

# **Drifting subpulse phenomenon in pulsars**

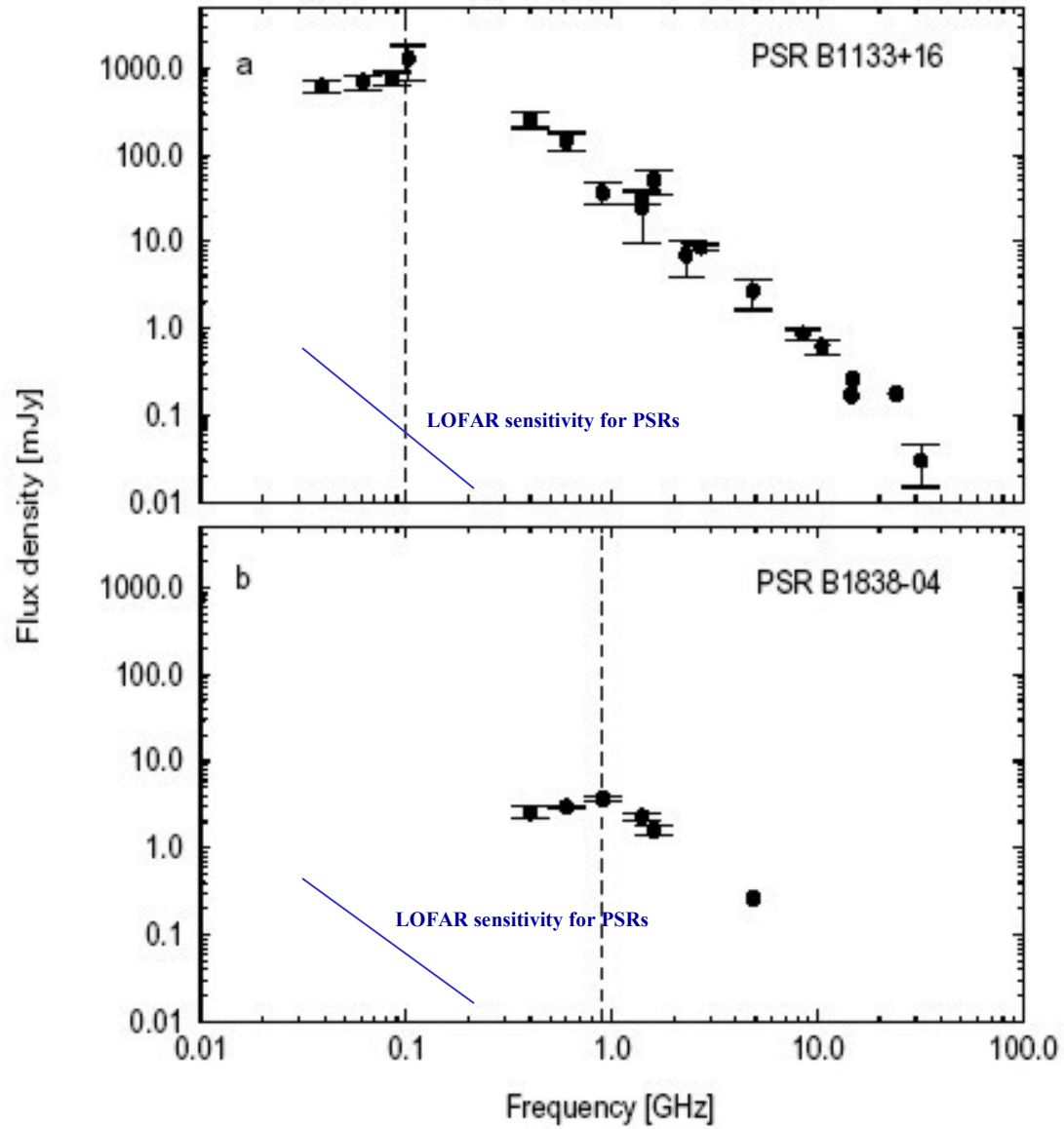
## **Lofar perspective**

**Janusz Gil**

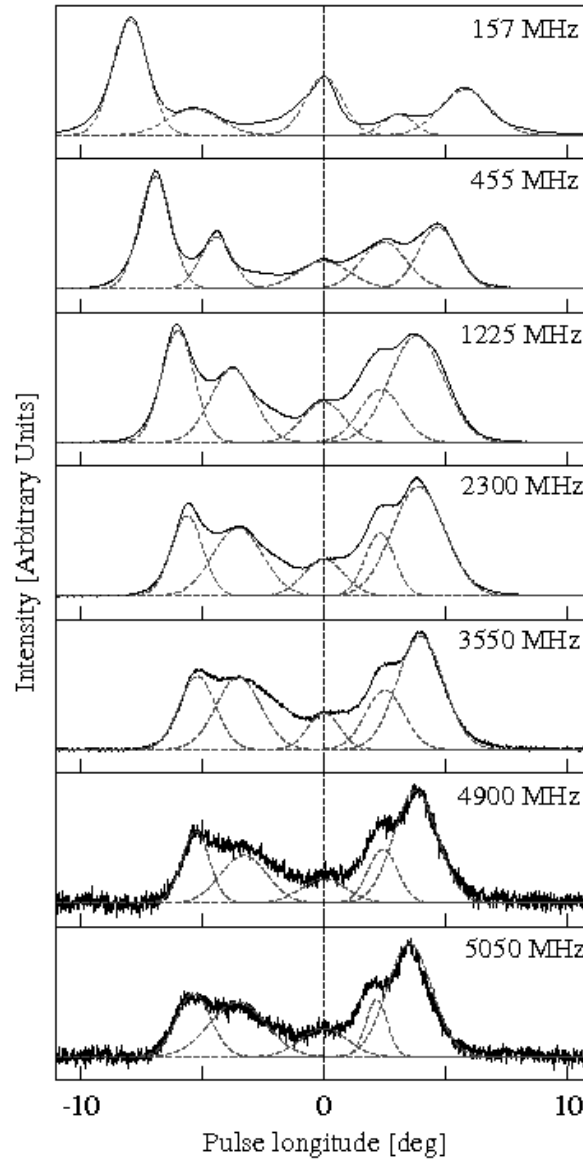
**J. Kepler Astronomical Institute  
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**Collaborators:**

**G. Melikidze, B. Zhang, U. Geppert, F. Haberl, J. Kijak, M. Sendyk**



B1237+35



**Broadening of the profile  
As frequency decreases**

**Evidence of the radius-to-frequency mapping  
and dipolar nature of magnetic field lines  
in the emission region**

**Sensitive observations below 160 MHz would be  
highly desirable**

**40 years after discovery of pulsars the actual mechanism of their coherent radio emission is still a mystery.**

**Drifting subpulses, which seem to be a common phenomenon in pulsar radiation, is also a puzzle.**

***„The mechanism for drifting subpulses cannot be very different from the mechanism of observed radio emission ...***

***...intrinsic property of radiation mechanism ,,  
(Weltevrede, Edwards & Stappers 2006, A&A 445,243)***

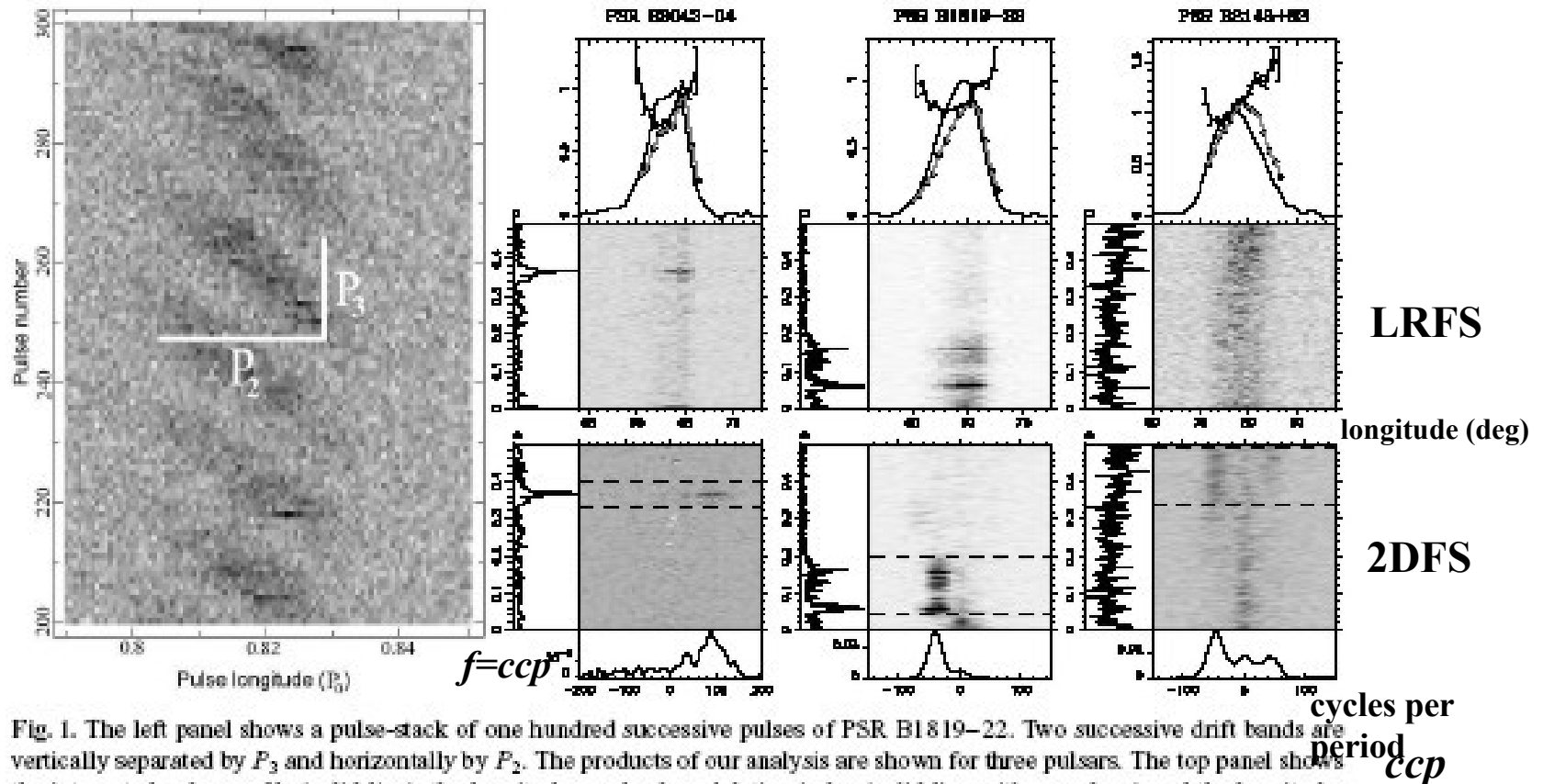


Fig. 1. The left panel shows a pulse-stack of one hundred successive pulses of PSR B1819–22. Two successive drift bands are vertically separated by  $P_3$  and horizontally by  $P_2$ . The products of our analysis are shown for three pulsars. The top panel shows the integrated pulse profile (solid line), the longitude-resolved modulation index (solid line with error bars) and the longitude-resolved standard deviation (open circles). Below this panel the LRFS is shown with on its horizontal axis the pulse longitude in degrees, which is also the scale for the abscissa of the plot above. Below the LRFS the 2DFS is plotted and the power in the 2DFS is vertically integrated between the dashed lines, producing the bottom plots. Both the LRFS and 2DFS are horizontally integrated, producing the side-panels of the spectra. See the main text for further details about the plots.

