

# High Time Resolution with LOFAR

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(ASTRON/U. of Amsterdam)



# Acknowledgements

- Anya Bilous - lots of plots
- Charlotte Sobey - plots
- Vlad Kondratiev - background info
- Aris Noutsos - background info
- LOFAR Pulsar Working Group -  
commissioning of LOFAR's BF modes

# Scope of this lecture

- Introduce LOFAR's high-time-resolution, beam-formed modes.
- Strongly biased to pulsar data analysis.
- Richard Fallow's lecture will complement this, and focus more on analyzing dynamic spectra.
- NB: LOFAR beam-formed modes are also used for scintillation studies, RRLs, solar and planetary studies, and fast radio transients.

# Motivation for high time resolution with LOFAR



# Some example LOFAR science results using the BF modes

Just in case you like laundry lists:

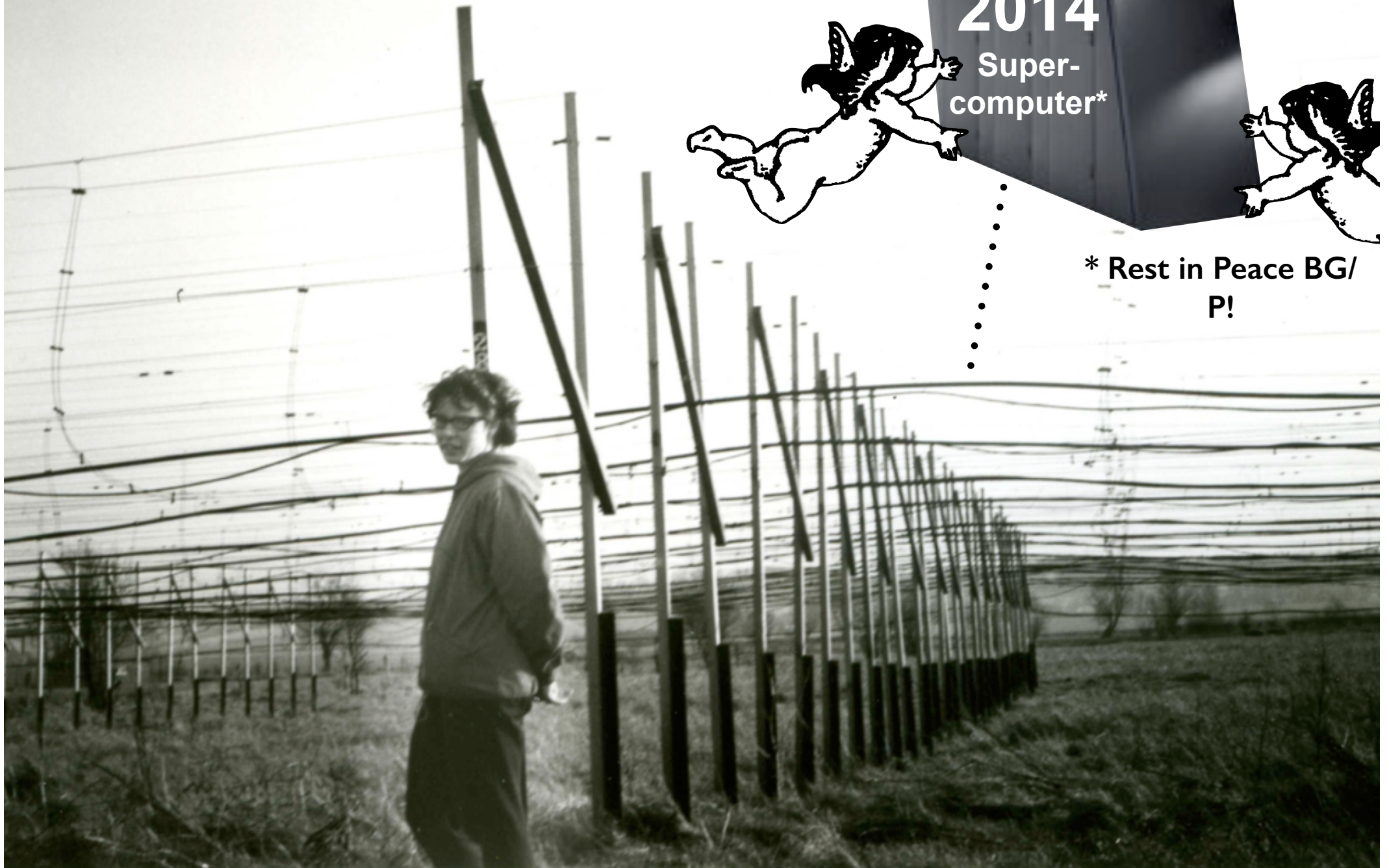
- Kondratiev et al. 2015: *Low-Frequency Profiles of Millisecond Pulsars with LOFAR*
- Sobey et al. 2015: *LOFAR discovery of a quiet emission mode in PSR B0823+26*
- Pilia et al. 2015: *Wide-Band, Low-Frequency Pulse Profiles of 100 Radio Pulsars with LOFAR*
- Bilous et al. 2014: *LOFAR observations of PSR B0943+10: profile evolution and discovery of a systematically changing profile delay in Bright mode*
- Dolch et al. 2014: *A 24 Hr Global Campaign to Assess Precision Timing of the Millisecond Pulsar J1713+0747*
- Stovall et al. 2014: *The GBNCC Pulsar Survey. I. Survey Description, Data Analysis, and Initial Results*
- Archibald et al. 2014: *Millisecond Pulsar Scintillation Studies with LOFAR: Initial Results*
- Coenen et al. 2014: *The LOFAR pilot surveys for pulsars and fast radio transients*
- Hassall et al. 2013: *Differential frequency-dependent delay from the pulsar magnetosphere*
- Hermsen et al. 2013: *Synchronous X-ray and Radio Mode Switches: A Rapid Global Transformation of the Pulsar Magnetosphere*
- Hassall et al. 2012: *Wide-band simultaneous observations of pulsars: disentangling dispersion measure and profile variations*
- Stappers et al. 2011: *Observing pulsars and fast transients with LOFAR*

# Pulsars discovered in 1967 at radio frequency of 82MHz

2014

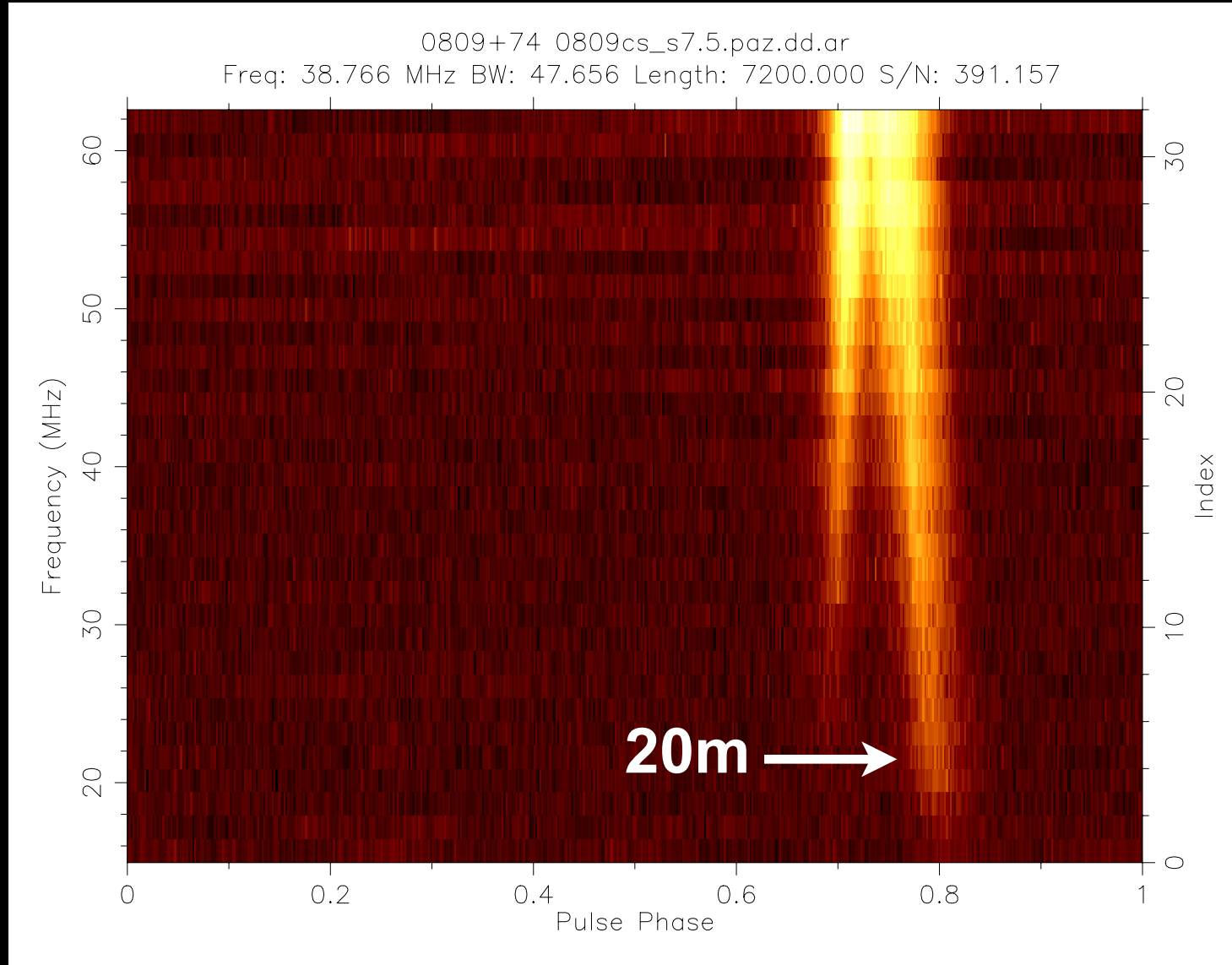
Super-  
computer\*

\* Rest in Peace BG/  
P!

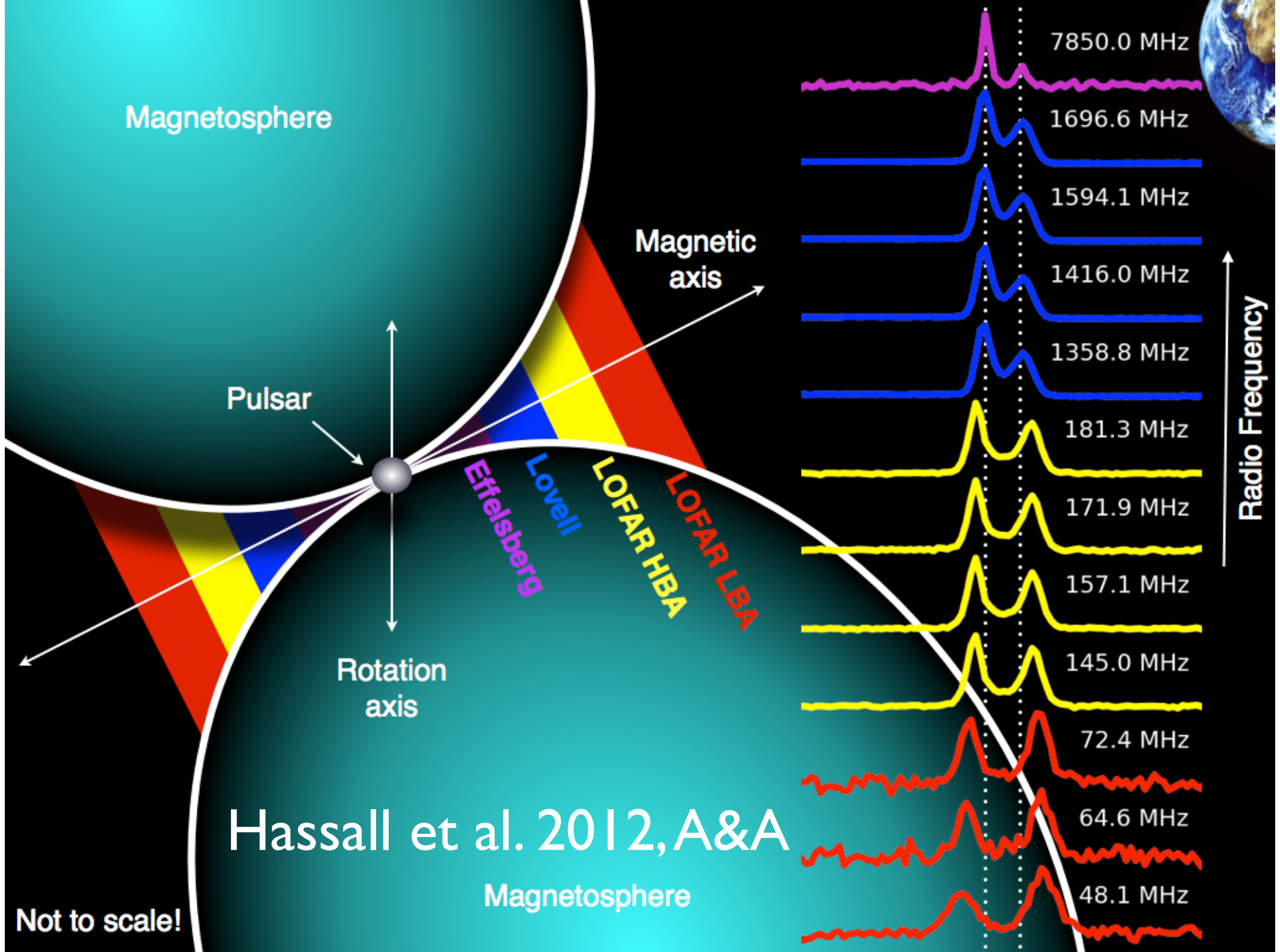


# PSR B0809+74 detected all the way down to 16MHz!

15 - 63 MHz Observing Frequency

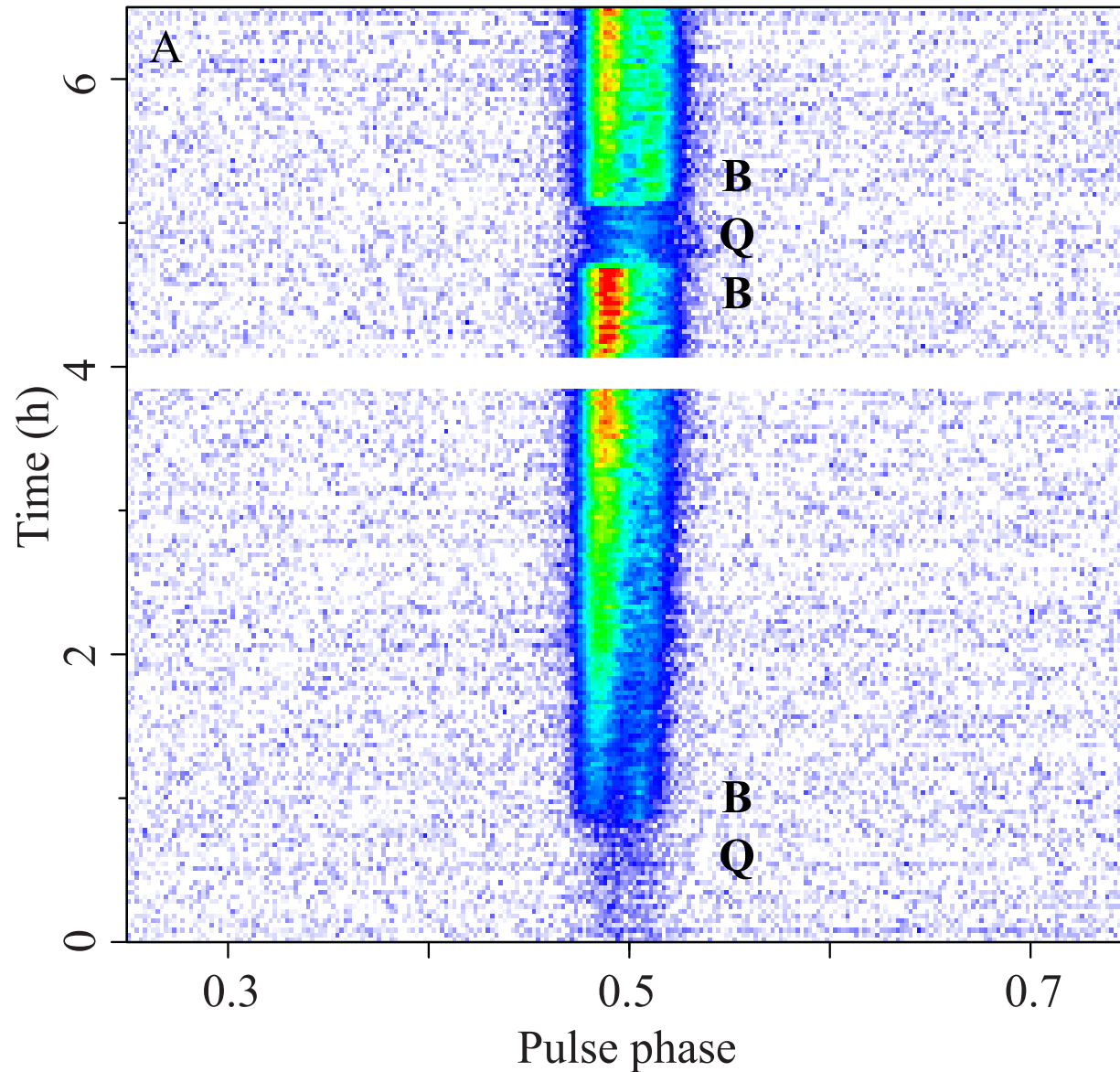


Kondratiev & Hessels



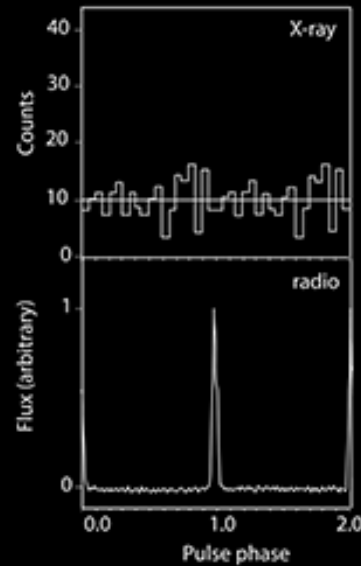
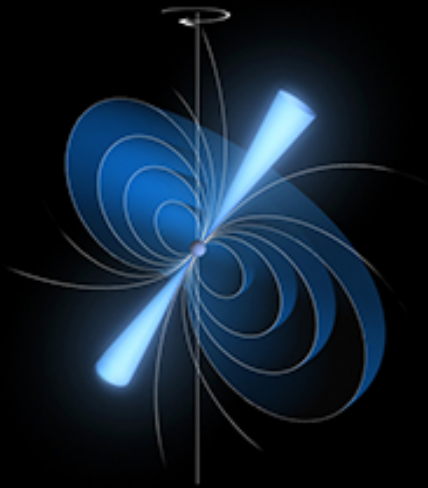


