te ~ 108 K relativistic
- $x = h/(kT_e)$
- f(x) is the spectral dependence
- Notice that the T shift is redshift independent
- Unbiased surveys for clusters

$$\frac{\Delta T_{SZE}}{T_{CMB}} = f(x) \ y = f(x) \int n_e \frac{k_B T_e}{m_e c^2} \sigma_T \ d\ell,$$

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![](_page_54_Figure_12.jpeg)

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![](_page_55_Picture_0.jpeg)

![](_page_55_Picture_1.jpeg)

![](_page_55_Picture_3.jpeg)

#### Bullet Cluster, Clowe et al 2006, ApJ, 648, L109

# Tracing Dark Energy

![](_page_57_Figure_1.jpeg)

Observations of cosmic acceleration have led to studies of Dark Energy:

- Clusters should be representative samples of the matter density in the Universe
- Study DE through various methods including the 'baryonic mass fraction'
- Requires assumption of hydrostatic equilibrium
- Merging cluster can be identified and removed using low frequency detections of halos and relics (Clarke et al. 2005)

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Allen et al. (2004)

![](_page_57_Picture_9.jpeg)

## Cosmic Microwave Background

#### WMAP (20 - 100 GHz)

\* After subtracting off the emission from all the "foregrounds", find fluctuations of ~10<sup>-6</sup> K at ~0.25° resolution

![](_page_58_Picture_3.jpeg)

![](_page_58_Picture_5.jpeg)

### Planck Mission

![](_page_59_Picture_1.jpeg)

![](_page_59_Picture_2.jpeg)

**Resolution** ~ x5 better

![](_page_59_Picture_4.jpeg)

![](_page_59_Picture_6.jpeg)

### Planck Mission

![](_page_60_Figure_1.jpeg)

![](_page_60_Picture_2.jpeg)

![](_page_60_Picture_3.jpeg)

## High Redshift Galaxies

![](_page_61_Figure_1.jpeg)

Observations of cosmic acceleration have led to studies of Dark Energy:

• Synchrotron losses steepen the spectrum of radio galaxies at high z

• Inverse Compton losses act similarly to steepen the spectrum, especially at high z since IC losses scale as  $z^4$ .

• Spectrum is also red shifted to lower frequencies so that the entire observed spectrum is steep.

![](_page_61_Picture_6.jpeg)

![](_page_61_Picture_8.jpeg)

## Dark Ages

![](_page_62_Figure_1.jpeg)

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## Epoch of Reionization

![](_page_63_Figure_1.jpeg)

![](_page_63_Picture_2.jpeg)

Tozzi et al. (2000)

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 Hydrogen 21 cm line during EoR between z~6 (v ~ 200 MHz) and z~11 (v ~ 115 MHz)

EoR Intruments: MWA, LOFAR, 2 I CMA, PAPER, SKA

![](_page_63_Picture_6.jpeg)

## Structure Formation

![](_page_64_Figure_1.jpeg)

![](_page_64_Picture_2.jpeg)

Clarke & Ensslin (2006)

- Galaxy clusters form through mergers and are identified by large regions of diffuse synchrotron emission (halos and relics)
- Important for study of plasma microphysics, dark matter and dark energy

![](_page_64_Picture_6.jpeg)

![](_page_64_Picture_8.jpeg)

## Questions?

![](_page_65_Picture_1.jpeg)

![](_page_65_Picture_3.jpeg)