**LRFS - Longitude Resolved Fluctuation Spectrum**

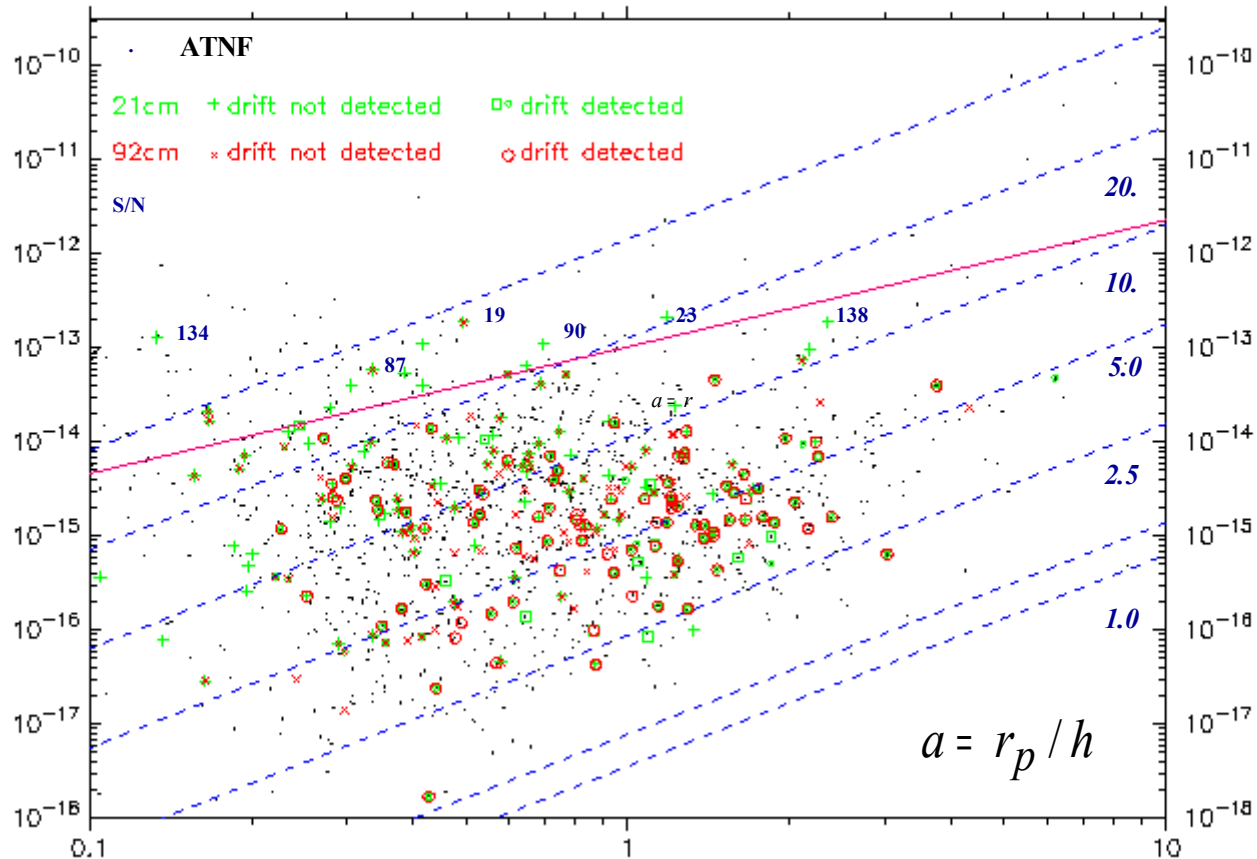
**2DFS - Two Dimensional Fluctuation Spectrum – calculated along various slopes**

$$P_2 = \pm P / ccp$$

# Unbiased search for drifting subpulses in 187 (191) pulsars

About 55 % (more) of drifting subpulse pulsars

Weltevrede, Edwards & Stappers et al. 2006, 2007



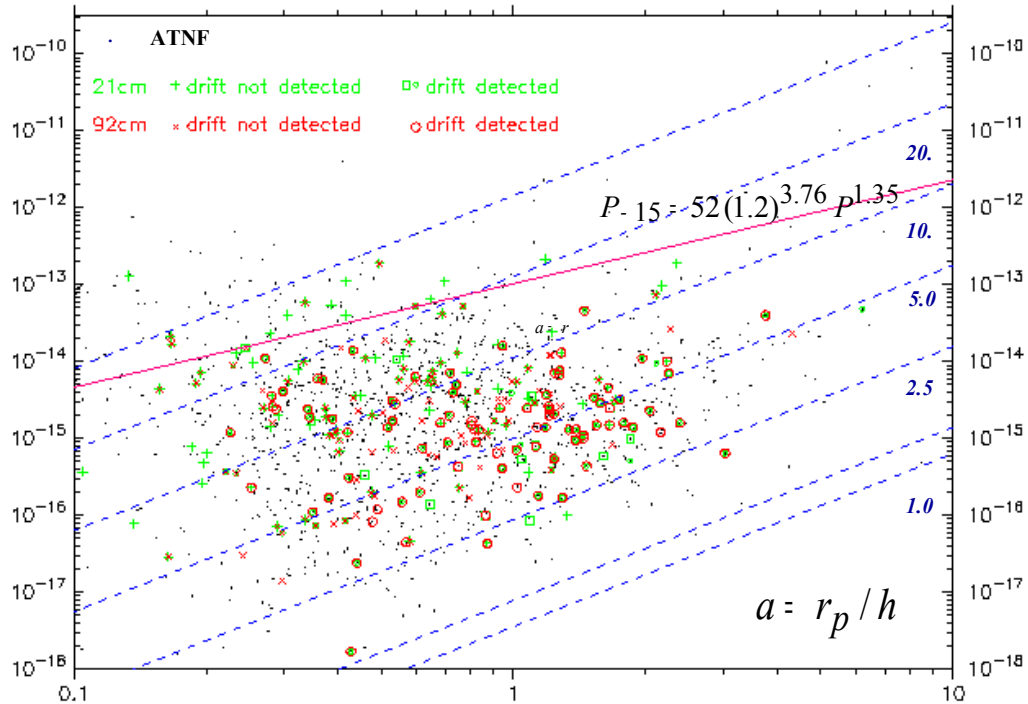
At frequencies lower than 320 MHz (LOFAR range) the ratio of detected drifting subpulses should be even higher



# Unbiased search for drifting subpulses in 187 (191) pulsars

About 55 % (more) of drifting subpulse pulsars

Weltevrede et al. 2006, 2007



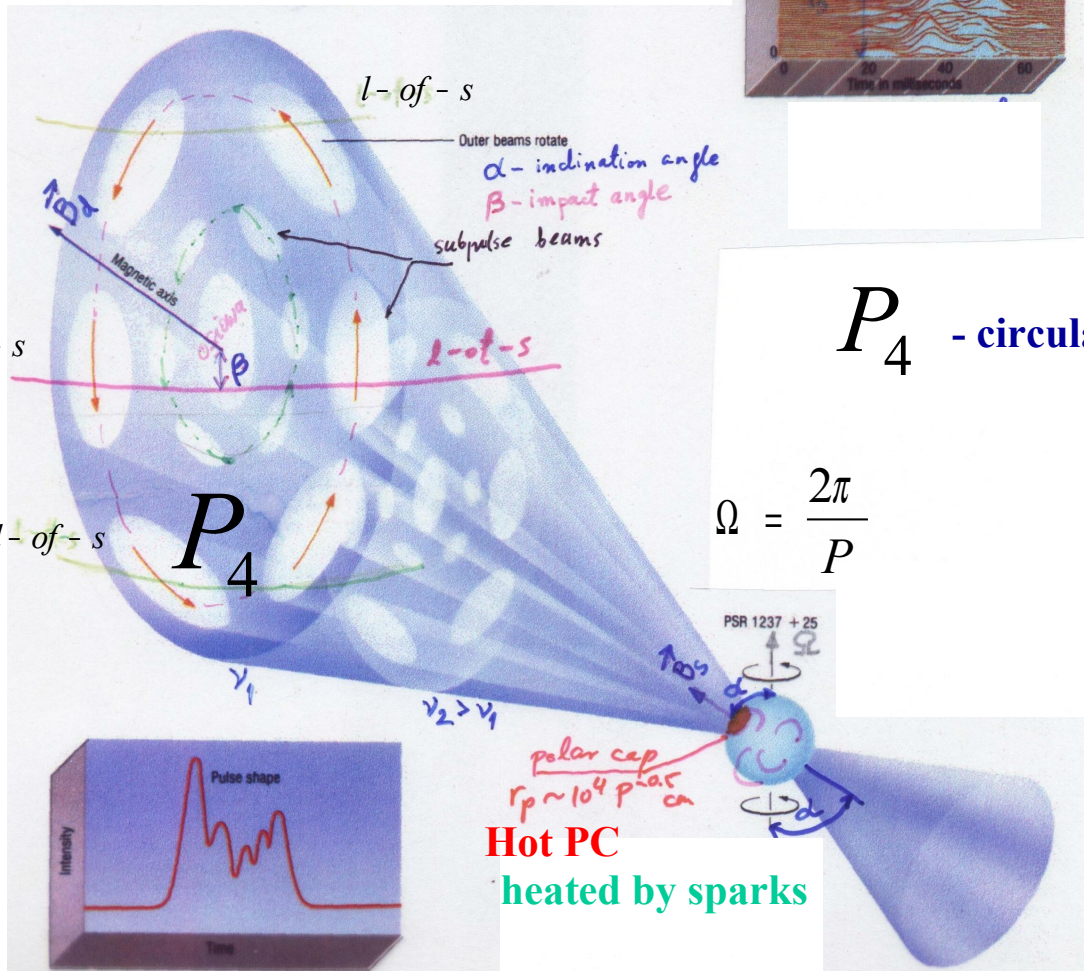
*Lorentz factor*

$$\gamma = 120$$



# Carousel model

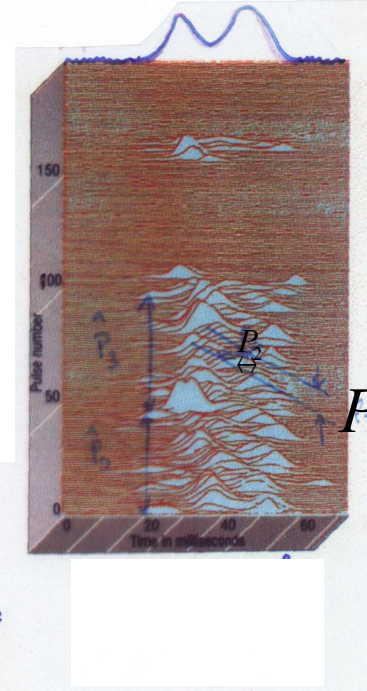
Sub-beams of radio emission presumably related to sparks operating just above the Polar Cap circulate around the magnetic axis