# PSR B0943+10 Switching Modes



Hermesen et al. 2013, *Science*

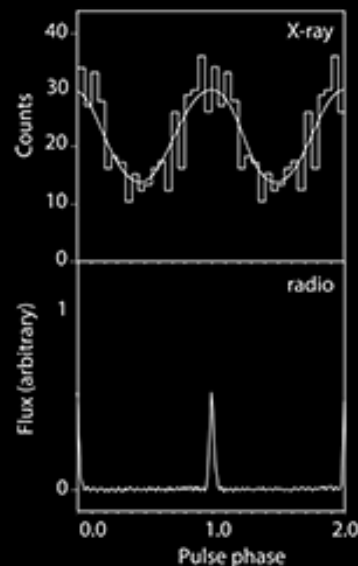
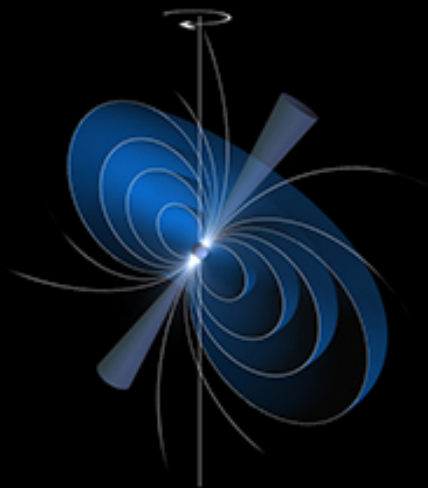
# Magnetospheric mode switching



X-ray dim

**'Bright' Mode**

Radio bright



X-ray bright

**'Quiet' Mode**

Radio dim

Hermesen et al. 2013, *Science*

**Observing with LOFAR at high  
time resolution**

# Terminology

So many types of beams...

van Leeuwen - From Stappers et al. 2011



*Element Beam*

or

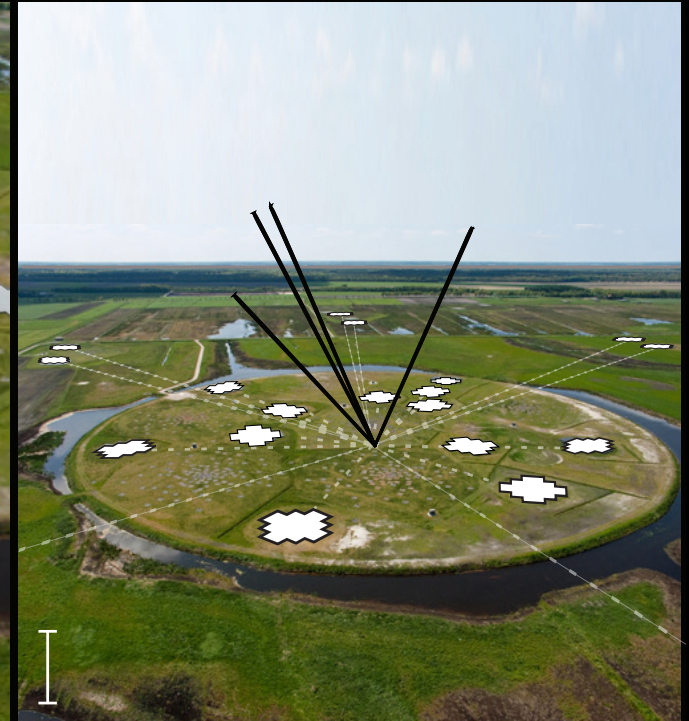
*Tile Beam*



*Station Beam*

or

*Sub-Array Pointing  
(SAP)*



*Array Beam*

or

*Tied-array Beam*



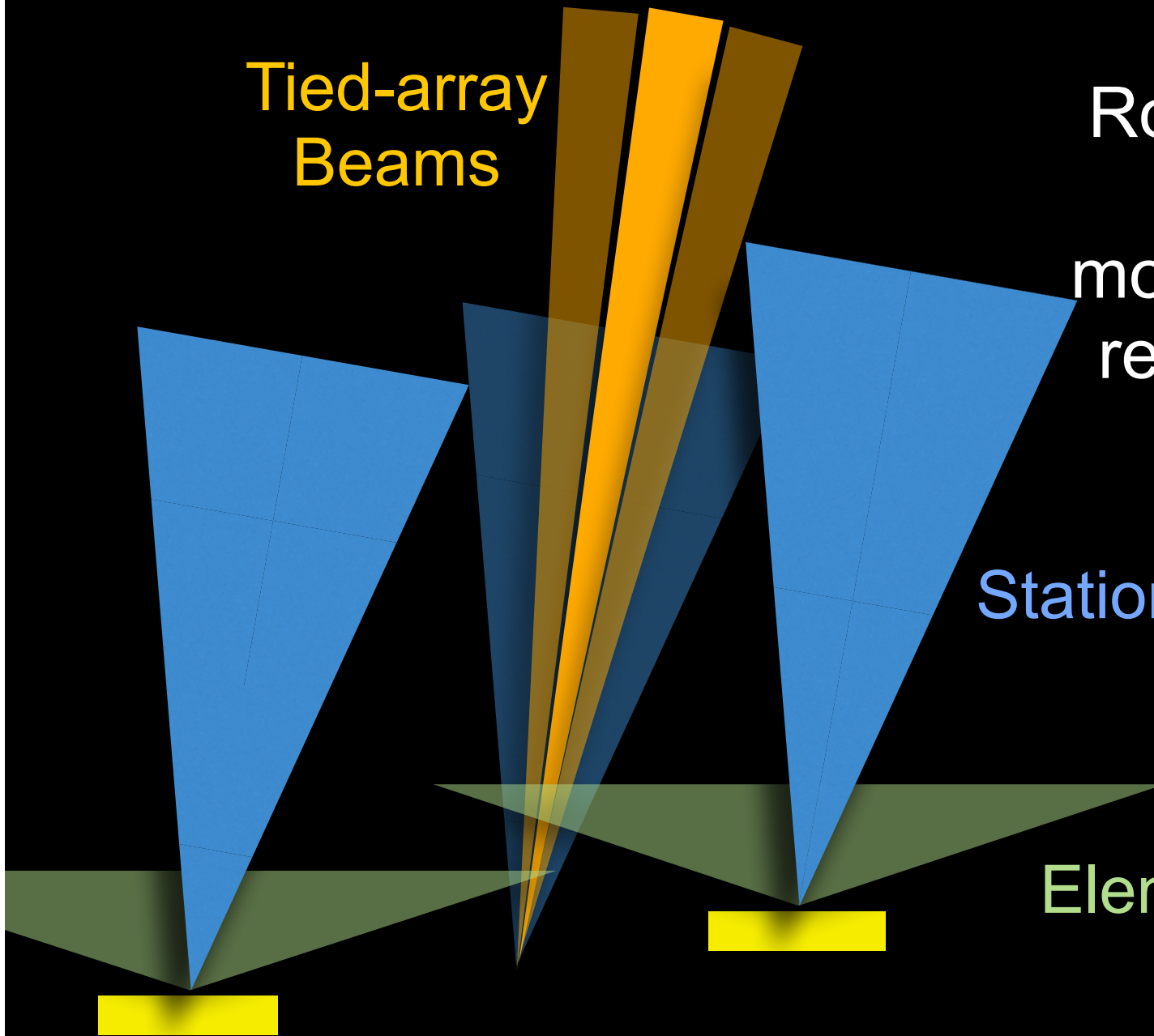
# Array Beam Forming

Tied-array  
Beams

Roughly speaking,  
beam-formed  
modes trade spatial  
resolution for time  
resolution.

Station Beam

Element Beam



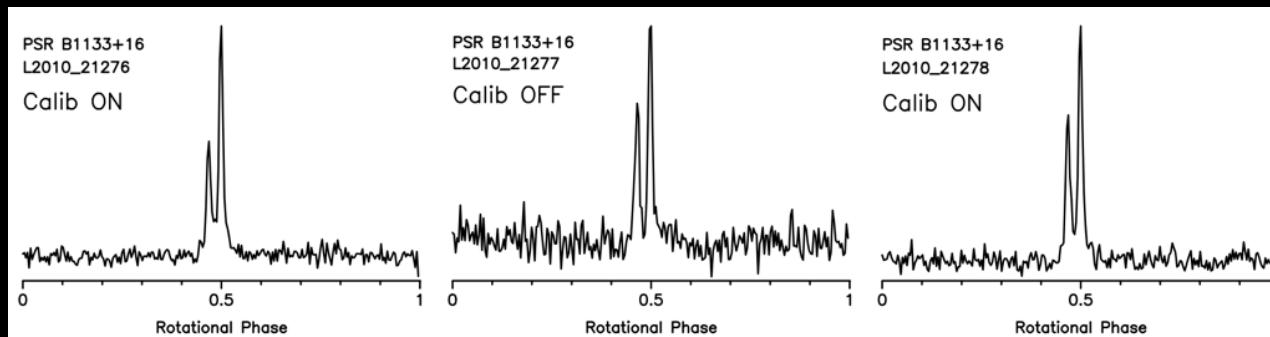
# Station beam calibration

## Sequence of 3 BF observations

Calibration ON

Calibration OFF

Calibration ON



- Station calibration is critical for getting the maximum station sensitivity and the right beam shape.





# LOFAR HBAs

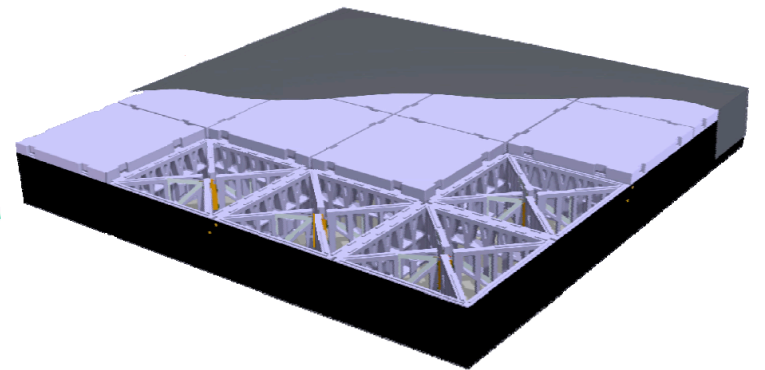
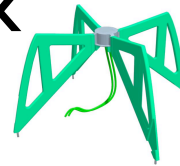


Hassall

HBAs

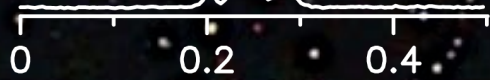
100-250MHz

(2x)24x



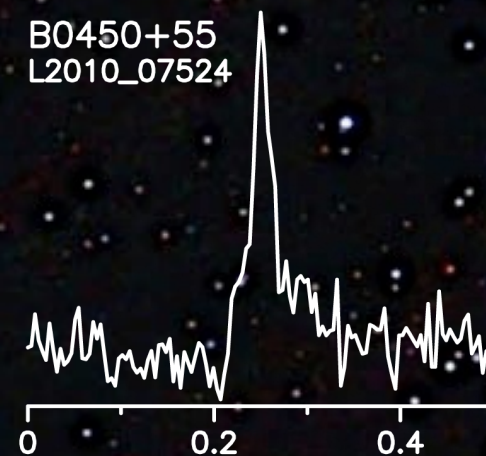


B0329+54  
L2010\_07524



0.5 degree

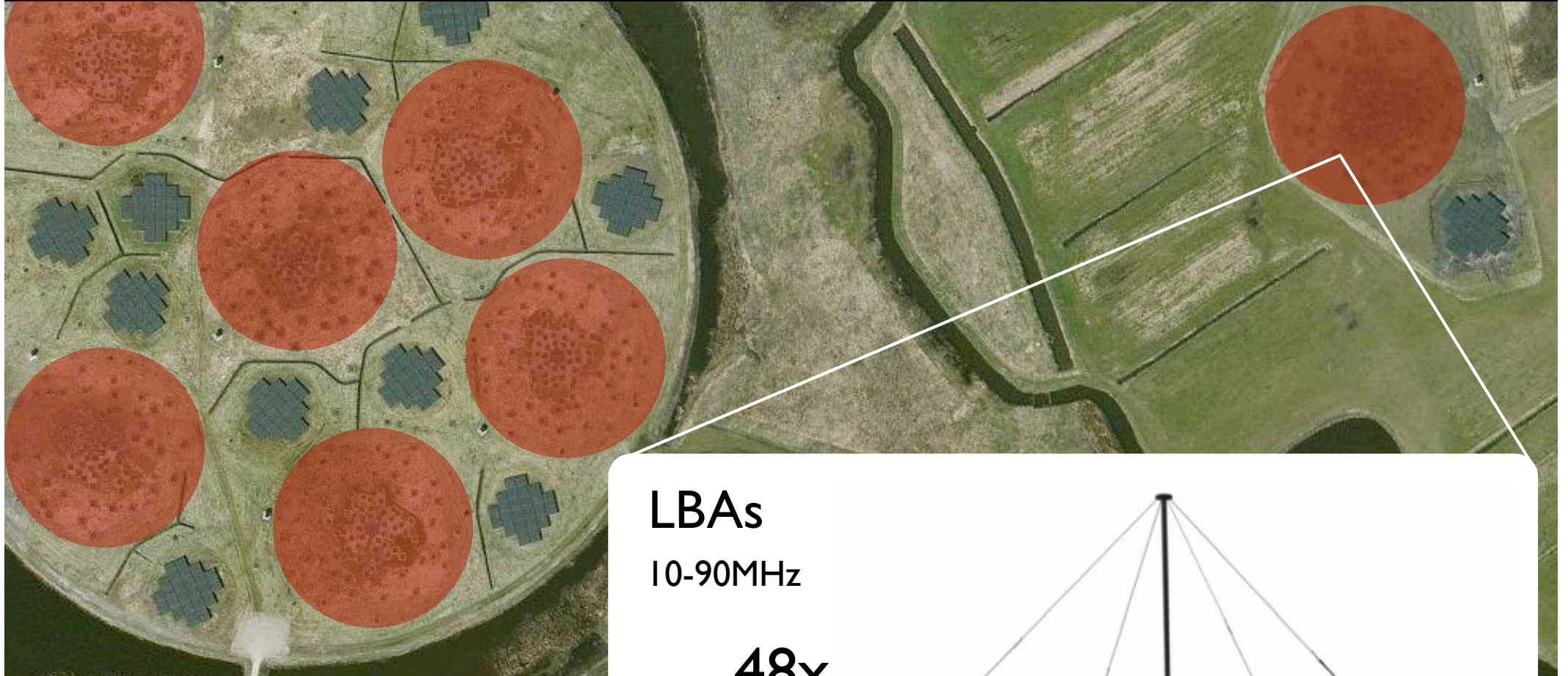
B0450+55  
L2010\_07524



# Multiple HBA Station Beams



# LOFAR LBAs

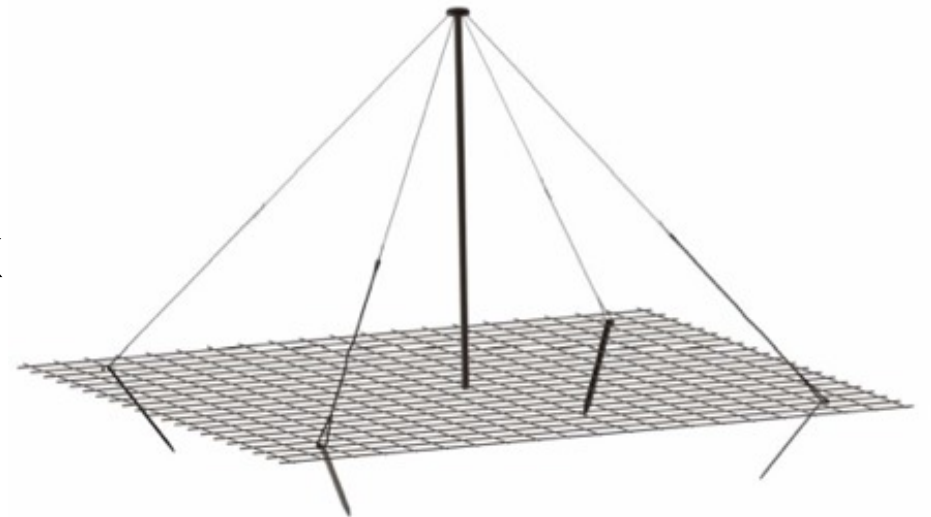


Hassall

LBAs

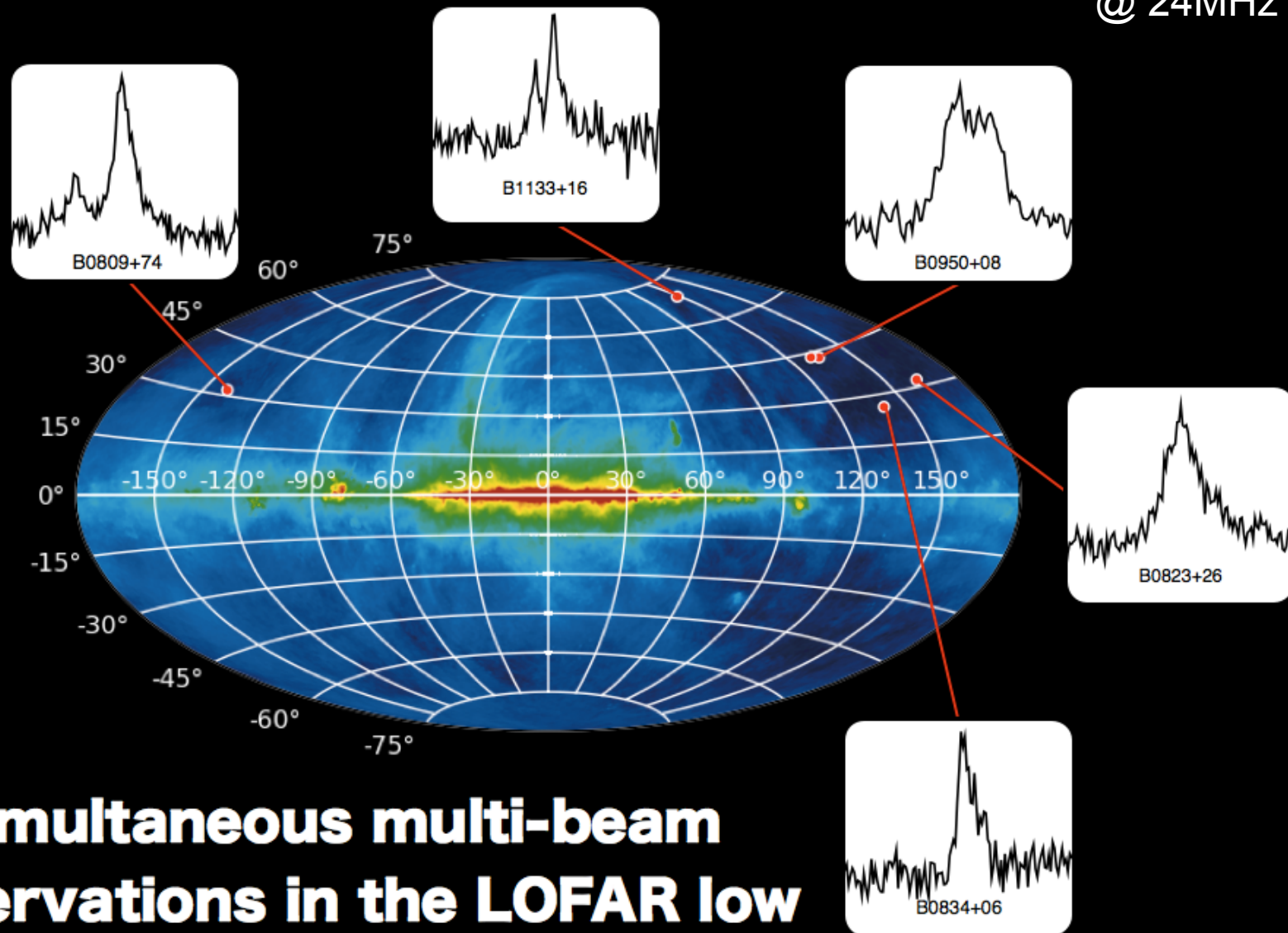
10-90MHz

48x



# LOFAR LBA Multi-beaming

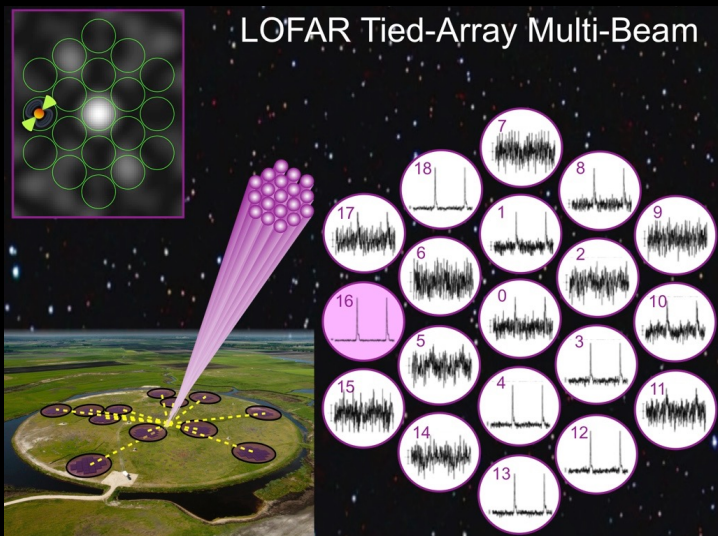
@ 24MHz



**simultaneous multi-beam  
observations in the LOFAR low  
band**

# Standard beam-formed modes

- *Incoherent Stokes (IS)*
- *Coherent Stokes (CS)*
- *Fly's Eye (FE)*
- *Complex Voltage (CV; subset of CS)*
- *Beam-formed+Imaging (BF+IM)*





# Incoherent Stokes (IS) mode

- The individual station beams (SAPs) are 'detected' and subsequently summed on COBALT.
- The phase information of the signals is lost.
- The full FoV of the stations is maintained, regardless of the baseline between them.
- RFI from different stations can pile up.
- Sensitivity increases only as the  $\sqrt{\text{\#stations}}$ .