## Subpulse drift

Subpulses in subsequent pulses arrive in phases determined by the apparent drift rate

$$D = P_2 / P_3$$

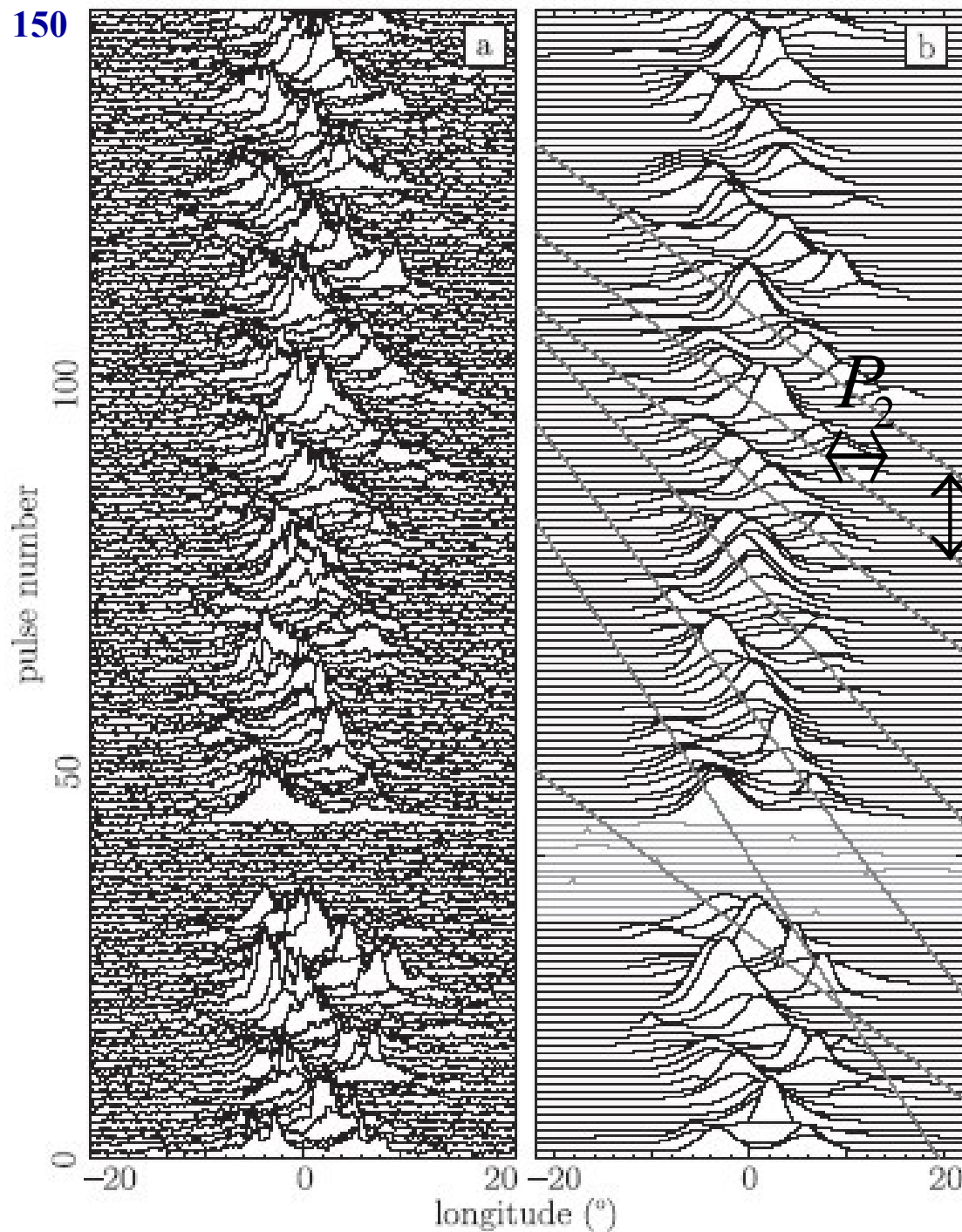


$P_4$  - circuational periodicity ?

$$\Omega = \frac{2\pi}{P}$$

## Polar cap

$$r_{pc} = 1.45 \times 10^4 P^{-0.5} \text{ cm}$$



## PSR B0809+74

Perhaps the best example of  
*Drifting subpulses*  
phenomenon in pulsars

*Apparent subpulse drift-bands*

$$P_3 \approx 11P$$

Modulation of intensity along  
drift-bands consistent with  
carousel model

*that is*

Sub-beams continue  
to circulate beyond  
the observed pulse-window

(after van Leuven, Stappers et al.)

## B0818-41

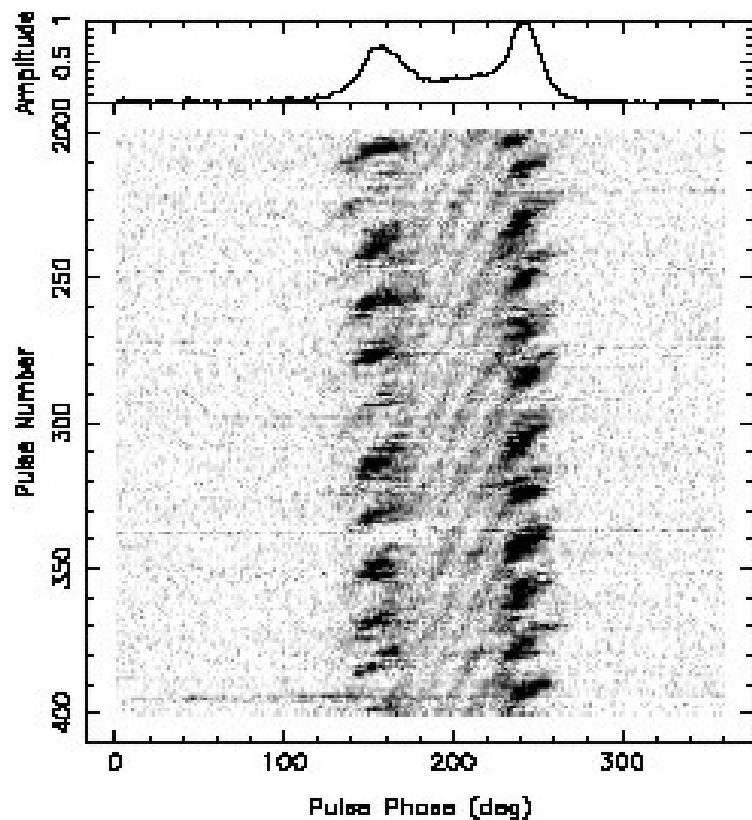
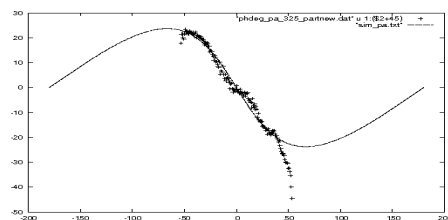
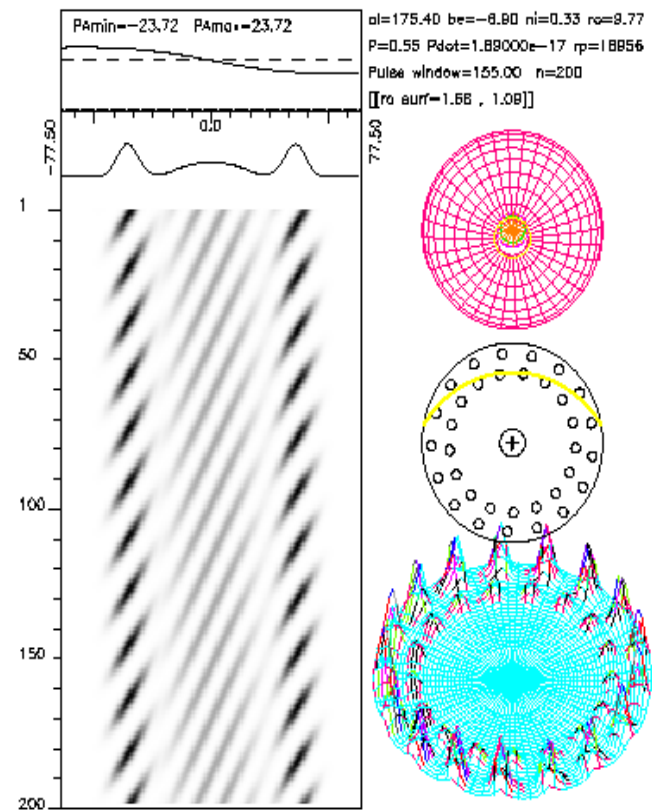


Figure 2. Grey-scale plot of single-pulse data (pulse # 200 to 400) of PSR B0818-41 at 325 MHz, with the average profile shown on top. Signatures of radio frequency interference are present around pulse numbers 220, 298, 338 and 397.



$$\alpha = 175^\circ$$

$$\beta = 7^\circ$$

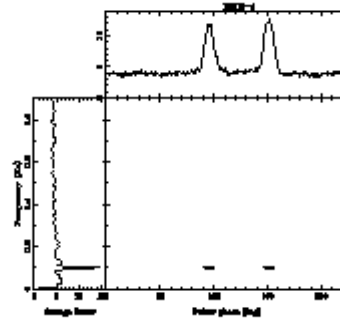


Figure 17: The contour plot of the power spectrum of the flux at 325 MHz as a function of phase (longitude) during a sequence of 200 pulses (pulse # 200-400). The left panel shows the power spectrum integrated over longitude. The upper panel shows the power integrated over frequency.

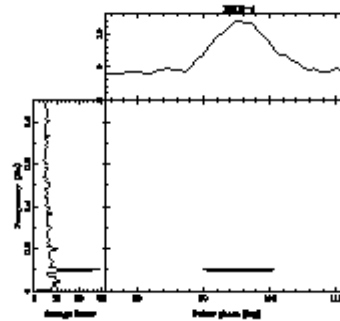


Figure 18: The contour plot of the power spectrum of the flux at 325 MHz as a function of phase (longitude) during a sequence of 200 pulses (pulse # 200-400), for the component 1 (line number 89-132). The left panel shows the power spectrum integrated over longitude. The upper panel shows the power integrated over frequency.

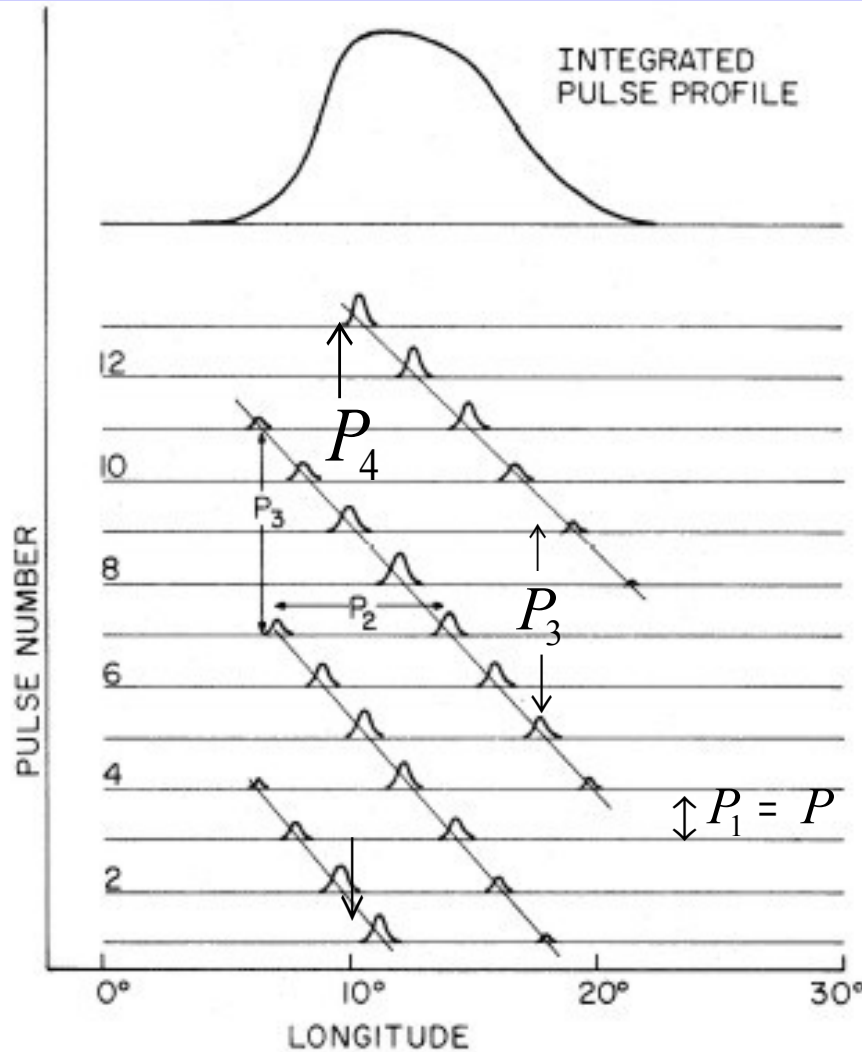


FIG. 5.—Schematic (after Backer 1973) of integrated pulse profile, arrival times of individual pulses, and definition of  $P_2, P_3$  for those pulsars showing the “drifting subpulse” phenomenon. Arrival times of individual pulses are given in terms of a longitude for which  $360^\circ$  corresponds to the full pulsar period.