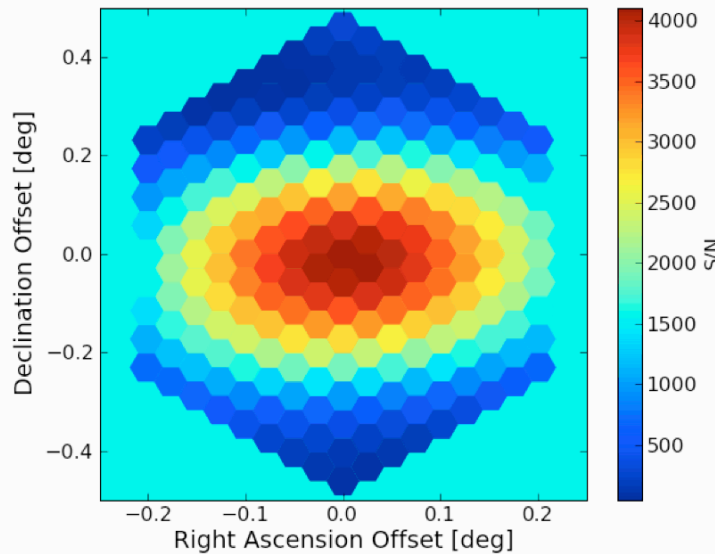


# Coherent Stokes (CS) mode

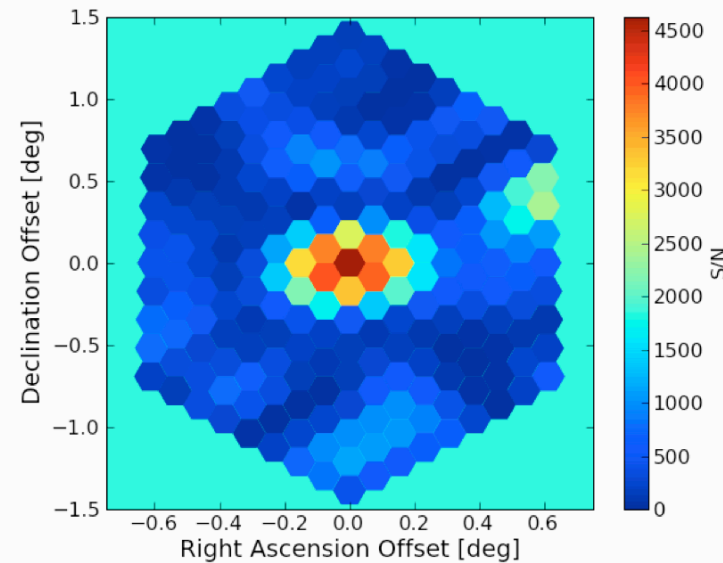
- The individual station beams (SAPs) are added on COBALT *before* `detection`.
- A time delay/phase calibration table is applied.
- The FoV depends on the maximum baseline and *uv*-distribution.
- Many CS beams can be synthesized within a single SAP.
- Fairly robust to RFI.
- Sensitivity increases *roughly* with the number of stations included.