$$P_1, P_2, P_3, P_4$$

Apparent drift rate  $D = P_2 / P_3$

$P_2$  distance between driftbands in longitude

$P_3$  distance between driftbands in  $P_1$

Intrinsic drift rate  $P_4 = P_3 N$

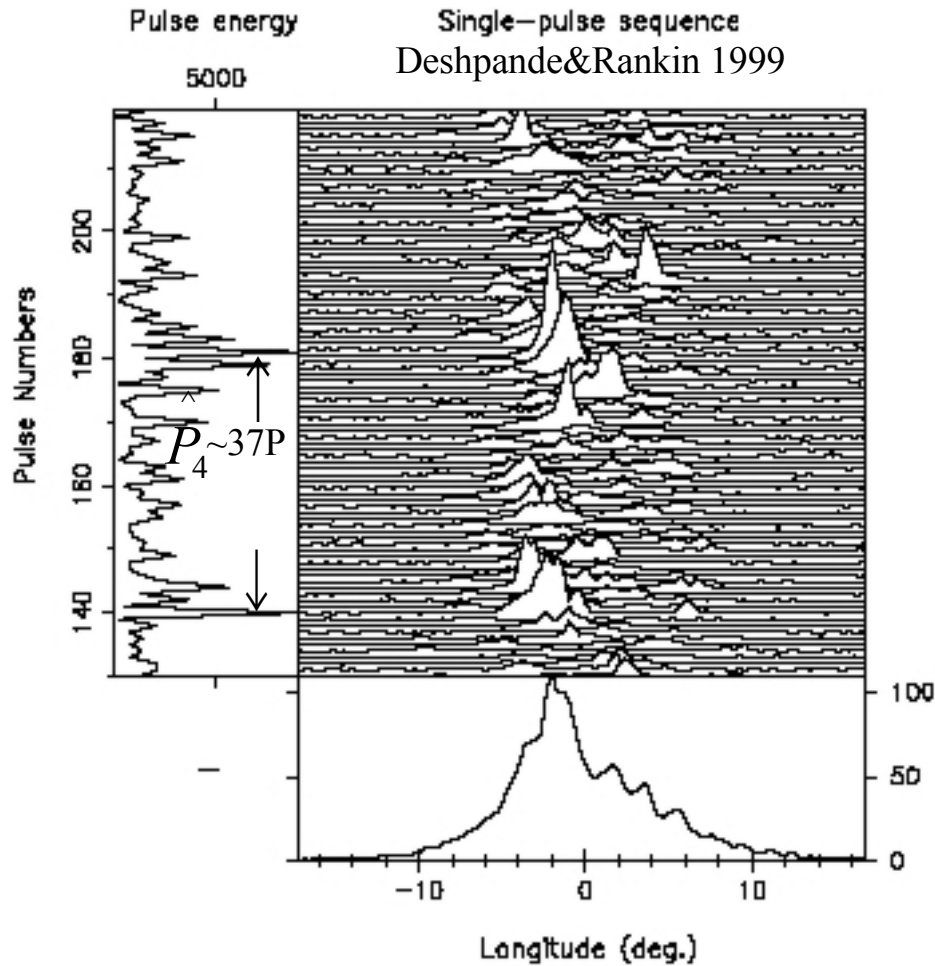
$N$  number of rotating sub-beams

$P_4$  distance between the same driftbands

$P_4$  time interval to complete one rotation around the pole

**very difficult to measure, only 8 cases known !!!**

# PSR B0943+10



$$P = 1.089 \text{ s}$$

$$P_3 = 1.87P$$

$$P_4 = 37.35P$$

Number of sub-beams  
circulating around B

$$N = P_4 / P_3 = 20$$

# PSR B0943+10

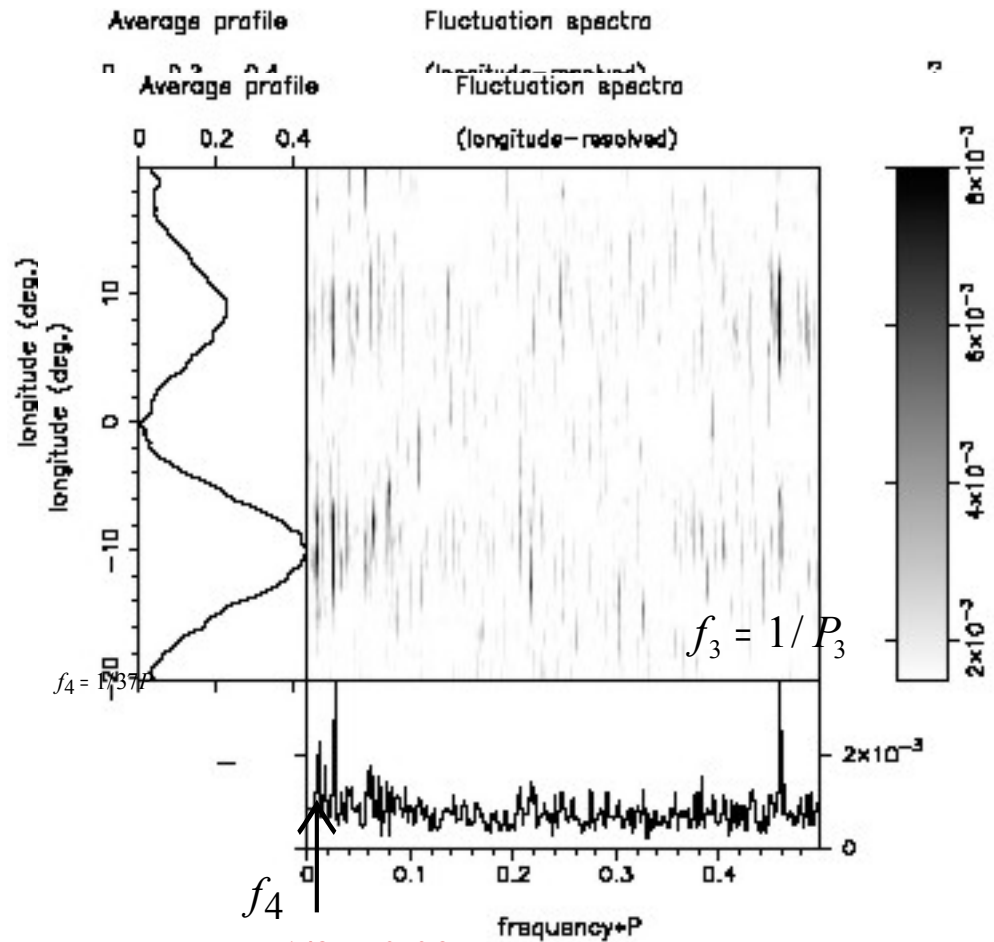
35 MHz observations  $f_4$   
Asgekar & Deshpande 2001

430 MHz observations  $f_3$   
Deshpande & Rankin

## Phased-resolved fluctuation spectrum

$$P_4 = 37.35 P = 41\text{s.}$$

Spectral analysis fully consistent with „carousel model”. Sub-beams continue to circulate around the beam axis beyond the pulse-window and reappear after the period needed to complete one full circulation around the magnetic axis



$$1/37 = 0.027$$

$$N = P_4 / P_3 = \frac{37.35}{1.87} = 20$$

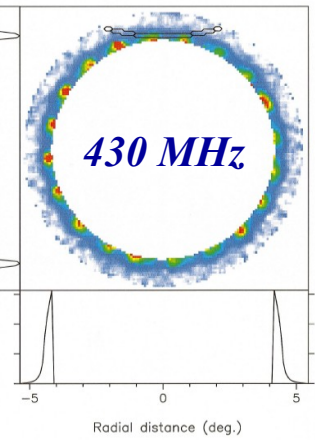
Low frequency observations (LOFAR range) are more sensitive to low frequency modulations possibly related to the „carousel” circulation times

# Radius-to-frequency mapping

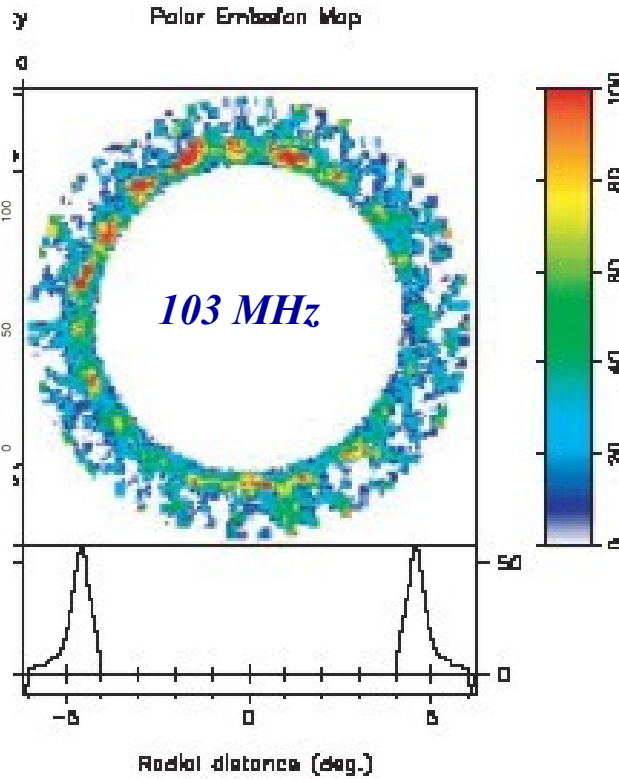
## Frequency dependent beam size

PSR B0943+10

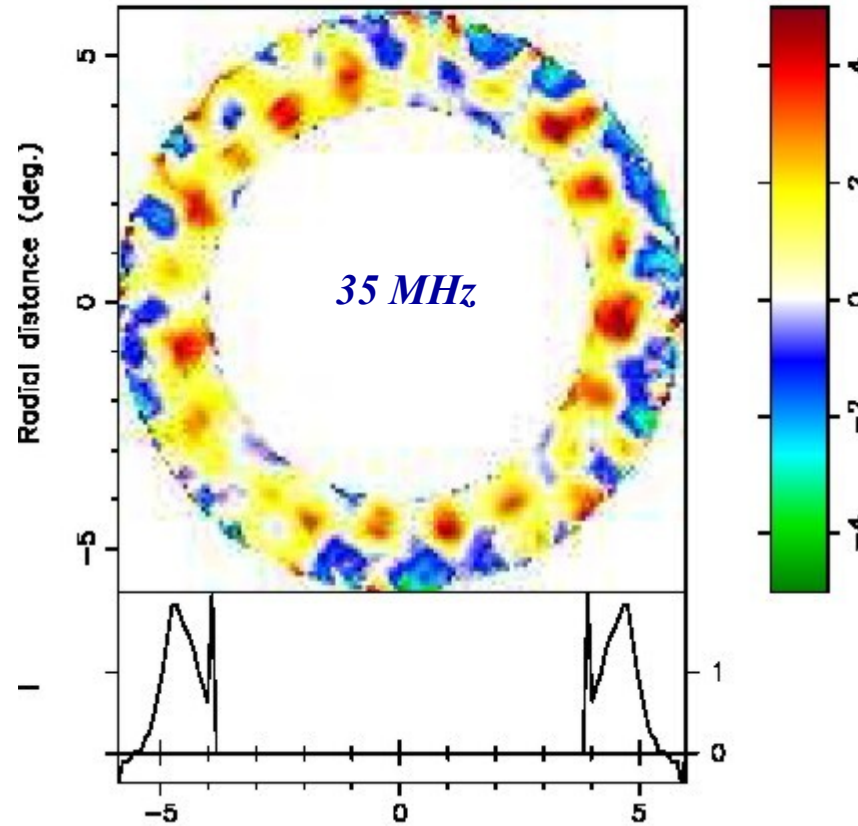
Polar Emission Map



Arecibo



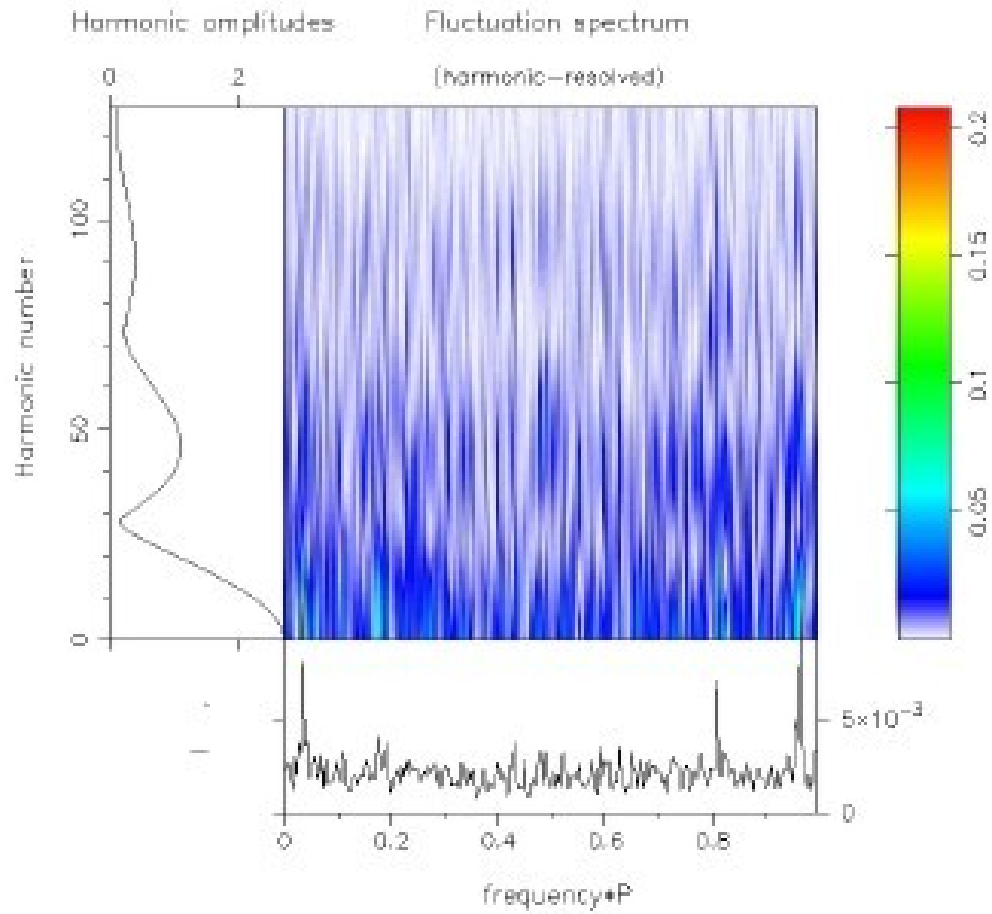
PRAO



Gauribidanur



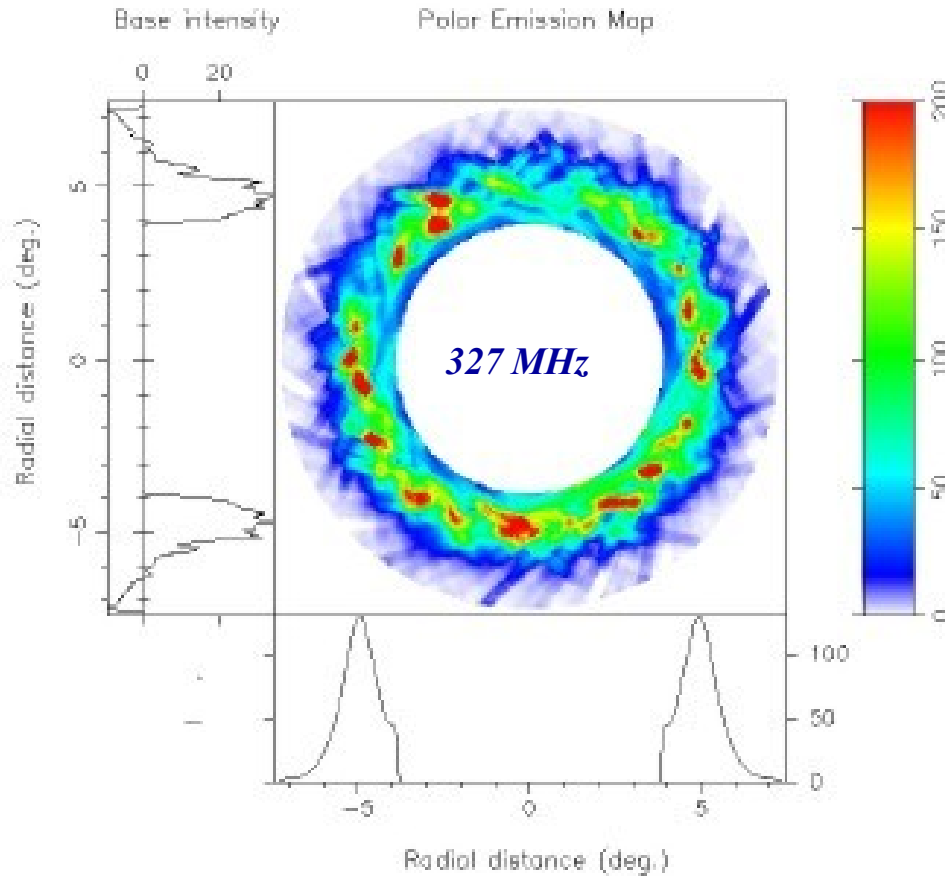
**B1133+16**



**Arecibo 327 MHz**

**Rankin et al. 2007**

## B1133+16



$$P = 1.19s$$

$$P_{-15} = 3.7$$

$$E = 9 \cdot 10^{31} \text{ erg / s}$$

$$P_3 = 1.237 P$$

$$P_4 = 28.44 P$$

$$N = P_4 / P_3 = 22$$

*Arecibo Observatory*

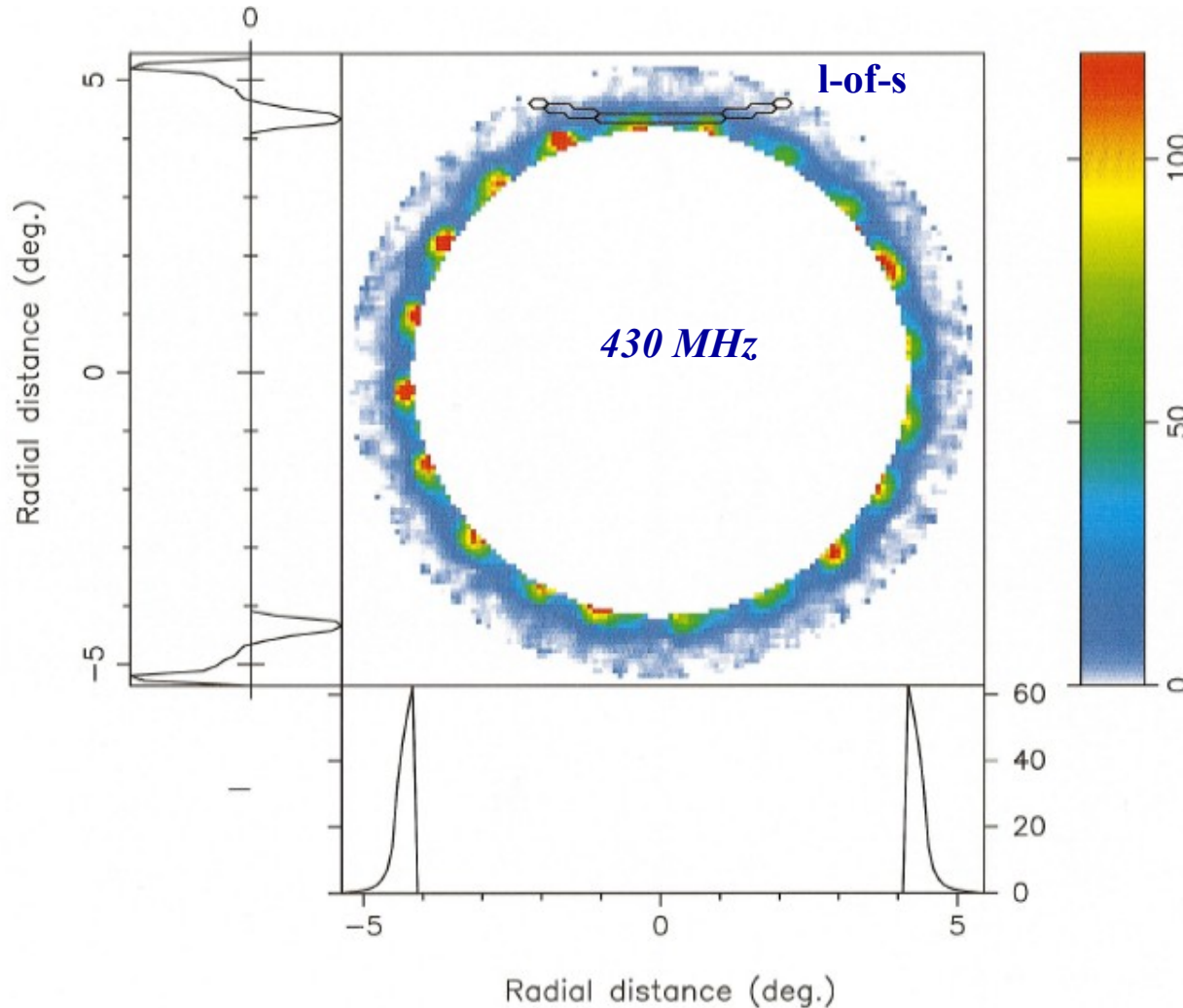
Rankin et al. 2007

327 MHz

**B0943+10**

Cartographic map of 20 subpulse beams „circulating” around the pole in about 37 pulsar periods