# Tied-array coherency and beam shape

Observed, zoomed in



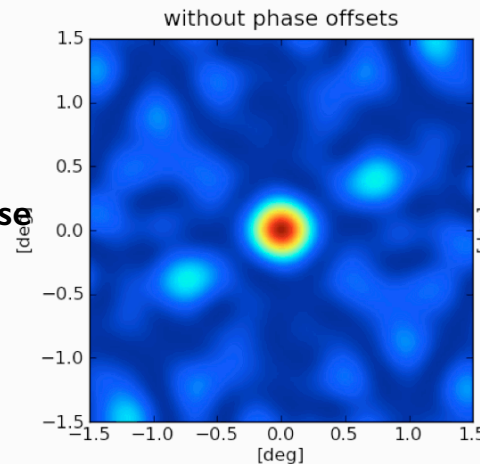
Observed, zoomed out



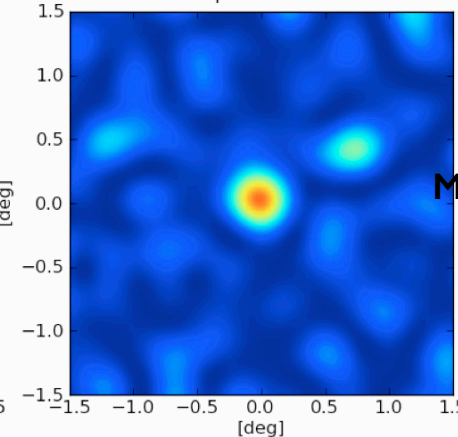
PSR B0329+54

HA = -2hr

Modeled, no phase offsets



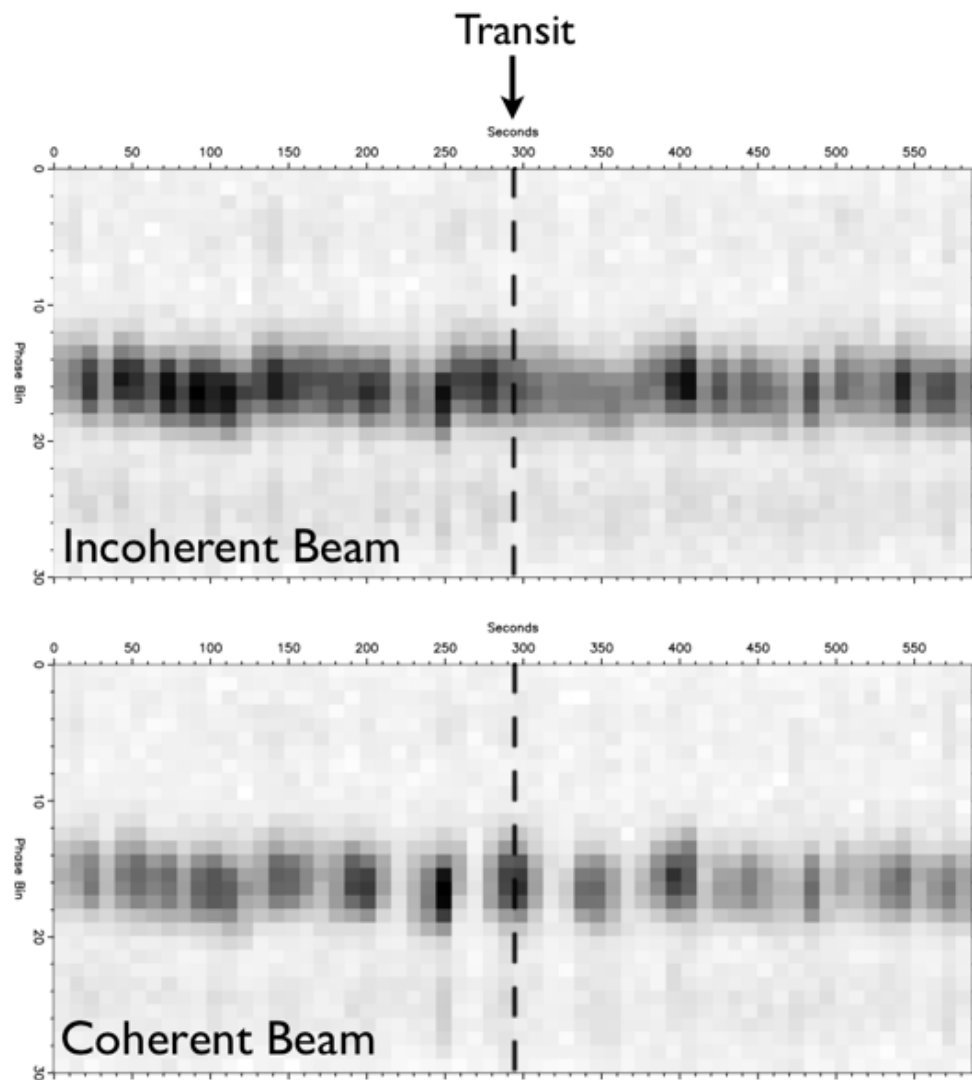
with phase offsets



Modeled, with phase offsets

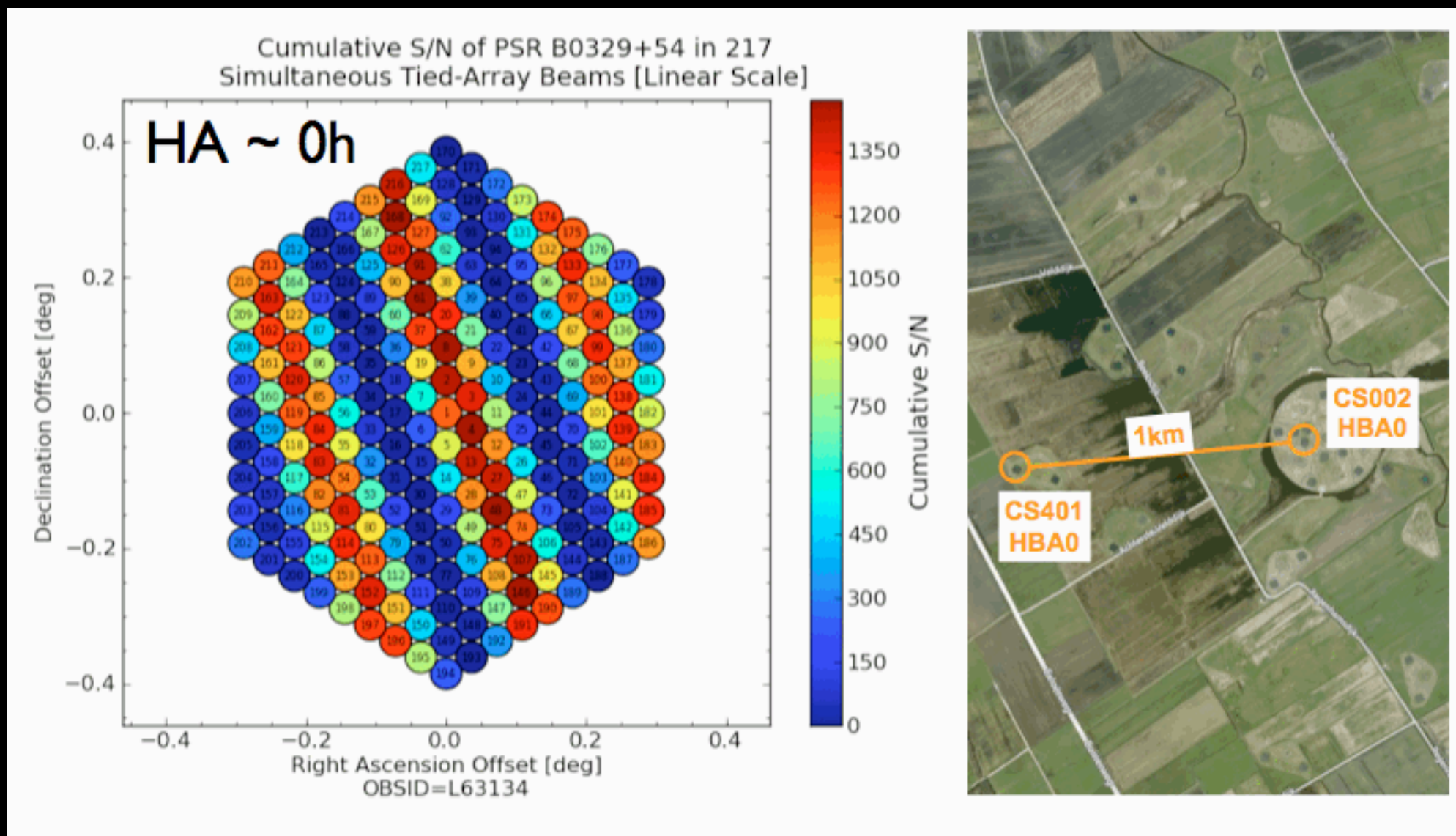
# CS vs. IS mode

## Transit experiment PSR B0329+54



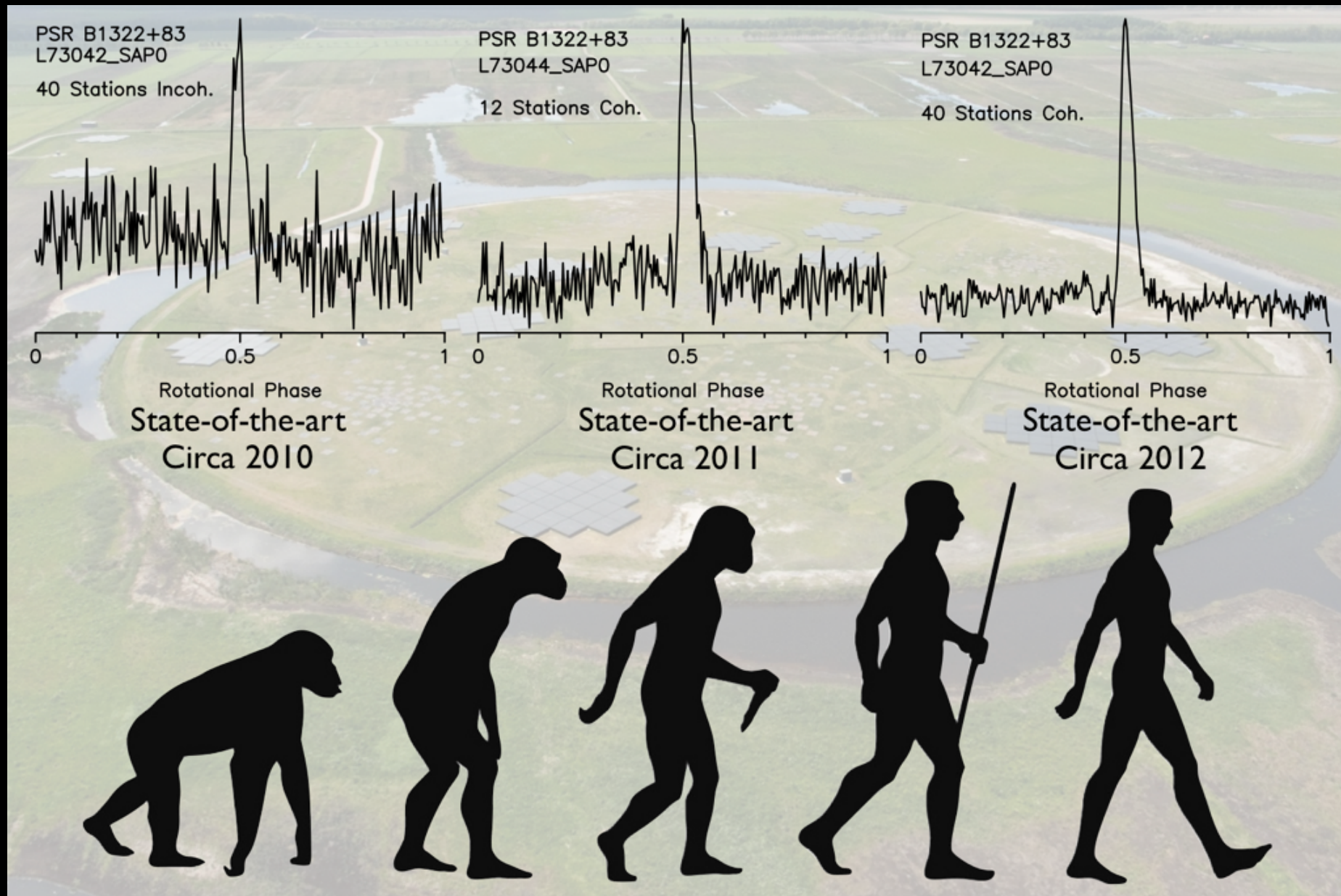
# CS vs. IS mode

Tracking PSR B0329+54 with 2 stations and 217 CS beams





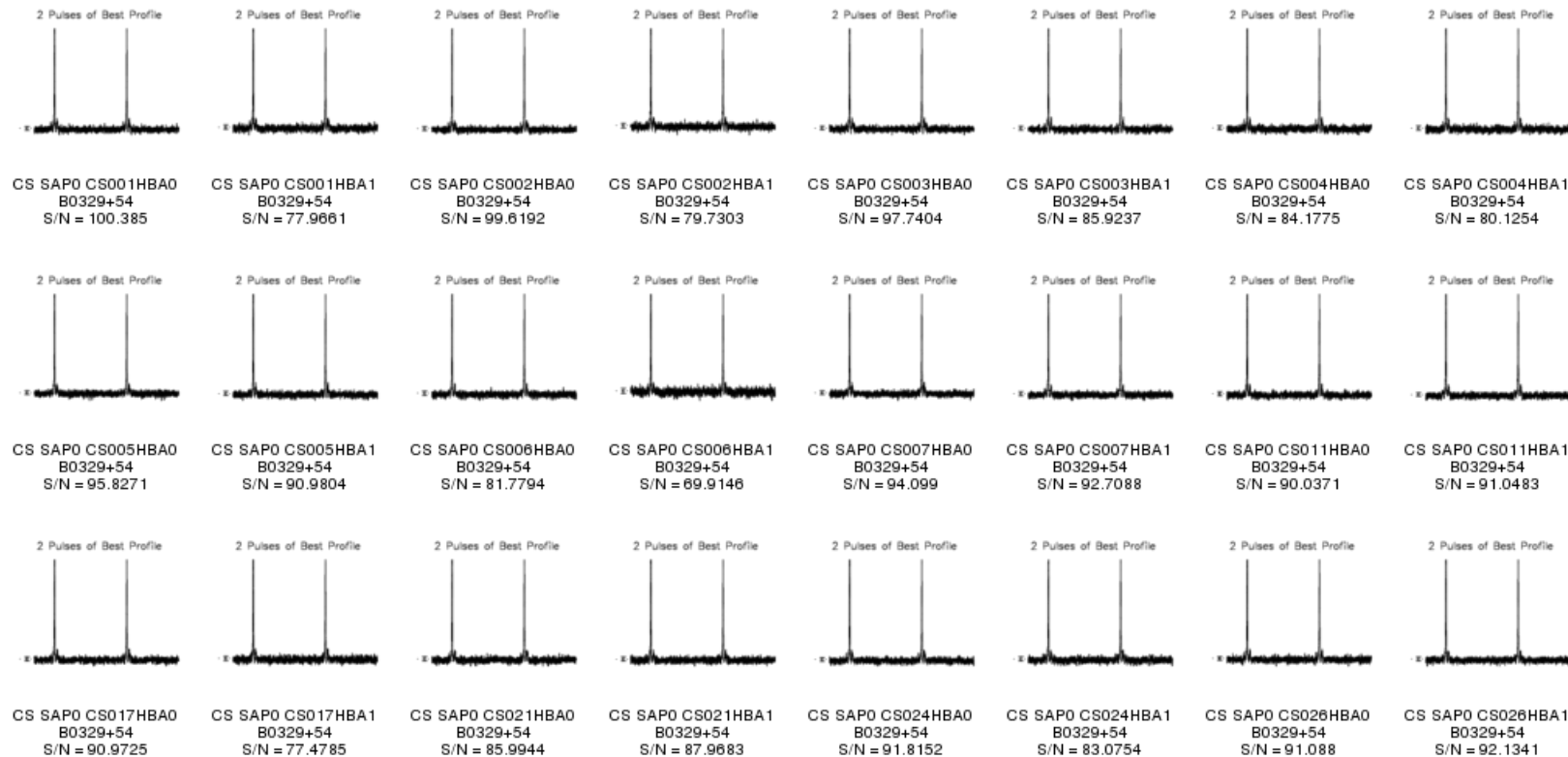
# An evolving telescope





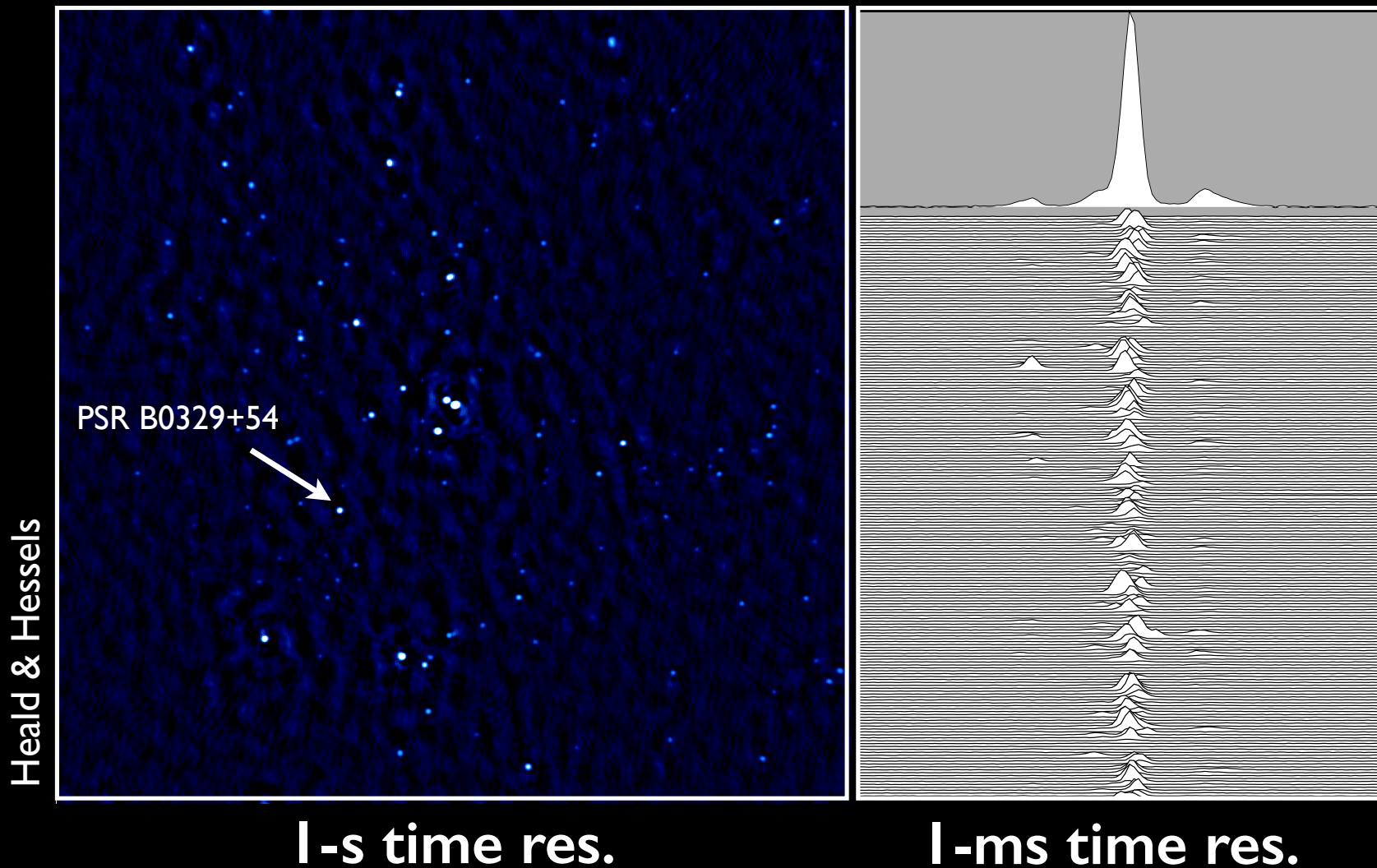
# Fly's Eye (FE) mode

- Each station beam (SAP) is processed separately on COBALT.
- Mainly used for testing.
- Could be used for science in the future.

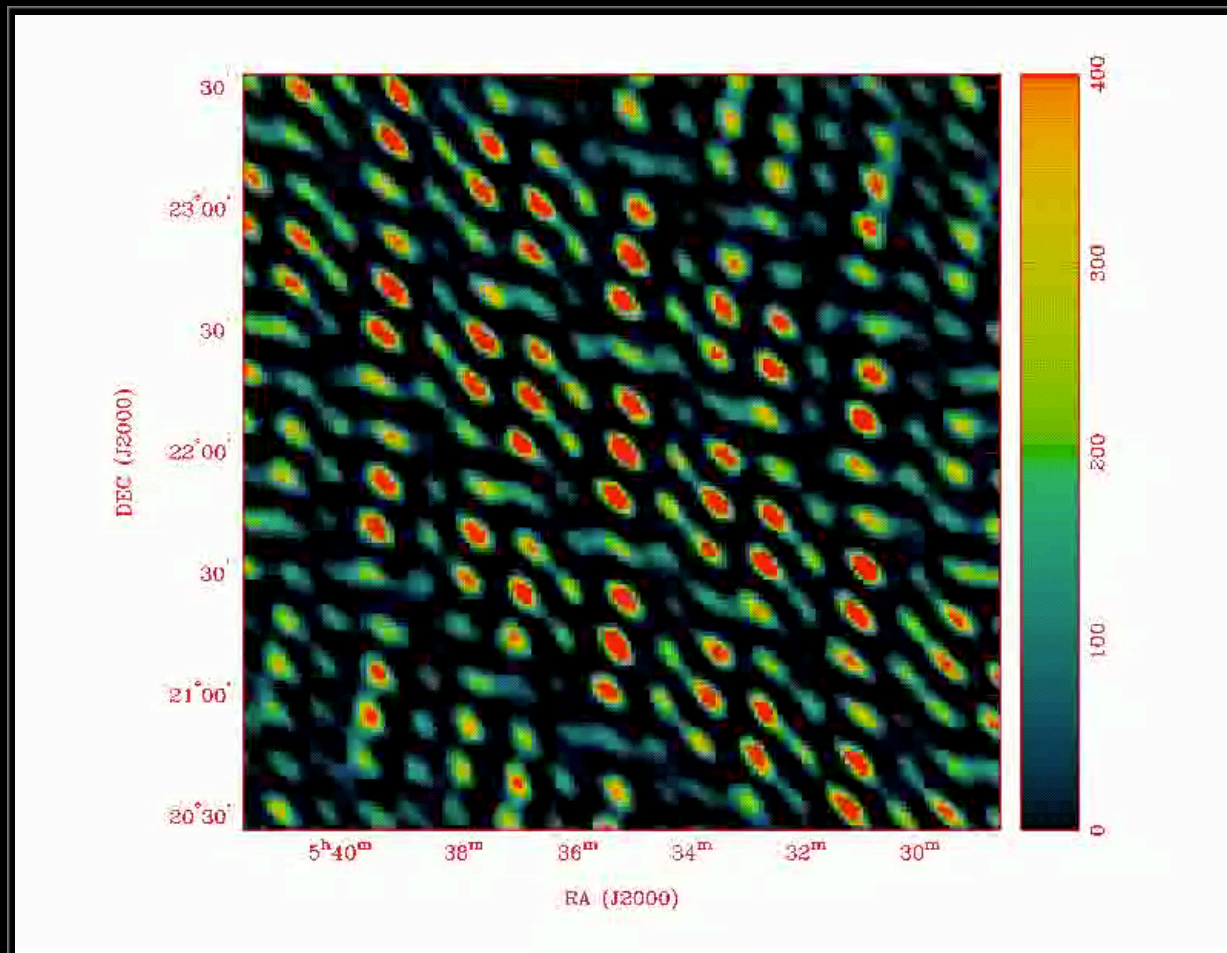


# Simultaneous beam-formed and imaging (BF/IM) mode

NB: both data types currently have to use the same station set



# Fast Imaging Exists...



- Movie showing imaging of a Crab giant pulse at 1/40th of the actual speed.
- Dedispersion required.

Law - *Not* LOFAR data

# Customizing BF modes

# Choice of time/frequency resolution

- Just like IM mode, can chose 16, 32, 64, 128, 256, etc. channels per subband.
- Possible to *skip* the 2PPF.
- Can also sum channels post 2PPF.
- Typically, one uses 16 or 64 channels (12 or 3 kHz) frequency resolution in the HBA and LBA bands, respectively.
- Time resolution is:  $5.12\mu\text{s} \times N_{\text{chan}} \times N_{\text{down}}$
- Time resolution is  $5.12\mu\text{s}$  or  $\geq 81.92\mu\text{s}$



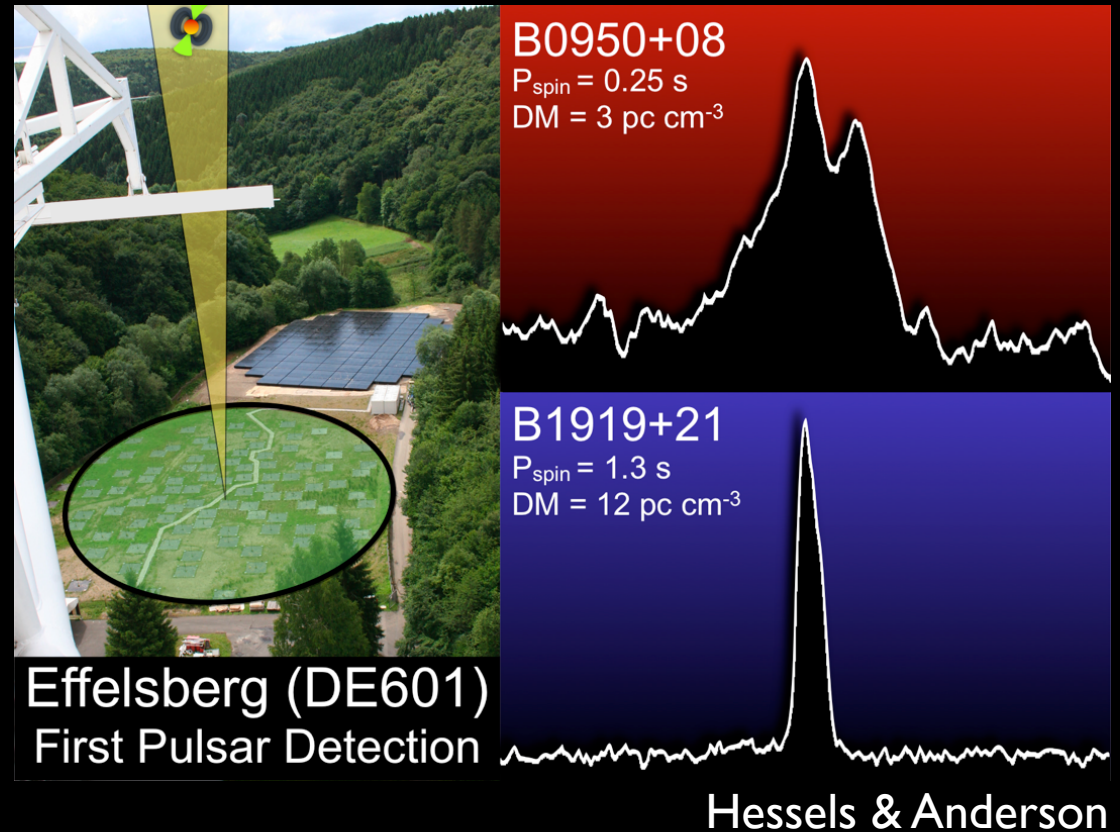
# Choice of Stokes (or not!) parameters

- Can record just *Stokes I* - e.g. for pulsar or transient search experiments.
- For polarimetry, can record *Stokes I, Q, U, V*.
- For more advanced offline signal processing, can record *XX, XY, YX, YY*. This option is also referred to as *Complex Voltage (CV)* mode.

**Other observing modes**

# Standalone mode

- Each International LOFAR HBA/LBA station has 1/3 the sensitivity of the Superterp!
- Standalone backends at these stations can record beam-formed data separate from COBALT.
- Ideal for high-cadence monitoring experiments of very bright sources.



# Raw UDP dumps

- It is also possible to record the *raw* station data, as it arrives at COBALT.
- Recording such data then allows one to repeatedly run the data through COBALT and create different types of observations.
- Data rate is 3Gb/s (full band), so only ~12 stations can be recorded at full bandwidth.
- This mode is only used for testing, currently.



**Observing challenges**

# Propagation effects

- Dispersion.
- Scattering.
- Scintillation.
- Faraday rotation.
- Ionospheric phase delays.

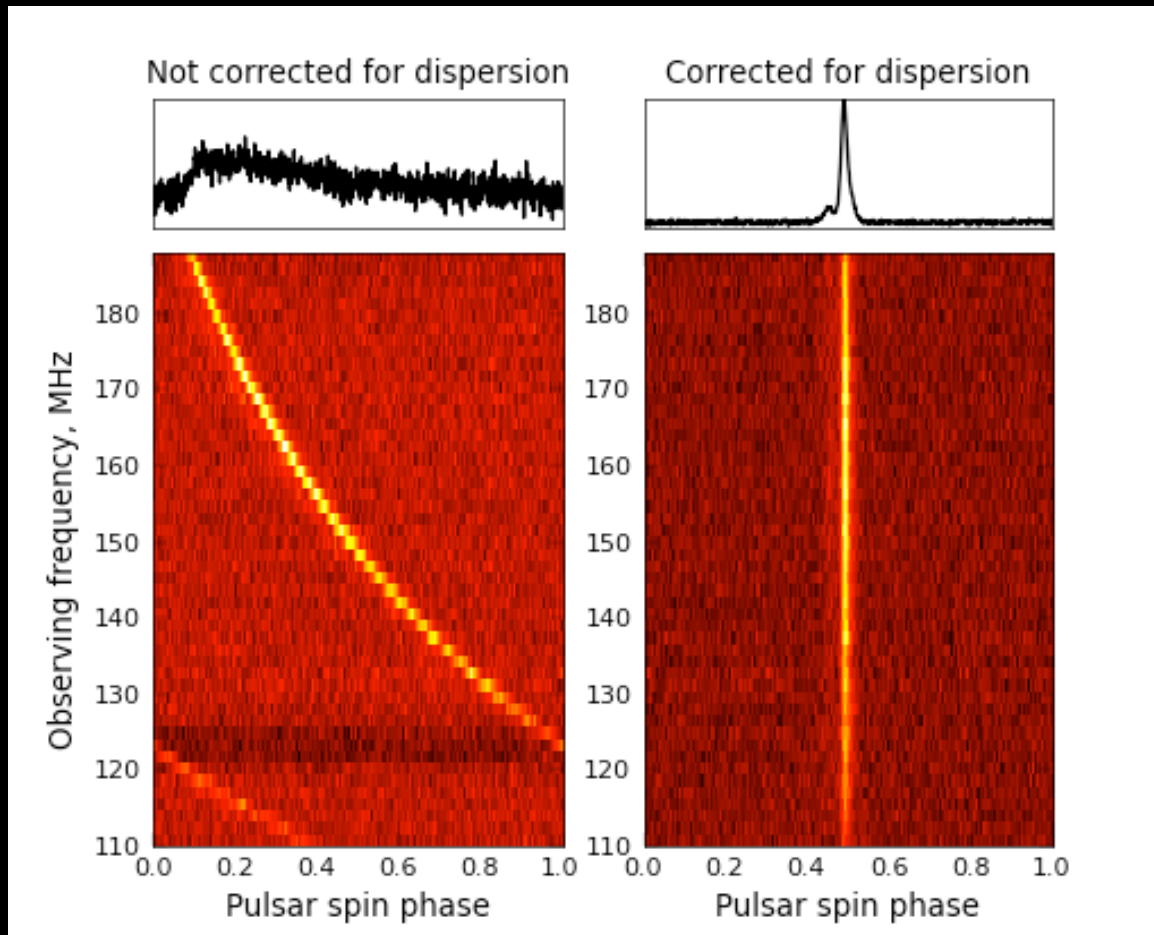
$$I(t) = g_r g_d S(t) * h_{DM}(t) * h_d(t) * h_{RX}(t) + N(t)$$

- These effects are strongly chromatic, increasing drastically in magnitude towards low radio frequencies.
- High-time-resolution (millisecond timescale) signals are often not detectable without correcting for these effects!