Deshpande & Rankin, 1999



$$P = 1.098 \text{ s}$$

$$P_{-15} = 3.52$$

$$E = 10^{32} \text{ erg/s}$$

$$P_3 = 1.86 P$$

$$P_4 = 37.35 P$$

$$N = P_4 / P_3 = 20$$

$\alpha, \beta$  Pulsar geometry known

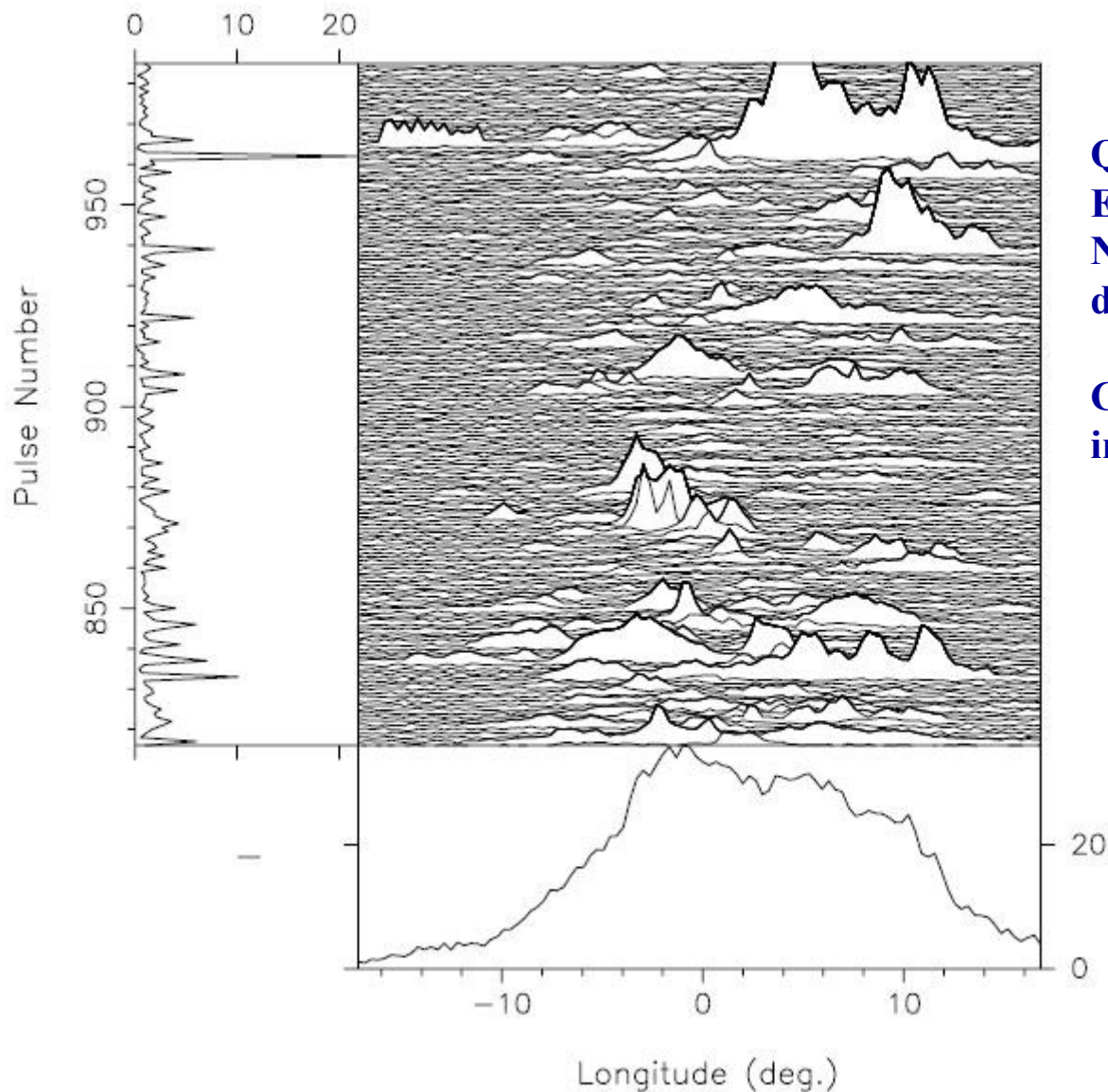
(Intensity; pulse longitude and pulse number)  $\rightarrow$  (Intensity; polar colatitude and azimuth)

Clear manifestation of subpulse sub-beams circulating around the magnetic axis

Average Flux

Single-pulse sequence

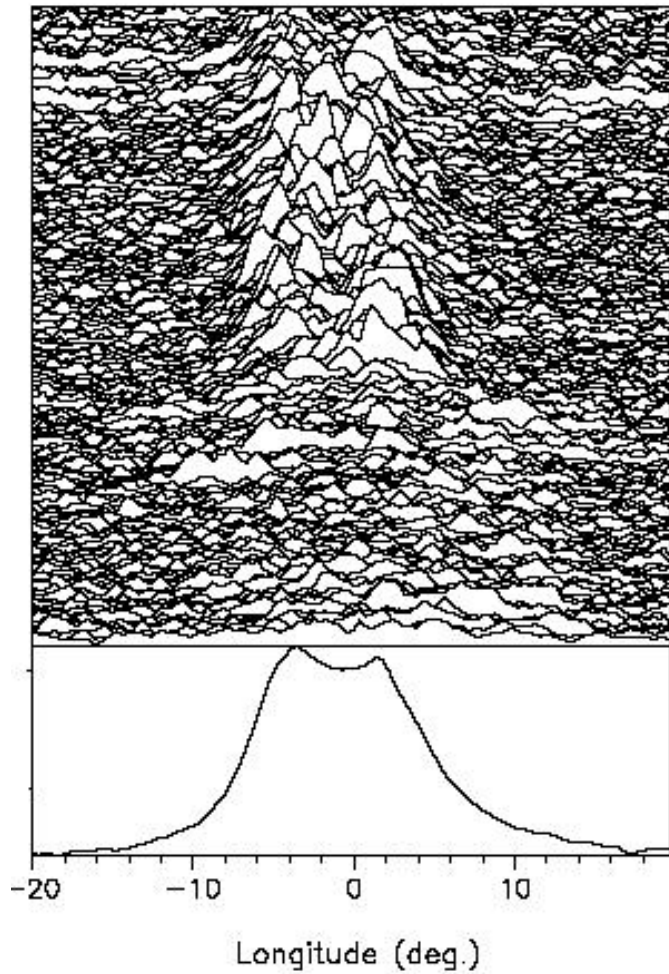
**B0943+10 430 MHz**



**Q-mode**  
**Erratic**  
**No organized**  
**drift visible**

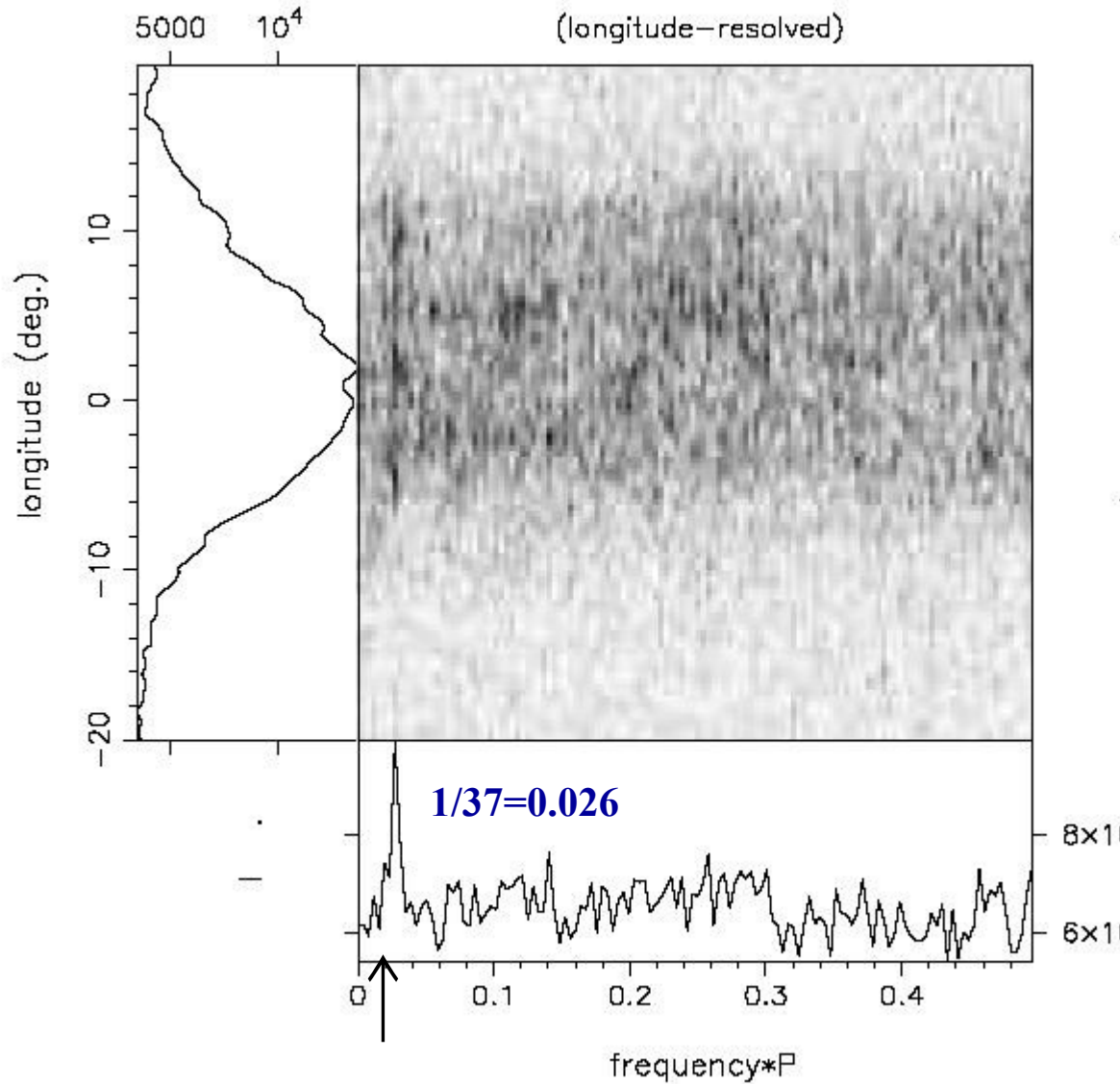
**Cartographic map**  
**impossible to make**

103 MHz



**B0943+10 Q-mode (erratic)**

**Suleymanova & Rankin 2006**



**Clear feature at 37 P as in the B-mode**

**Spark plasma circulates around the local magnetic pole on the Polar Cap with a specific period  $P_4$ , regardless it is fragmented into equally spaced filaments or operates in much less organized manner.**

**One cannot switch off the  $E \times B$  drift, except when there is no  $E$  or  $B$ .**

# Natural mechanism of subpulse drift

$E \times B$

Natural state of the magnetospheric plasma frozen into electric and magnetic field is corotation with NS (global corotation)

$$v_{cor} = c(E_c \times B_s) / B^2 = cE_c / B_s \quad \Leftrightarrow \quad \rho = \rho_{GJ} \quad \text{corotation}$$

$$\text{if } E \neq E_c \text{ then } v \neq v_{cor} \quad \Leftrightarrow \quad \rho \neq \rho_{GJ} \quad \text{Polar Gap charge depletion}$$

Non-corotation plasma lags behind pulsar rotation and drifts with respects the polar cap surface with velocity  $v_{dr}$

$$v_{dr} = c(\Delta E \times B_s) / B^2 = c\Delta E / B_s$$

$$\Delta E \quad \text{Electric field associated with charge depletion} \quad \Delta \rho = \rho_{GJ} - \rho$$

If plasma has transversal structure (spark filaments) then this **inevitable**

$\Delta E \times B$  drift should be observed in the form of drifting subpulses, and/or specific features in the intensity fluctuation spectrum

# $\overrightarrow{\Delta E} \times \overrightarrow{B}$ spark plasma circulation drift rate

## Linear velocity of the $E \times B$ drift (RS75)

$$v_d = \frac{c\Delta E}{B_s} = \frac{c\eta (2\pi / cP) B_s h}{B_s} = \eta \frac{2\pi}{P} h \text{ [cm/s]}$$

$B_s$  -actual surface magnetic field  
 $B_d$  -dipolar magnetic field at PC

$\Delta E$  - component of electric field caused by charge depletion  $\Delta \rho = \rho_{GJ} - \rho_{th} = \eta \rho_{GJ}$

$$\omega = v_d / d = \eta (2\pi / P)(h / d) \quad \text{Carousel angular speed}$$

## Time interval to complete one circulation around periphery of PC

$$P_4 = \frac{P}{2\eta} \frac{d}{h} \leq \frac{P}{2\eta} \frac{r_p}{h}$$

Gil, Melikidze  
& Geppert 2003



**Within the model of the inner acceleration region to surface of the PC is heated to high temperatures by the back-flow of particles produced in sparking discharges.**

**The heating rate is determined by the same value of the electric field that is involved in the E x B drifting phenomenon.**

**thus, the observed drifting rate**

$$P_4 = 2\pi d / v_d = \frac{P}{2\eta} \frac{d}{h} \leq \frac{P}{2\eta} \frac{r_p}{h}$$

**and the observed heating rate (thermal X-ray luminosity from hot PC)**

$$L_x = \sigma T_s^4 A_{bol} = \sigma T_s^4 A_{pc} (B_d / B_s)$$

**should be strongly correlated.**

## Thermal X-ray luminosity from spark-heated polar cap

$$L_x = 2.5 \times 10^{31} \times (\dot{P}_{-15} / P^3) (P_4 / P)^{-2} \text{ erg/s}$$

Efficiency

$$L_x / \dot{E} = (0.63 / I_{45}) (P_4 / P)^{-2}$$

$$\dot{E} = I \dot{\Omega} \dot{\Omega}$$

Spin-down power

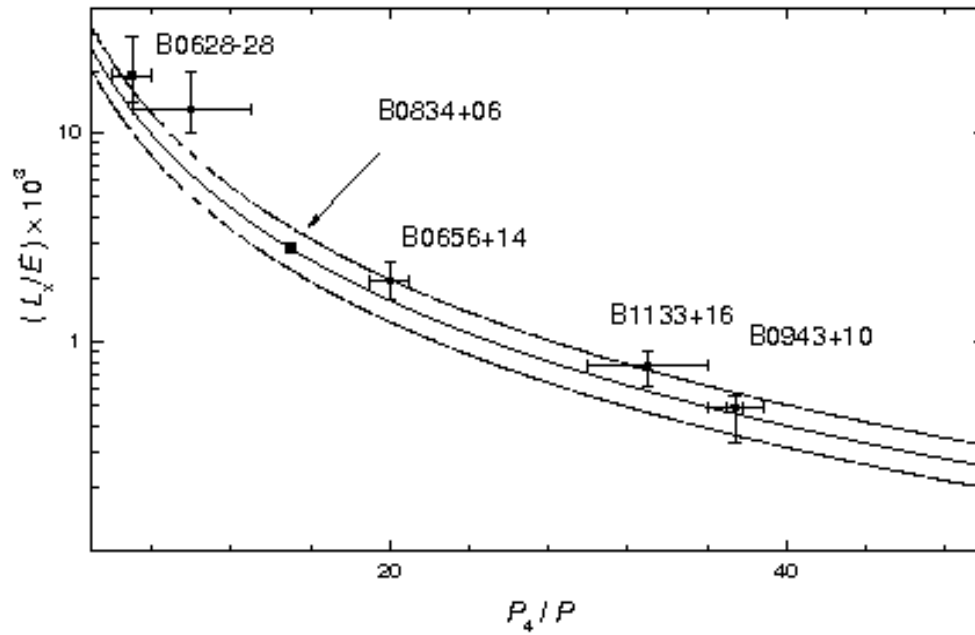
$$I = I_{45} 10^{45} \text{ g cm}^2$$

$$I_{45} = 1 \pm 0.15$$

## **X-ray Multi Mirror (XMM) – Newton satellite telescope**



**One revolution on an excentric orbit around the Earth takes 48 hours – observations are not performed close to the Earth due to strong noise contamination**



$$I_{45} = 1 \pm 0.15$$

$$L_x / E = (0.63 / I_{45}) (P_4 / P)^{-2}$$

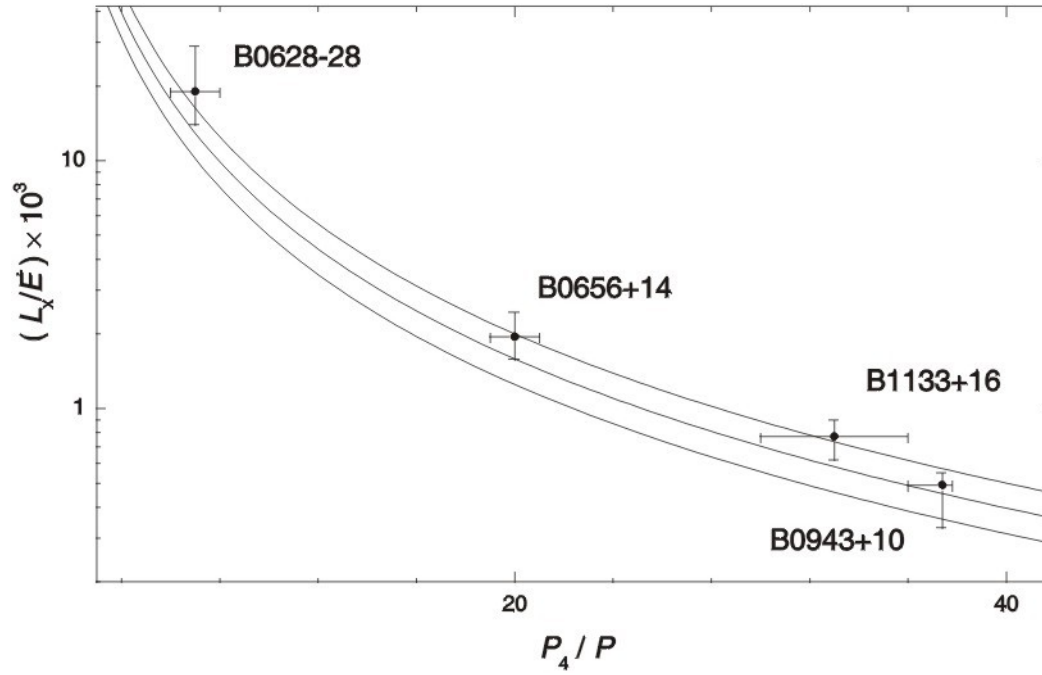
Further low frequency LOFAR observation using 2DFS techniques should result in

Detection more drifting subpulse pulsars and possible more determination of  $P_4$   
In nearby pulsars, in which thermal X-ray component from hot polar cap can be determined. Then the polar gap relationship  $L_x \propto P_4^{-2}$  can be tested further.



B0628-28  $L_x=2.78 \times 10^{30}$  erg/s  $E_{\dot{}}=1.5 \times 10^{32}$  erg/s  $\rightarrow P_4=6 P$

Weltevrede et al.2006  $P_3=(7\pm 1) P \rightarrow P_4=P_3$



# Ruderman & Sutherland 1975

## Pure vacuum gap

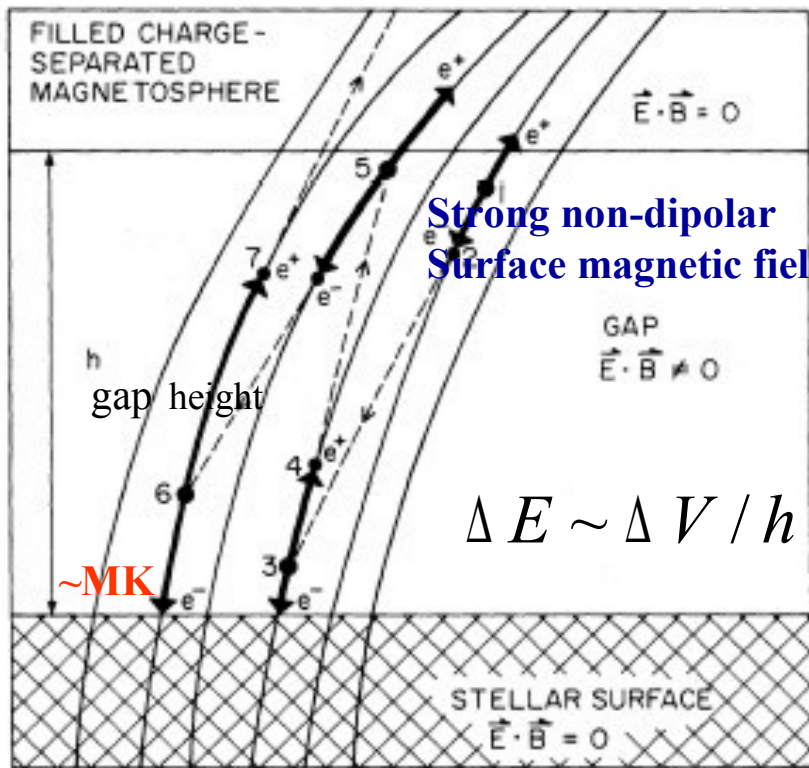
Charge depletion maximum possible  $\Delta \rho = \rho_{GJ}$

Very strong electric field  $\Delta E$

$\Delta E \times B$  drift much too fast as compared with observations

Polar cap heating too intense and subpulse drift was too fast as compared with observations

**Modification needed**



Within the acceleration region the spark generated positrons are moving towards the magnetosphere while back-flow of electrons bombard the polar cap surface and heat it to MK temperatures



# Future work

**New XMM-Newton observations of PSR B0826-34**

**50 Ks performed in November 2006**

**Zhang, Gil, Melikidze, Geppert, Haberl**

*Non-detected*                       $P_4 / P = 14 \pm 1$                       (Gupta, Gil, Kijak, Sendyk 2004)

**Proposal for XMM-Newton observations of**

**PSR B0834+06 accepted – observation in summer 2006**

(simultaneous radio observations with GMRT planned)

*Very promising*                       $P_4 / P = 15 \pm 1$                       (Asgekar, Deshapande 2005)

**Proposal for XMM-Newton observations of PSR B1702-19**

**will be submitted for the next cycle**

*Very promising*                       $P_4 / P = 10 \pm 1$                       (Weltevrede 2006; GMRT planned)

## Co-rotating magnetosphere

$$E_c = - (\Omega \times r / c) \times B_s$$

Force-free magnetosphere

$$E_c \cdot B_s = 0 \quad \Delta V_{\parallel} = 0$$

No acceleration along  $B$  GJ69, RS75

$$\rho_c = (1 / 2\pi) \operatorname{div} E_c =$$
$$= - \Omega \cdot B_s / (2\pi c) = \pm B_s / cP$$