# Propagation effects

## Dispersion

PSR B2021+51



Bilous

- DM [ $\text{pc cm}^{-3}$ ] measures the integrated column density of free electrons along the LoS.
- Can correct using (in)coherent dedispersion.

$$\Delta t_{\text{DM}} \propto \nu^{-2}$$

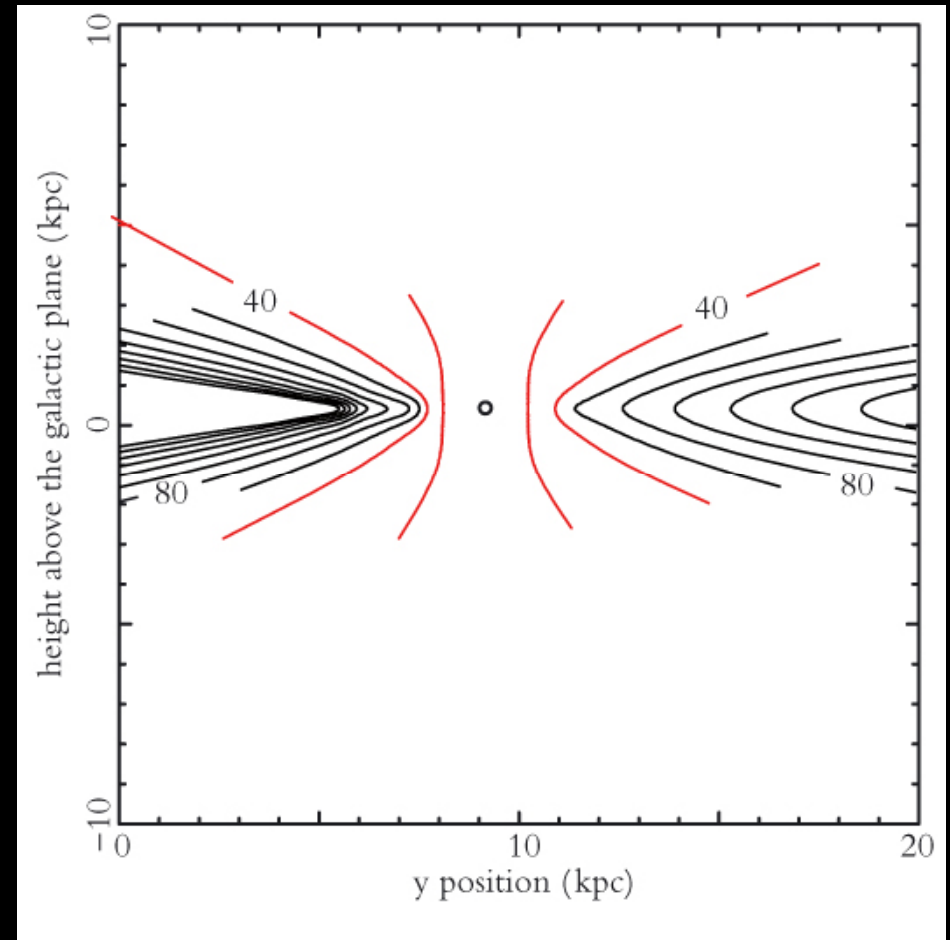
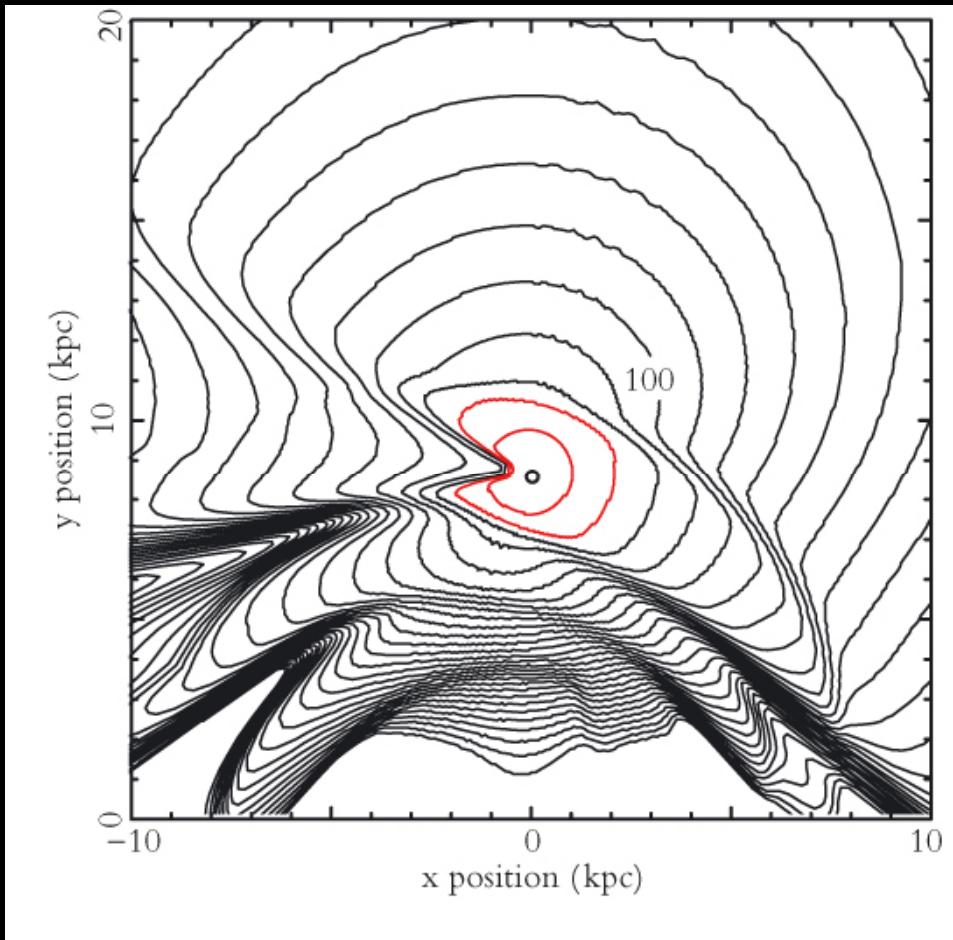
DM off by only  $3 \text{ pc cm}^{-3}$ !



# Galactic dispersion measures

Loose correlation with amount of scattering.

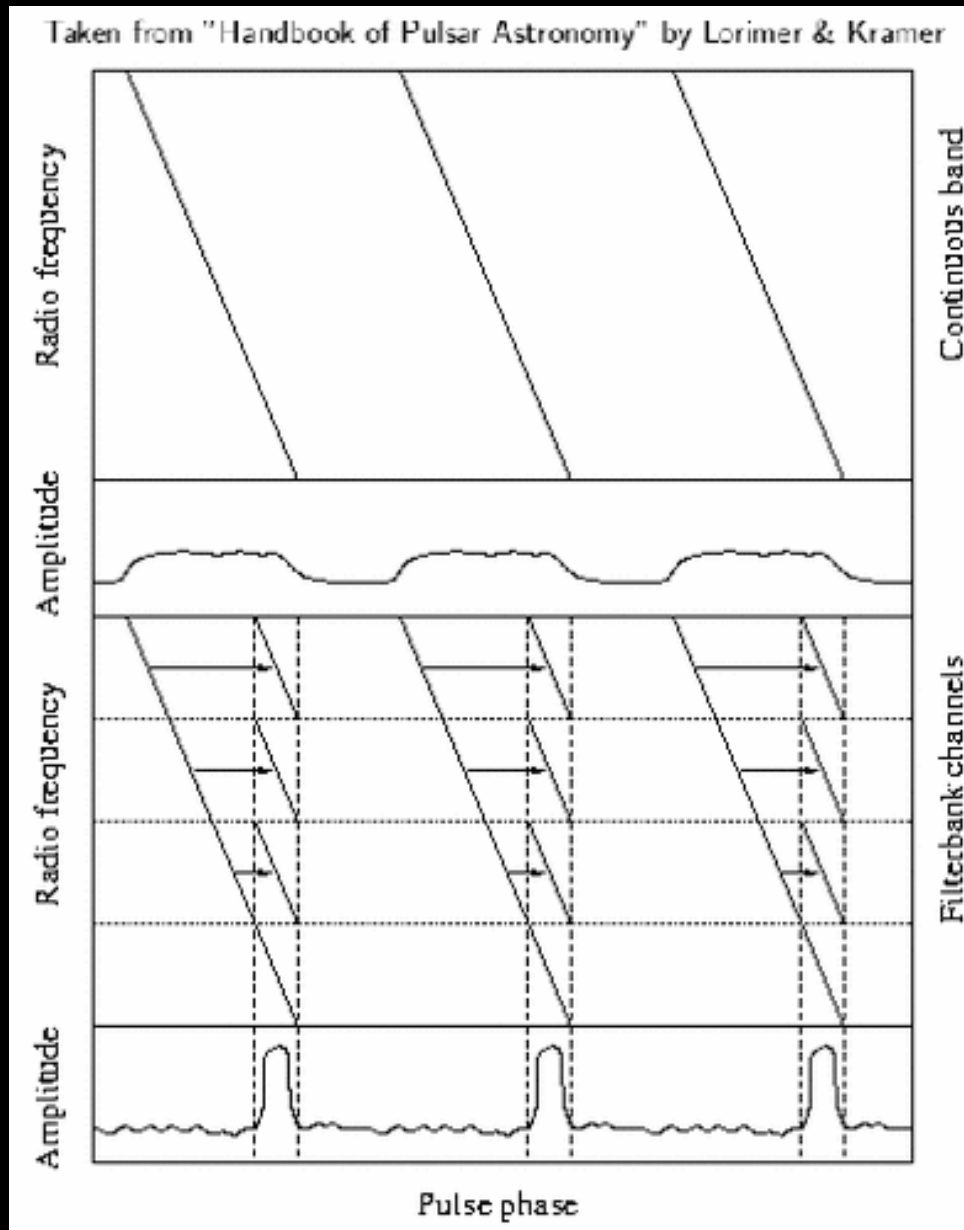
Creates a 'horizon' for Galactic LOFAR observations.



van Leeuwen

NE2001 model of Cordes & Lazio (2001)

# Dedispersion

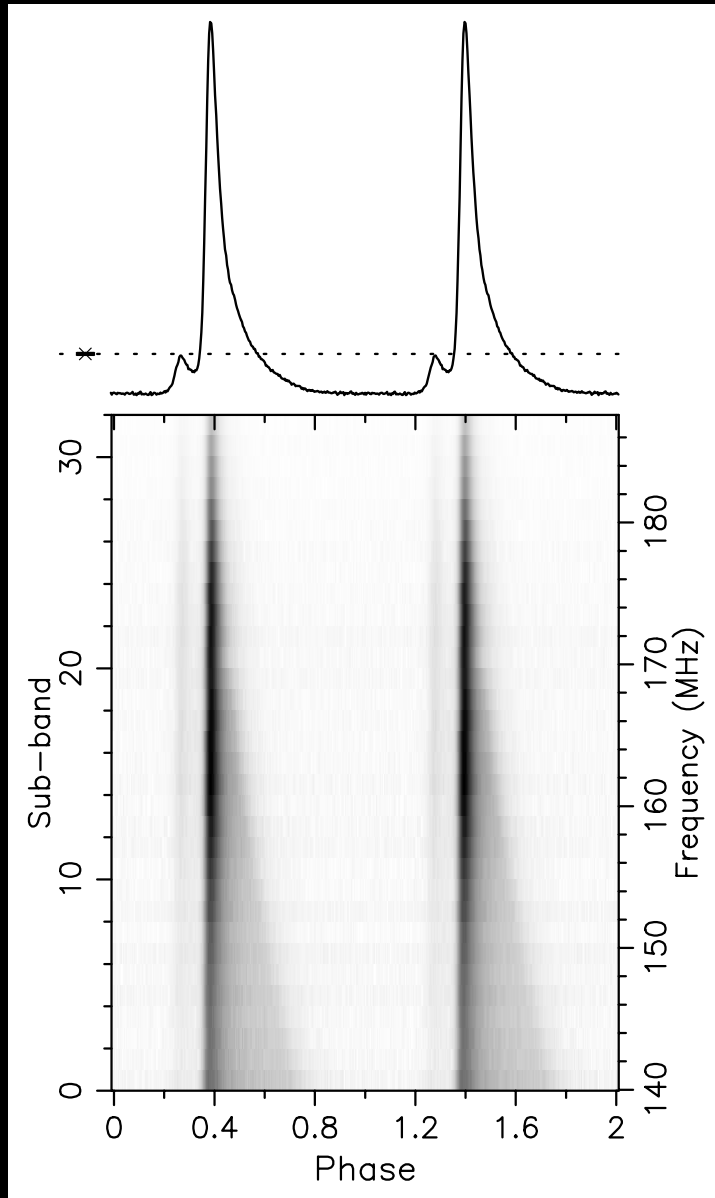


- Incoherent dedispersion works by shifting channels in time.
- Coherent dedispersion is more computationally expensive and requires the raw voltages.

# Propagation effects

## Scattering

PSR B2111+46



Hessels

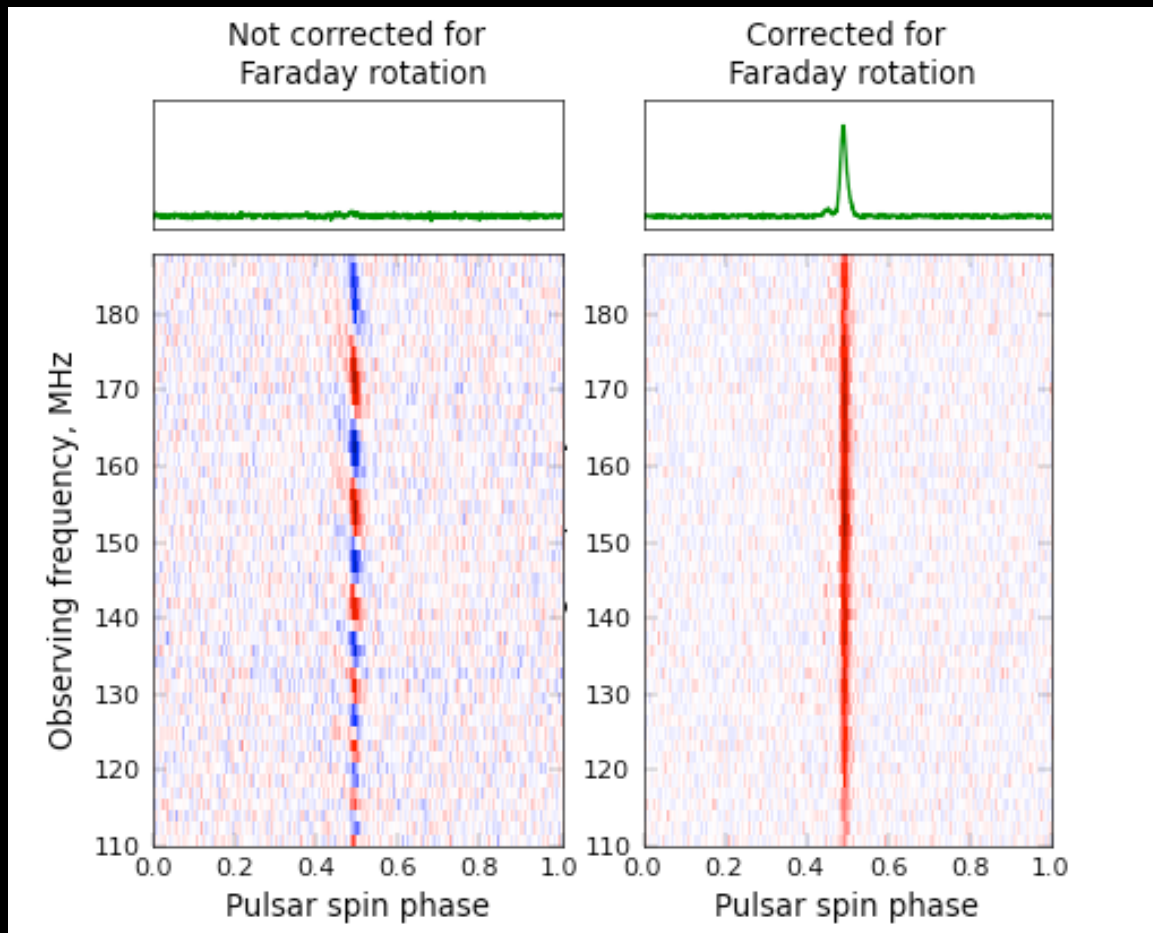
- Scattering reflects the inhomogeneity in the medium.
- No easy way to correct for this.
- Creates a sort of Galactic horizon for short-duration radio signals.

$$\Delta t_{\text{Scatt}} \propto \nu^{-4}$$

# Propagation effects

## Faraday rotation

PSR B2021+51



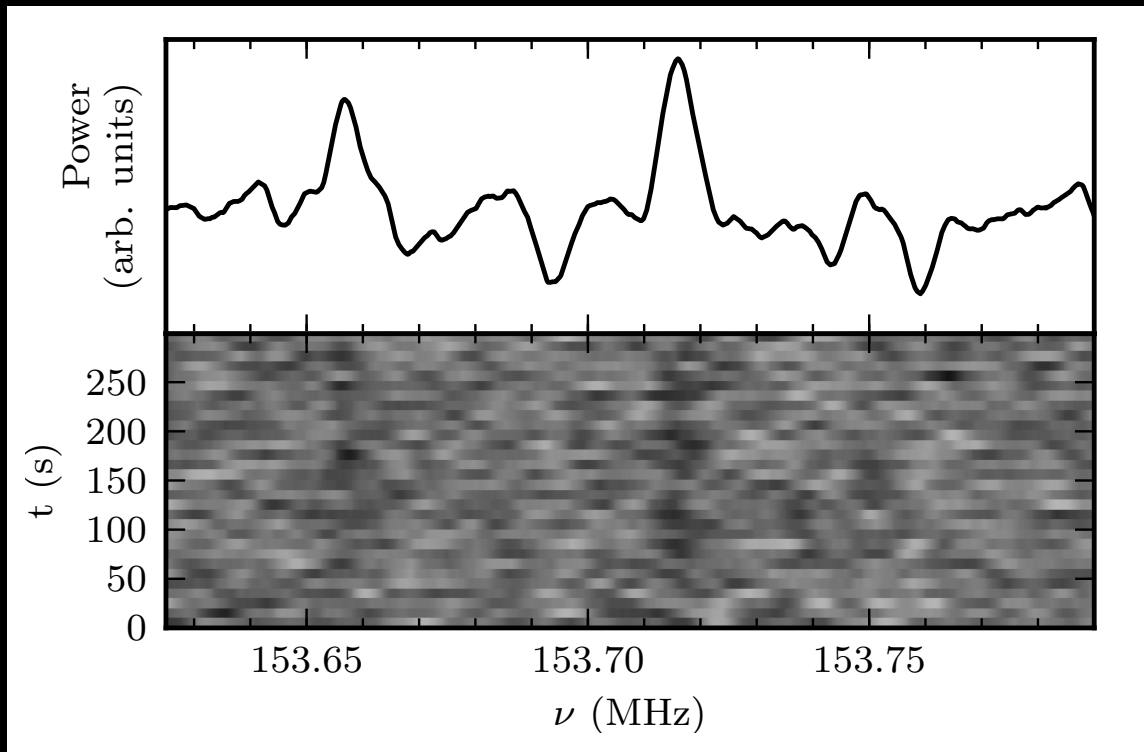
- RM [ $\text{rad m}^{-2}$ ] measures the electron-density-weighted magnetic field along the LoS.
- Ionospheric depolarization.

Bilous



# Propagation effects

## Scintillation



Archibald

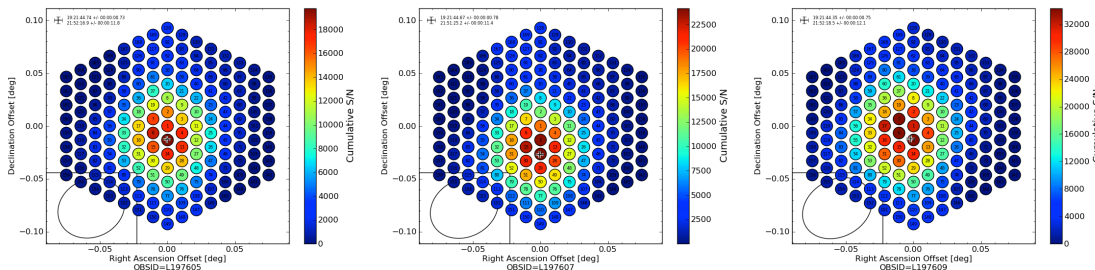
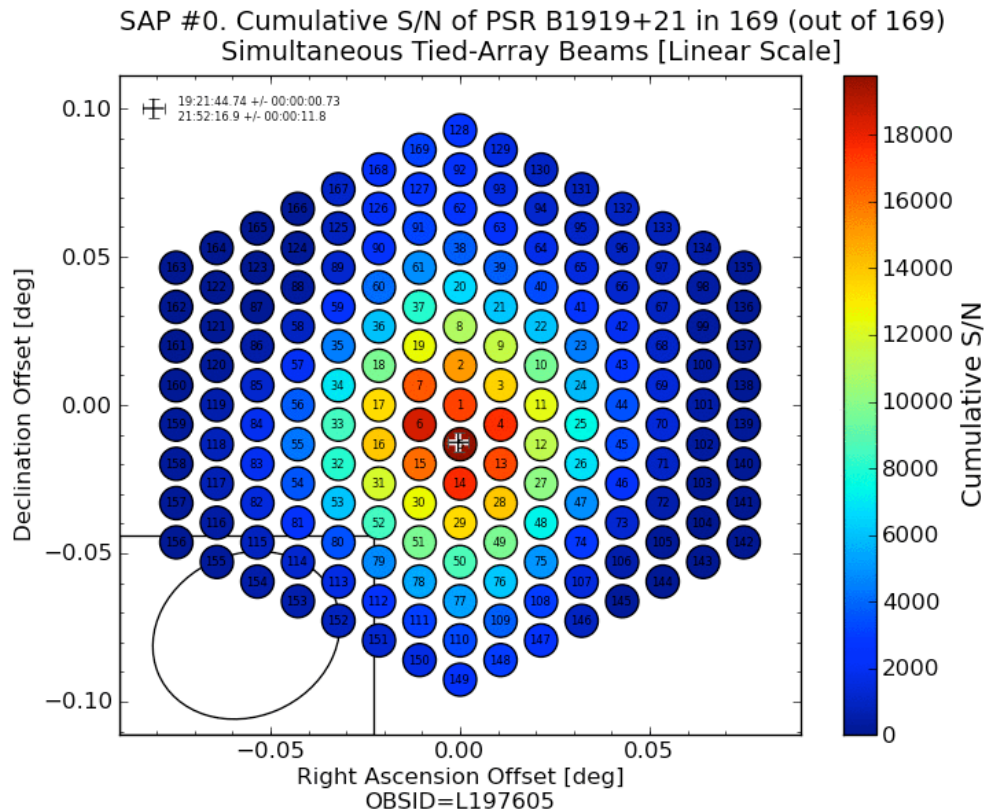
These scintles are only  
~1 kHz wide!

- Scintillation is due to (de/con)-structive interference of the signal due to the intervening material (refractive and diffractive).
- At LOFAR frequencies, we typically average over many scintles.

# Propagation effects

## Ionospheric beam wobble

- Differential ionospheric phase delays between stations can cause the tied-array beam position to wobble on the sky.
- Likely a much bigger problem for the Full Core than the Superterp.
- Some periods will be worse than others.



# Planning an observation

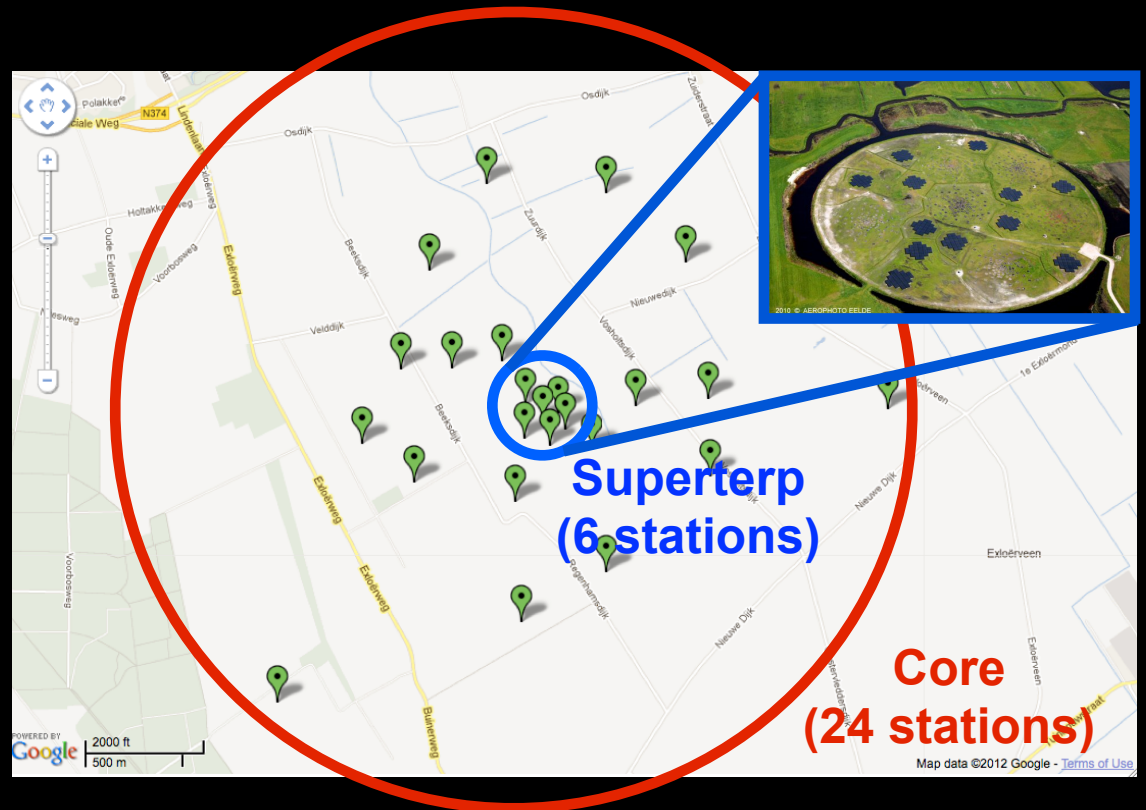
# Data volume

- BF mode data volumes can be very large (after all, we're recording thousands of samples per second, many beams, and many frequency channels).
- A single-beam, *Complex Voltage* observation takes 4.1 TB/hr.
- Maximum system throughput is  $\sim 40$  Gb/s and is used in the 222-beam pulsar survey observations.
- You may need to spread your beams and bandwidth over many CEP2 nodes.



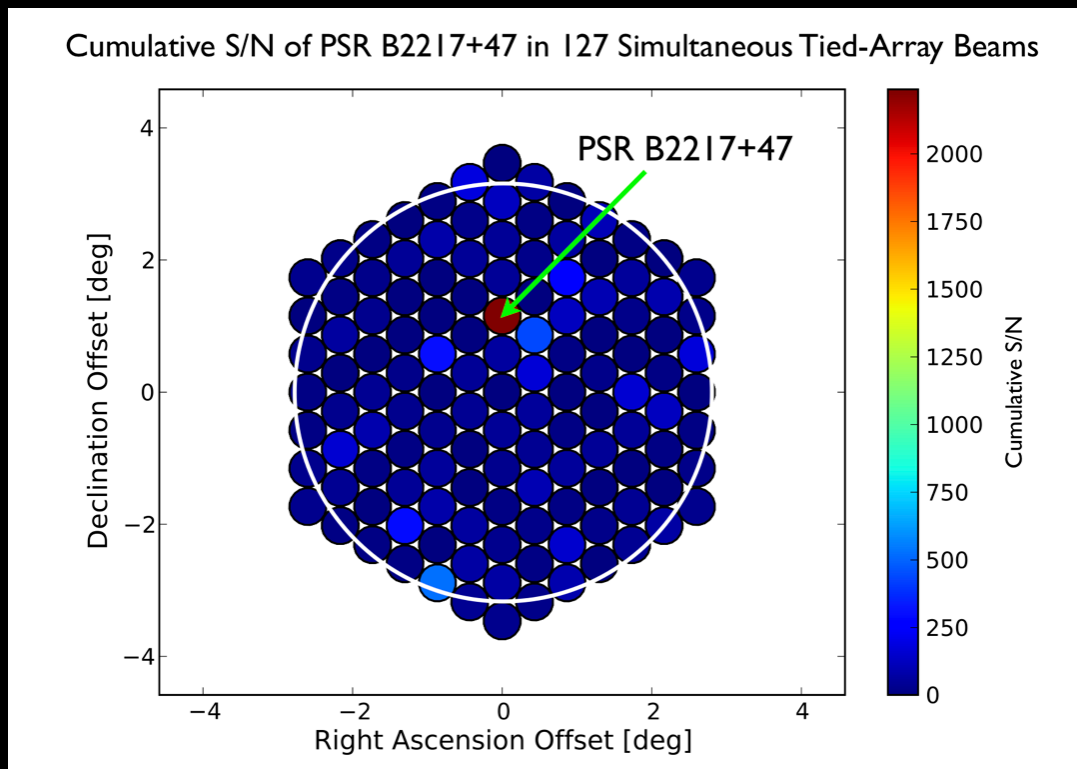
# Choosing the right stations

- Only the Core stations are on the LOFAR *Single Clock*.
- Max sensitivity: Full Core (24 stations, 5 arcmin beam).
- Max survey FoM: Superterp (6 stations, 30 arcmin beam).
- Need to be really careful not to include malfunctioning stations (use FE results as your guide).

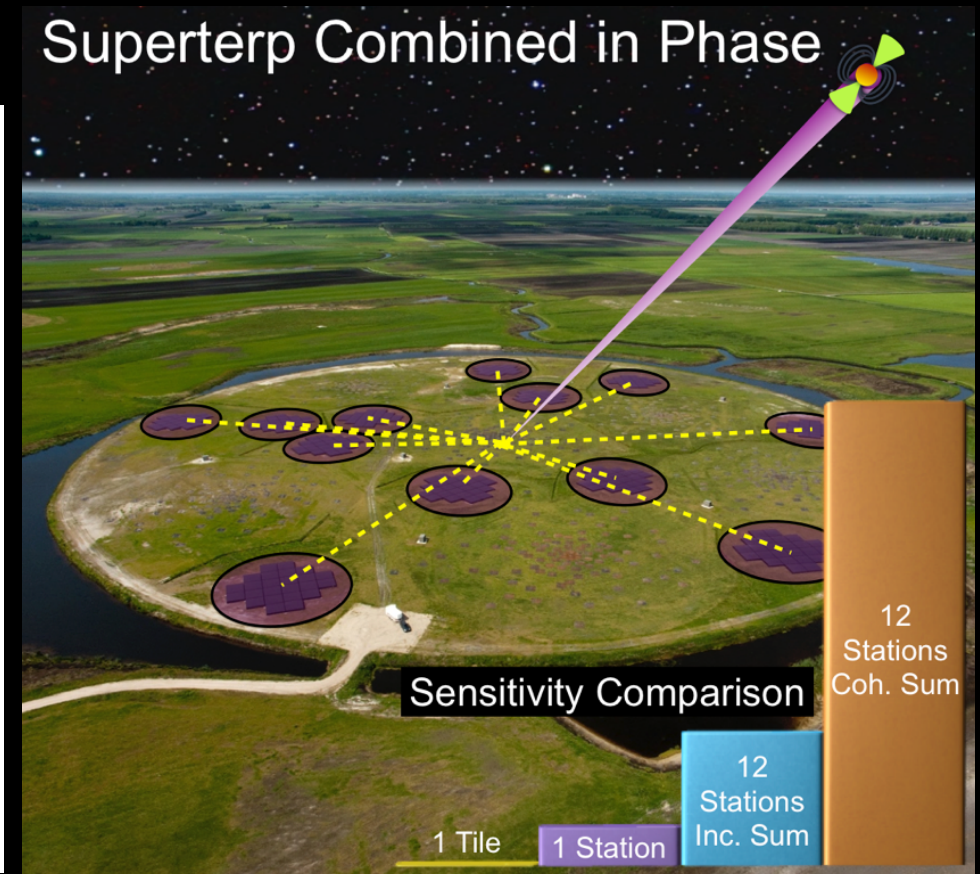


# Choosing CS vs. IS mode

- IS is useful for piggy-backing, but only if you're looking for something relatively bright and rarely occurring.



Hessels



Hessels

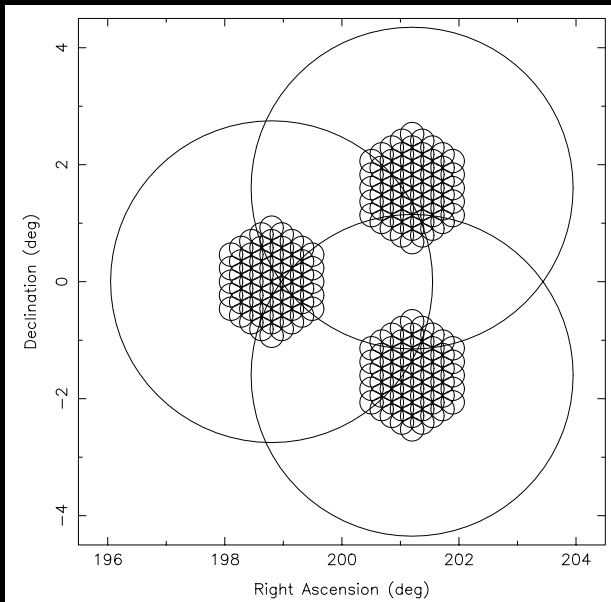
# Choosing time/frequency resolution

- Frequency resolution is often dictated by the requirement to dedisperse (or resolve a spectral line).
- Higher frequency resolution - even if you don't need it - will also help with RFI excision.
- Time resolution can be anywhere from 5 microseconds up to 100s of milliseconds.

# Choosing number of beams

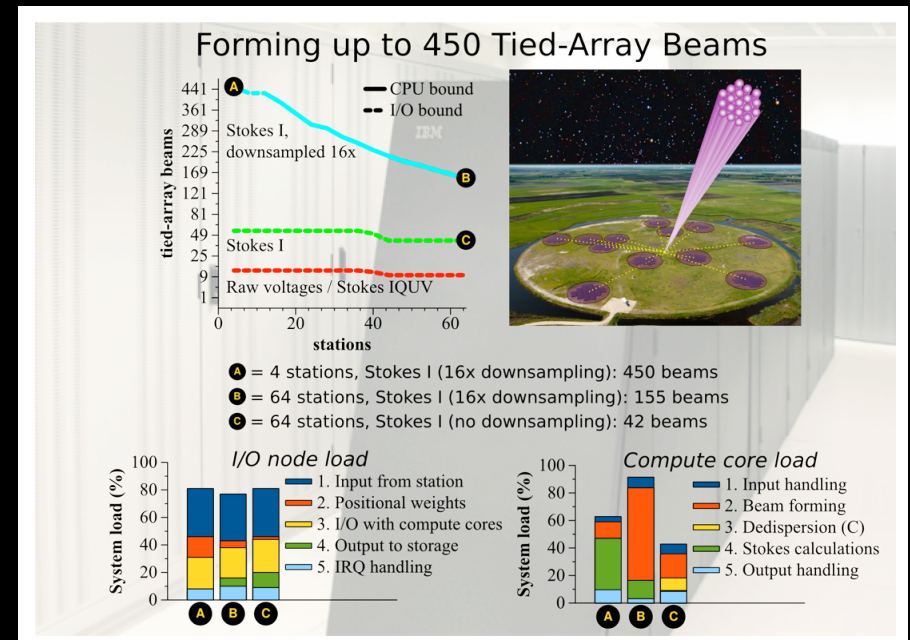
- You can use anywhere from 1 to hundreds of beams - as necessary, but limited by maximum data rate and computing power on COBALT.
- CS + IS can be run in combination.

222-beam LOTAAS pointing



Hessels

Check with Science Support for the latest performance numbers

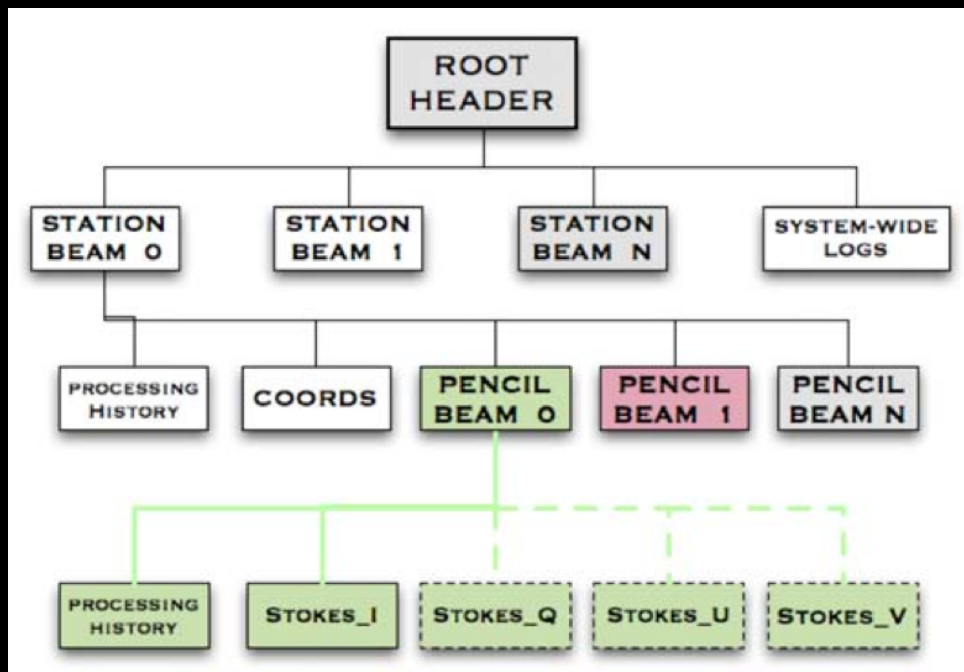


Mol & Romain



# Analyzing LOFAR BF data

# HDF5 format



Alexov - see documentation for LOFAR ICD3

- Separate .raw (data) and .h5 (metadata) file.
- No more than one beam per file.
- One beam can be split into multiple frequency bands.

## Filename structure

Sub-array pointing number      Stokes parameter

LOFAR observation ID      Beam number      Frequency part

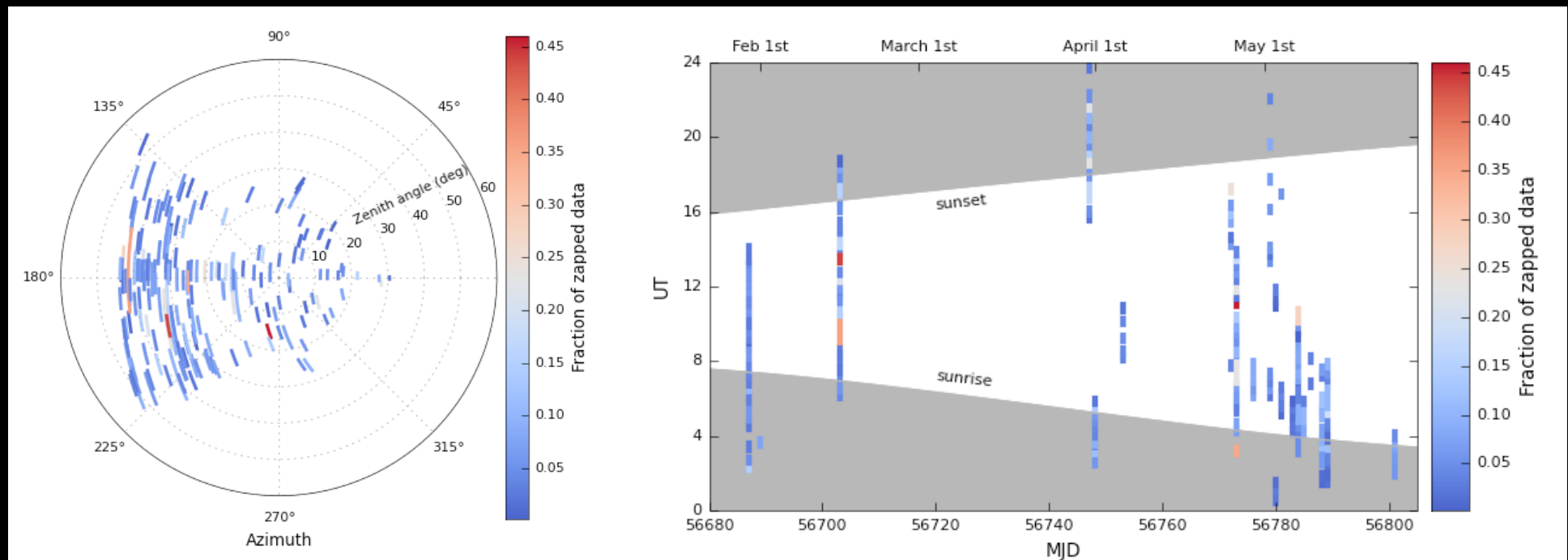
LNNNNNNN\_SAPNNN\_BNNN\_SN\_PNNN\_bf.raw

# PSRFITS format

- The 32-bit HDF5 data is sometimes converted to 8-bit PSRFITS format.
- Allows direct reading into standard 3rd party software packages like PRESTO and PSRCHIVE.
- Quite a bit of the `raw' data in the LTA is in this format.