Co-rotating charge density

$$v_{cor} = c(E_c \times B_s) / B^2 = cE_c / B_s$$

Linear co-rotation velocity

Name	$\hat{P}_3/P$		$L_x/\dot{E} \times 10^{-3}$		$L_x \times 10^{28}$		$b$	$T_s^{(obs)}$	$T_s^{(pred)}$	$B_d$	$B_e$
PSR B	Obs.	Pred.	Obs.	Pred.	Obs.	Pred.	$A_{pc}/A_{bol}$	$10^6$ K	$10^8$ K	$10^{12}$ G	$10^{14}$ G
0943 + 10	37.4	37	$0.5^{+0.2}_{-0.2}$	0.46	$5^{+2}_{-2}$	4.8	$60^{+140}_{-48}$	$3.1^{+0.9}_{-1.1}$	$3^{+1}_{-1}$	3.95	$2.37^{+5.53}_{-1.90}$
1133 + 16	$(33^{+3}_{\circ})$	$31^{+3}_{\circ}$	$0.77^{+0.13}_{-0.12}$	$1.0^{+0.3}_{\circ}$	$7.7^{+1.3}_{-1.2}$	$8.9^{+1.3}_{-1.2}$	$11.1^{+16.6}_{-5.2}$	$2.8^{+1.2}_{-1.2}$	$2.4^{+0.8}_{-0.7}$	4.25	$0.47^{+0.71}_{-0.34}$

**The only two cases existing with both measurements**

<b>B1133+16</b>	$L_x / \dot{E} \sim 0.77 \times 10^{-3}$	$\hat{P}_3 / P \sim 33$
<b>B0943+10</b>	$L_x / \dot{E} \sim 0.5 \times 10^{-3}$	$\hat{P}_3 / P \sim 37$

# Gil, Melikidze & Zhang 2006

$$\eta = (1/2\pi)(P/P_3)$$

Screening factor  $\sim(0.05-0.1)$

only few % of GJ plasma involved in acceleration

$$L_x = 2.9 \times 10^{31} \times (\dot{P}_{-15}/P^3)(\hat{P}_3/P)^{-2} \text{ erg/s}$$

X-ray bolometric  
luminosity  
 $10^{(28-29)} \text{ erg/s}$

$$L_x / \dot{E} = 0.63 (\hat{P}_3/P)^{-2}$$

Efficiency  $\sim$   
0.001

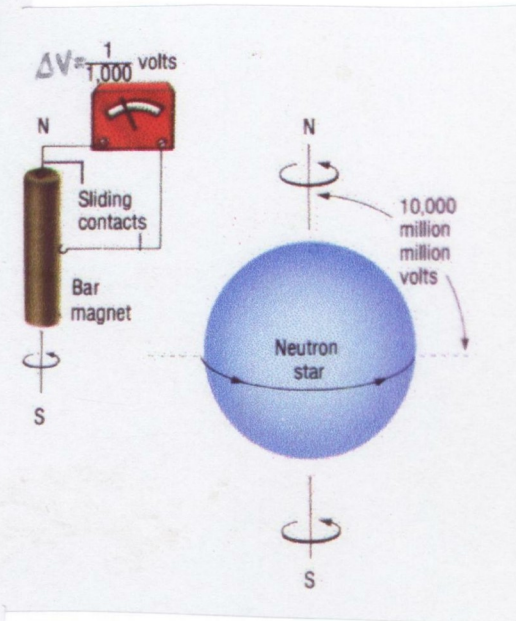
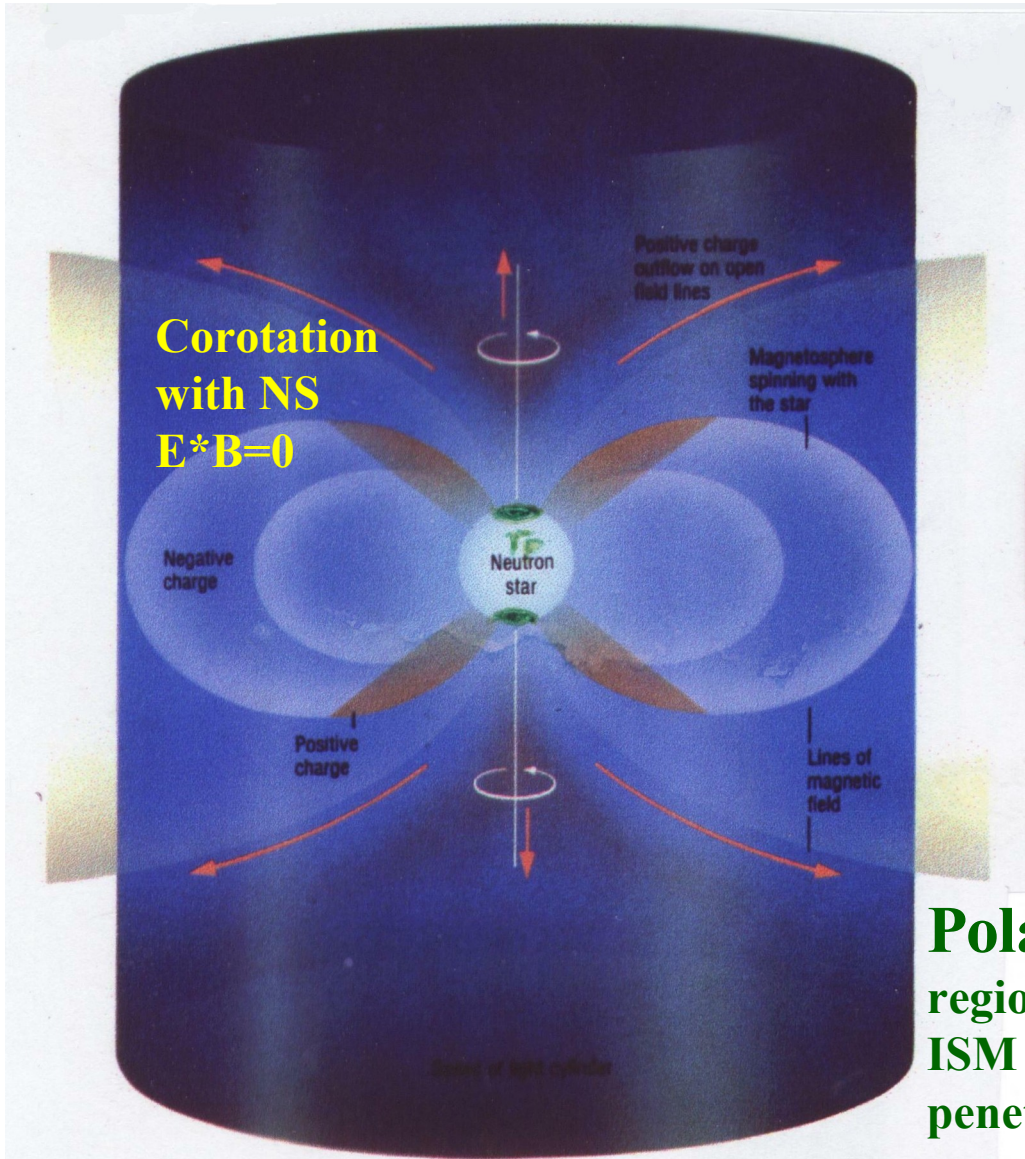
$$T_s = (8.2 \times 10^6 \text{ K}) A_4^{-0.25} \dot{P}_{-15}^{0.25} P^{-0.75} (\hat{P}_3/P)^{-0.5}$$

$$A_4 = A_{bol}/(10^4 \text{ m}^2) \sim 0.1$$

$$T_s \sim (2-3) \text{ MK}$$

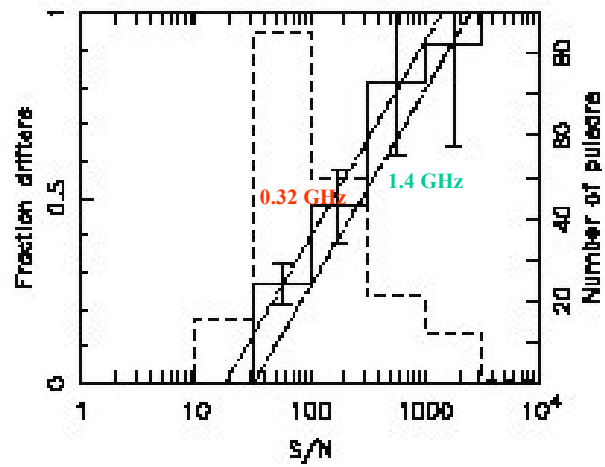
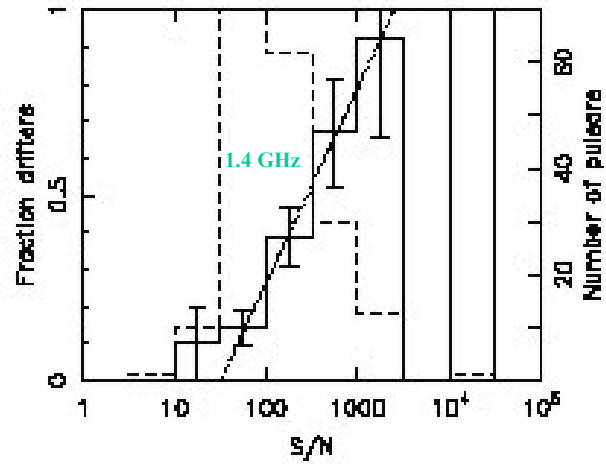
Name PSR B	$\hat{P}_3/P$		$L_x/\dot{E} \times 10^{-3}$		$L_x \times 10^{28}$		$b$ $A_{pc}/A_{bol}$	$T_s^{(obs)}$	$T_s^{(pred)}$	$B_d$ $10^{12} \text{ G}$	$B_s$ $10^{14} \text{ G}$
	Obs.	Pred.	Obs.	Pred.	Obs.	Pred.		$10^6 \text{ K}$	$10^6 \text{ K}$		
0943 + 10	37.4	37	$0.5^{+0.2}_{-0.2}$	0.46	$5^{+2}_{-2}$	4.8	$60^{+140}_{-48}$	$3.1^{+0.9}_{-1.1}$	$3^{+1}_{-1}$	3.95	$2.37^{+5.53}_{-1.90}$
1133 + 16	$(33^{+3}_{-3})$	$31^{+3}_{-2}$	$0.77^{+0.13}_{-0.18}$	$1.0^{+0.3}_{-0.2}$	$7.7^{+1.3}_{-1.3}$	$8.9^{+1.3}_{-1.8}$	$11.1^{+16.6}_{-5.6}$	$2.8^{+1.2}_{-1.2}$	$2.4^{+0.8}_{-0.5}$	4.25	$0.47^{+0.71}_{-0.24}$
0826 - 34	$14^{+1}_{-1}$			$3.2^{+0.5}_{-0.4}$		$2.0^{+0.33}_{-0.25}$				2.74	
0834 + 06	15			2.8		37				5.94	

**Pulsars are fast rotating and strongly magnetized Neutron Stars (NS)**



**Polar Cap (PC)**  
 region of NS surface connected to ISM via open magnetic field lines penetrating the Light Cylinder

Charged particles will leave through LC due to inertia and create charge depletion just above the PC. If this charge cannot be re-supplied by the PC surface (strong binding) then huge accelerating potential drop will occur along the open magnetic field lines close to the PC surface.



Weltevrede, Edwards & Stappers et al. 2006, 2007