# RFI excision

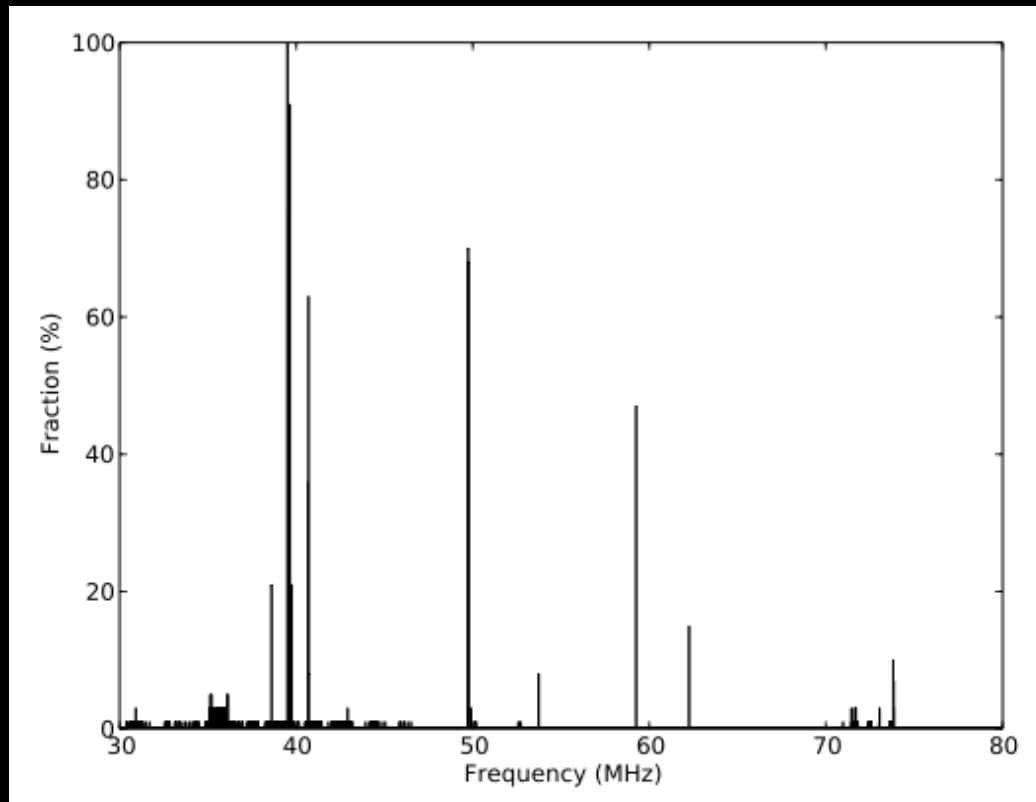
- On average 5-10% of the data need to be excised.
- Signals often very short in time or very narrow in frequency.
- Standard tool is PRESTO's ``rfifind'`.



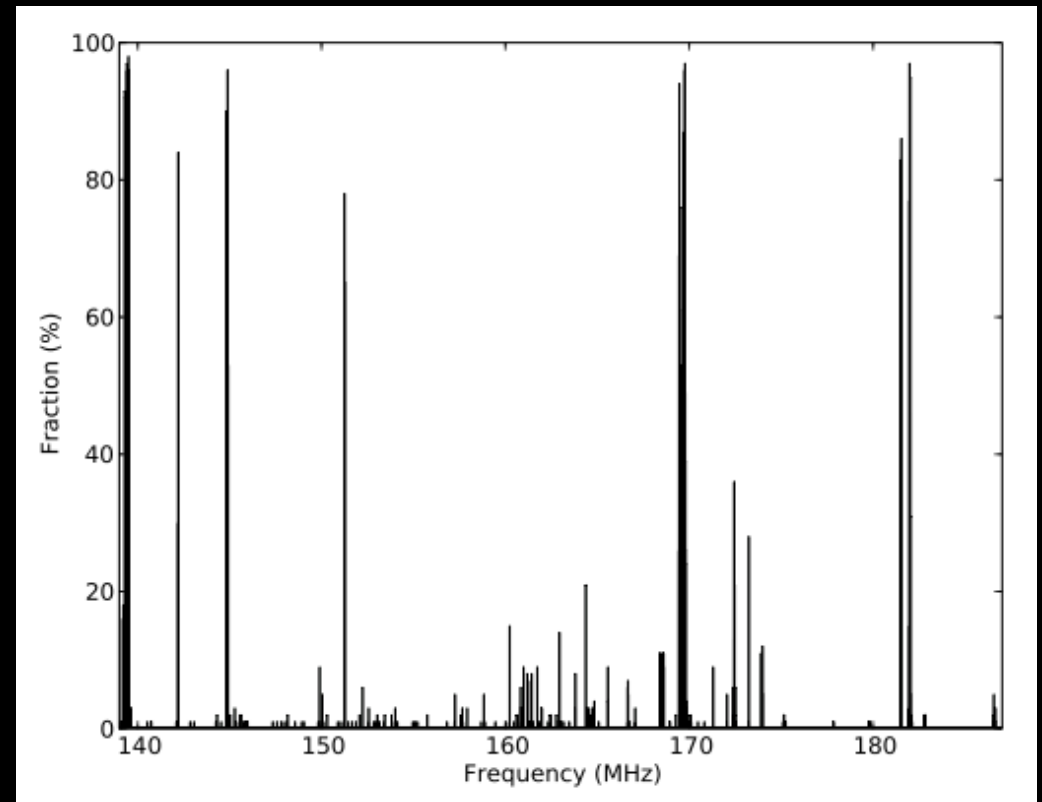


# RFI excision

## LBA - 12-kHz resolution



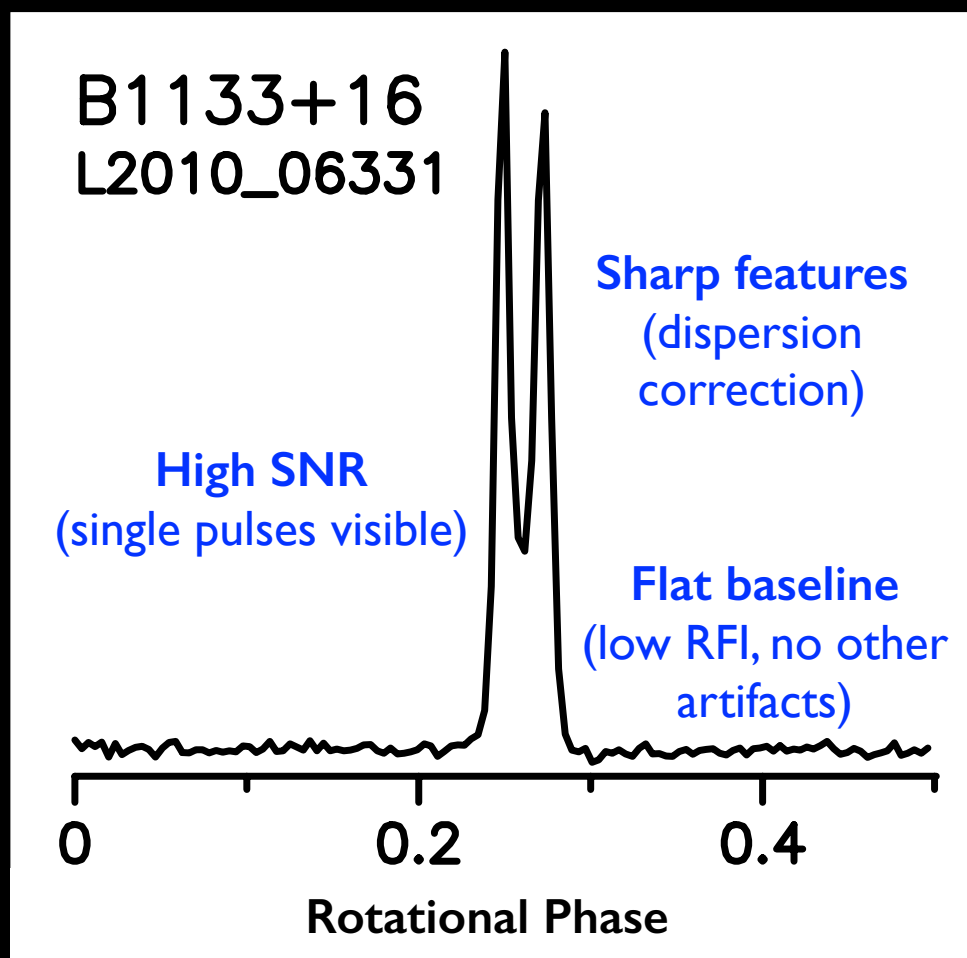
## HBA - 12-kHz resolution



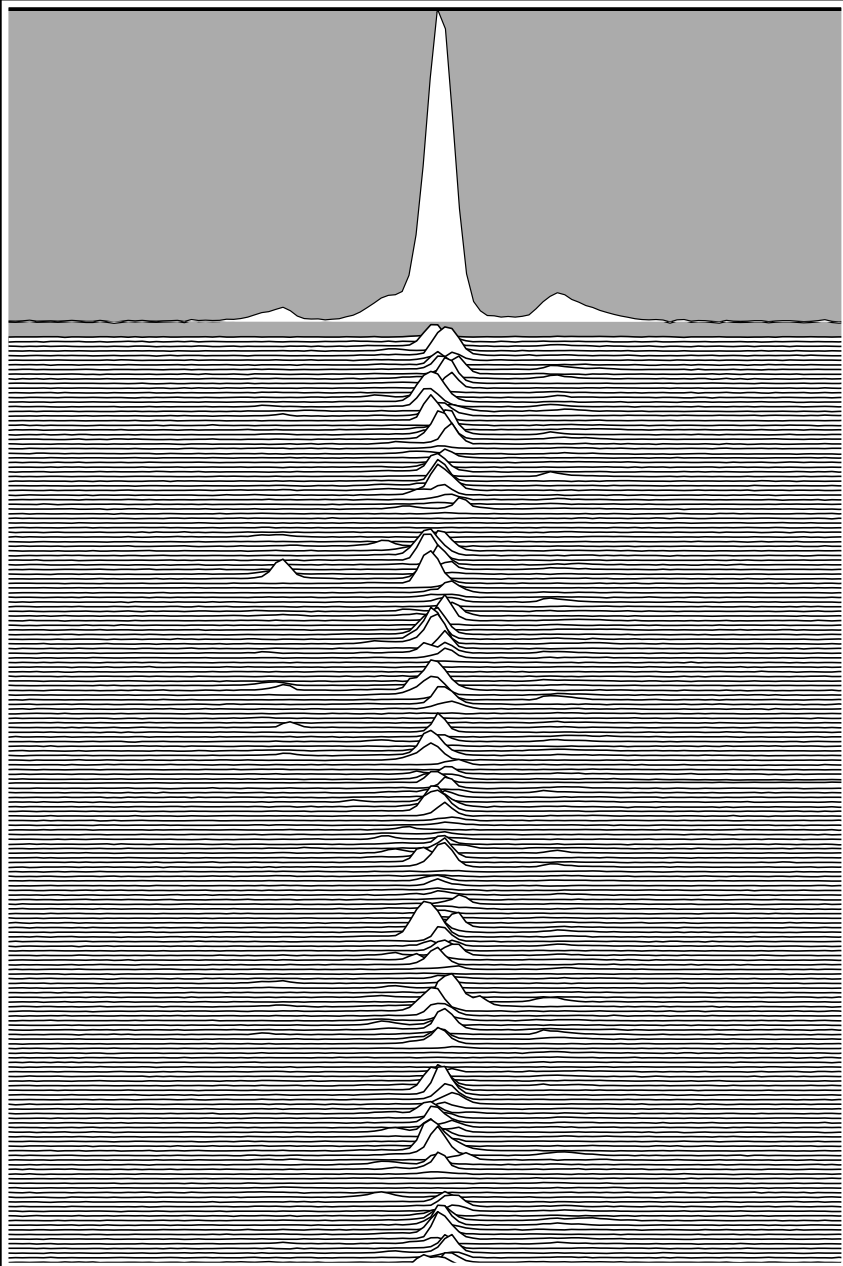
Kondratiev - From Stappers et al. 2011

# Dedispersion

- Standard tools are: PRESTO's 'prepsubband' and the dspsr package.
- Be careful: at very low observing frequencies and/or very high DMs, the dispersive sweep can be a significant fraction of the observation length (or longer!).
- Intra-channel dispersion can also be severe for LOFAR.

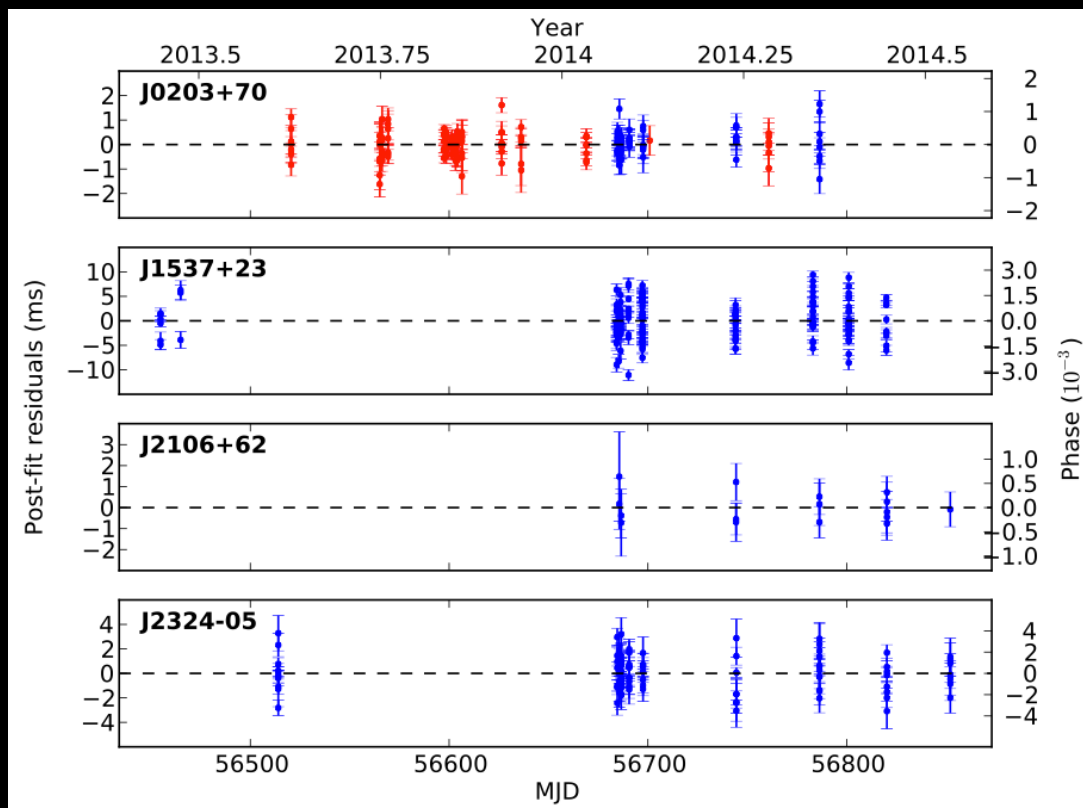


# Pulsar folding



- dspsr and PRESTO's 'prepfold' will both dedisperse and fold the data given an ephemeris or separate input parameters.

# Timing

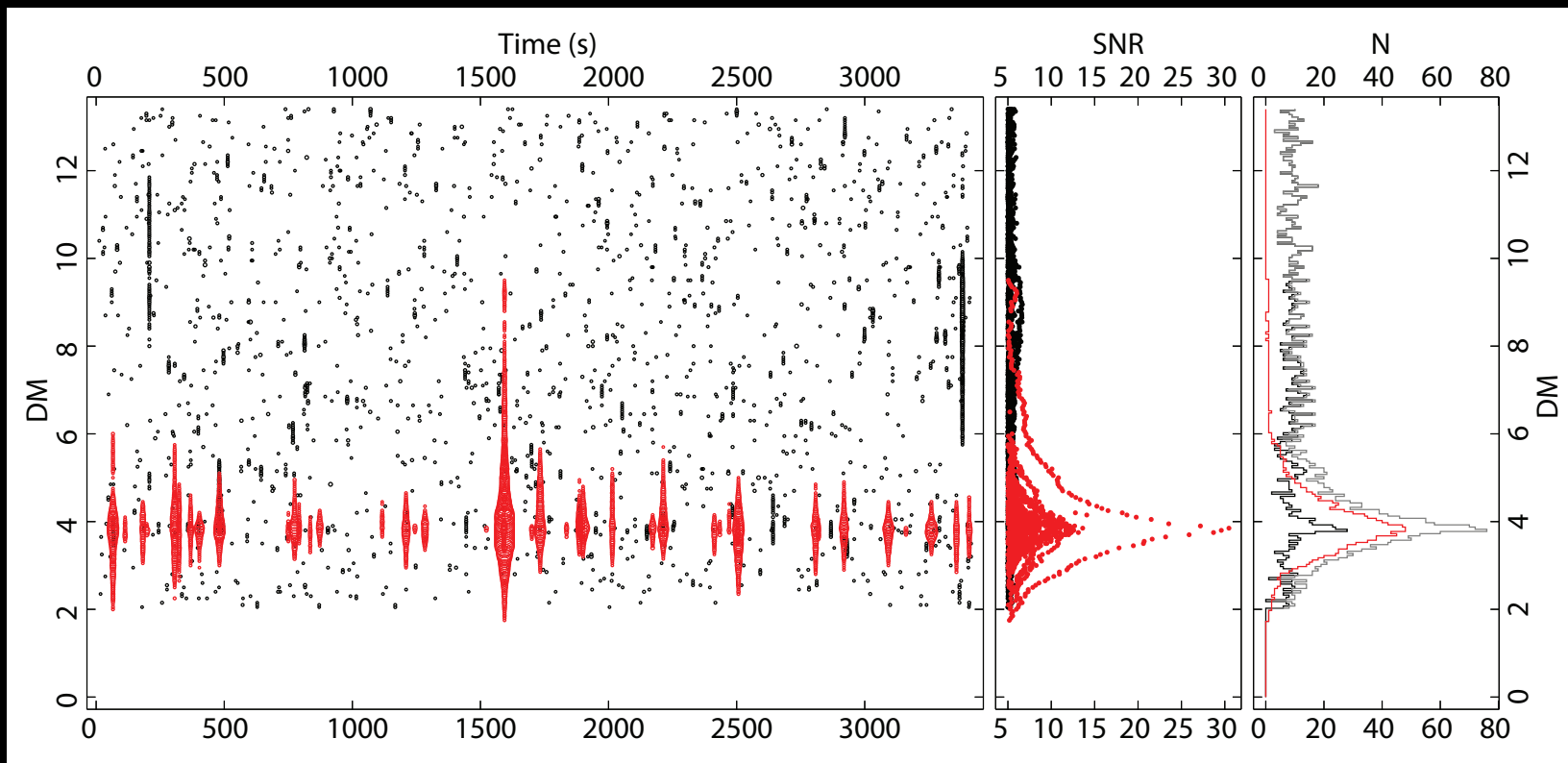


Karako

- LOFAR is known to the standard packages, i.e. TEMPO & TEMPO2.
- LOFAR's position (phase center) is always CS002/LBA.
- Standalone observations will use that station's position.

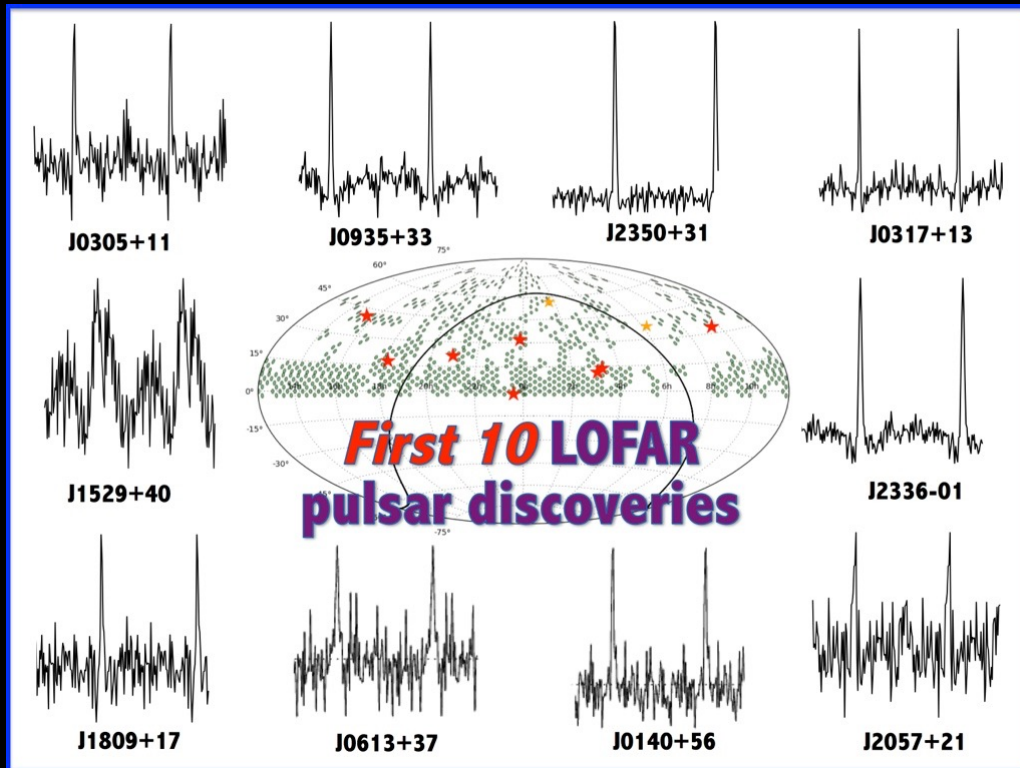
# Single-pulse searches

- Standardly use PRESTO's *single\_pulse\_search.py*.
- A huge amount of events can be generated.
- Talk to Daniele Michilli (UvA) about sifting through these.





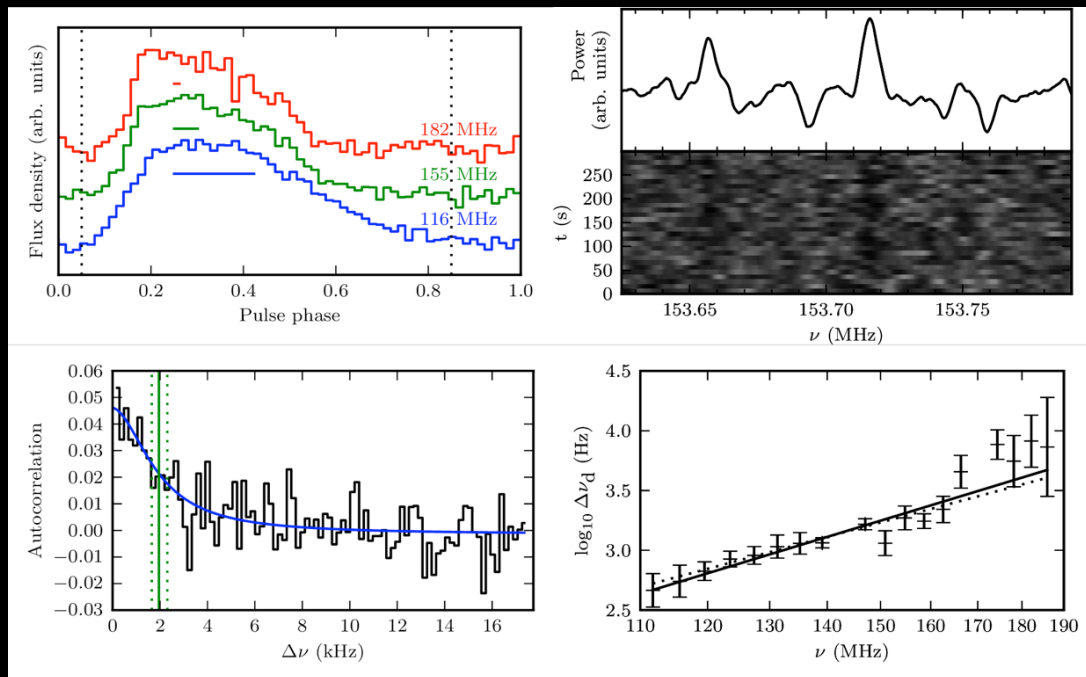
# Periodicity searches



Cooper - LPPS, LOTAS & LOTAAS surveys

- Standardly use PRESTO's *accsearch*.
- Very large numbers of dispersion measure trials needed.
- Processing doesn't fit on CEP2.

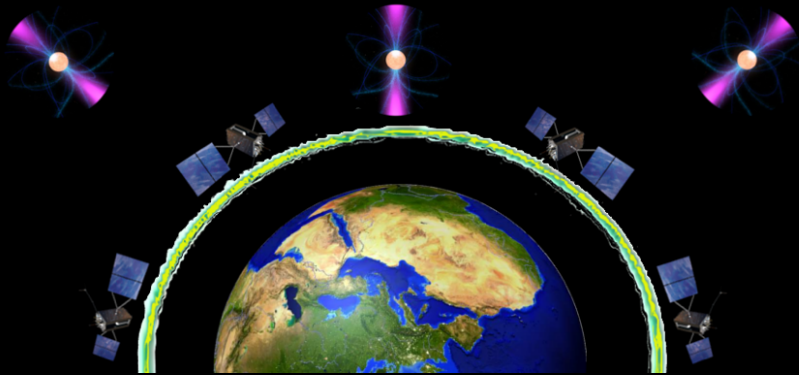
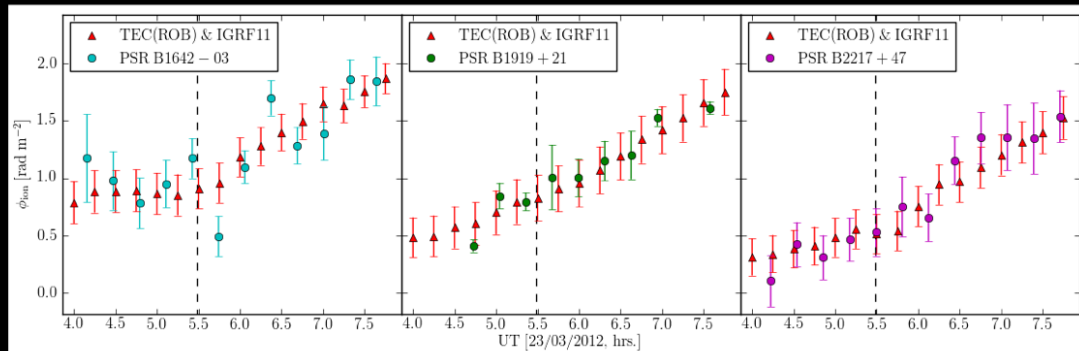
# Cyclic spectroscopy



- Advanced technique that exploits the periodic nature of the pulsar signal to get both high time resolution on the pulsar phase *and* high frequency resolution.

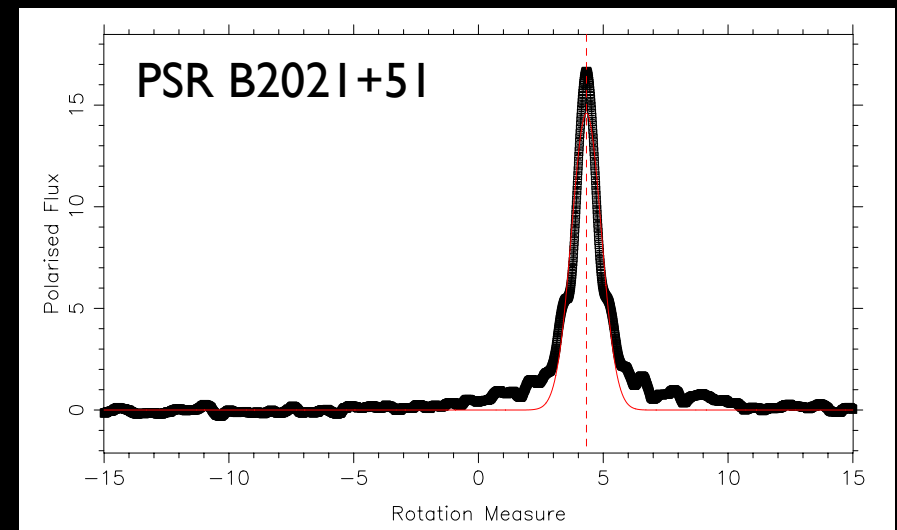
Archibald - From Archibald et al. 2014

# Deriving and applying rotation measures (RMs)



Sobey - From Sotomayor-Beltran et al. 2013

- RM's can be determined very precisely, *but* accuracy may be dominated by ionospheric contribution.



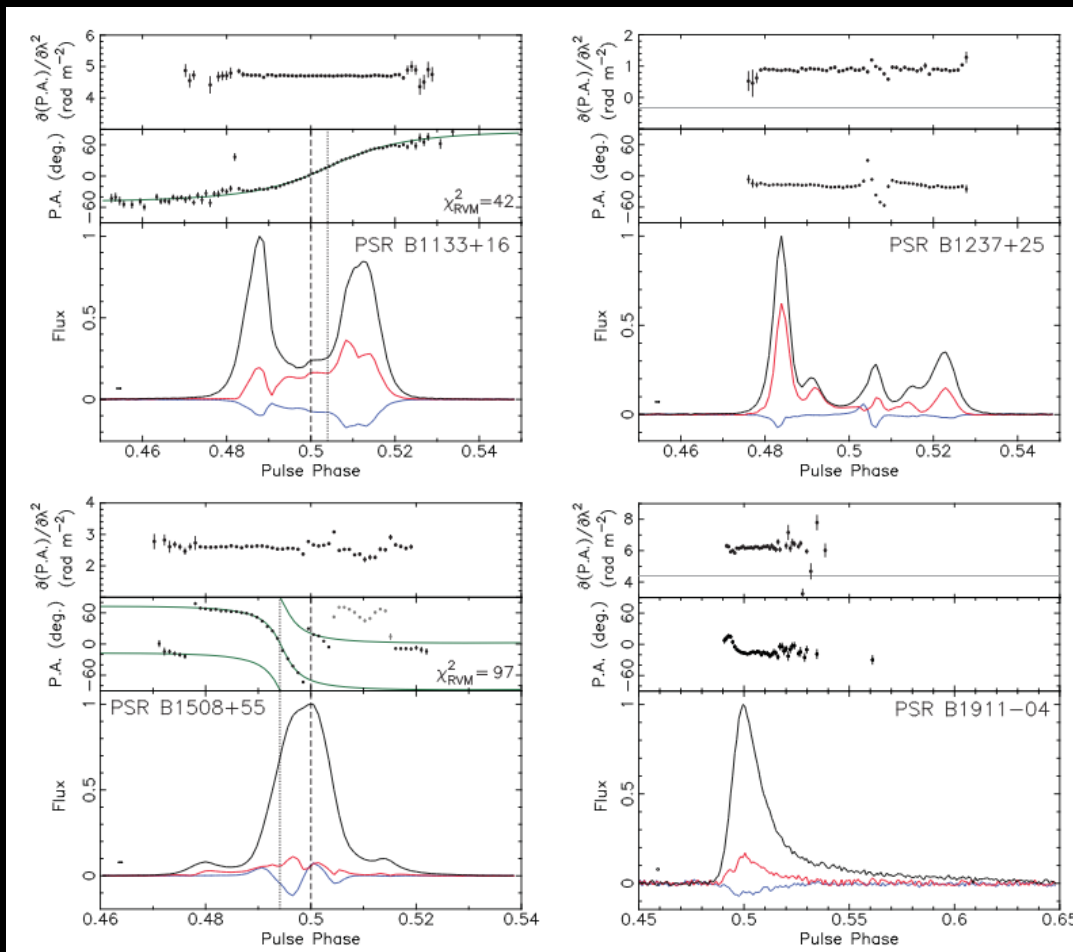
Sobey

# Polarimetric calibration

Black profiles = total intensity

Red profiles = linearly polarized intensity

Blue profiles = circularly polarized intensity



- Standardly implementing polarimetric calibration in the LOFAR Pulsar Pipeline is nearly done.

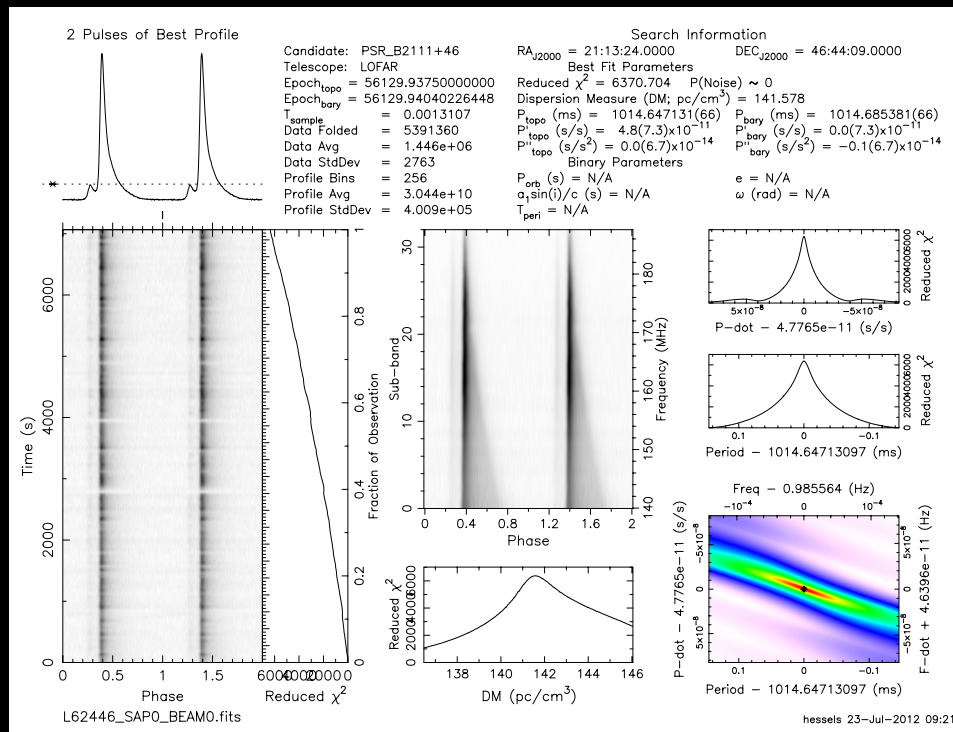
# The LOFAR Standard Pulsar Pipeline (PulP)

- Written by Vlad Kondratiev and Anastasia Alexov.
- Makes use of 3rd party software suites like PRESTO, PSRCHIVE, dspsr, TEMPO, etc.
- Recently incorporated into the LOFAR MoM/Scheduler framework.
- Runs dedispersion, folding, data conversion, RFI excision, limited searches, etc.
- Pulsar equivalent of the Standard Imaging Pipeline.



# PuLP Data Products

## (also in the LTA)



- Raw data in 8-bit format.
- Diagnostic plots.
- RFI mask.
- Data cubes for known sources.
- Source localization.
- Simple dynamic spectra.

Hessels - Automatically generated by PuLP

Scrunched cube of pulsar brightness with time, rotational phase, and observing frequency.

# Future prospects

- Separate station lists for BF/IM data.
- Parallel observing and sub-arraying.
- Online RFI excision - i.e. on a *per station* basis.
- Online coherent dedispersion.

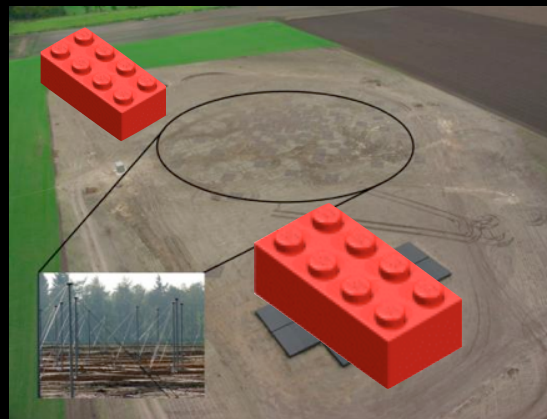
## Sub-arraying

Customize your own telescope



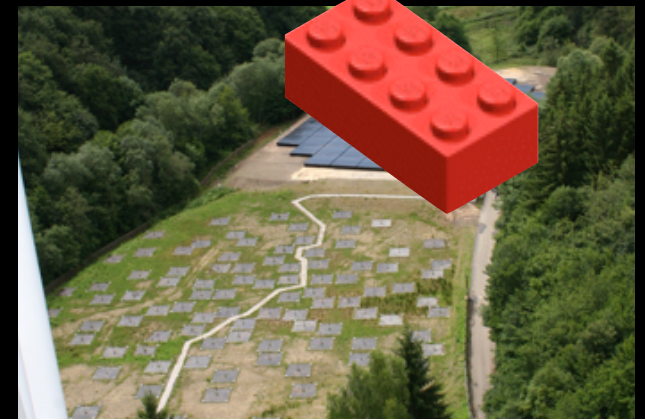
48

Dutch Core  
Stations



16

Dutch Remote  
Stations



8

International  
Stations

THE end

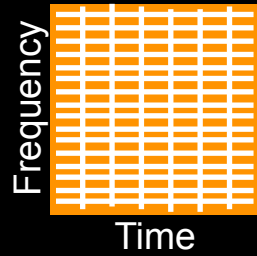
# Appendices

# **Appendix A:**

## **Pulsar searching**



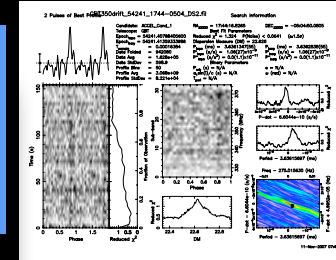
# Standard Pulsar/Fast Transient Search



## RFI Excision

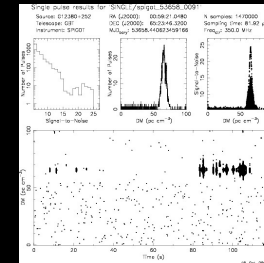
# Dedispersion

# FFT Search



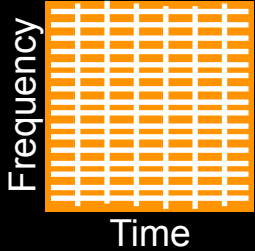
## Cand Sifting

# Single Pulse Search



## Cand Sifting

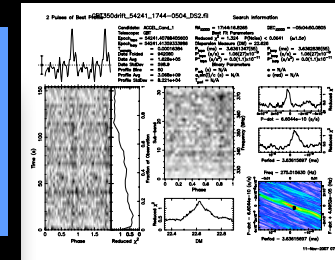
# Standard Pulsar/Fast Transient Search



## RFI Excision

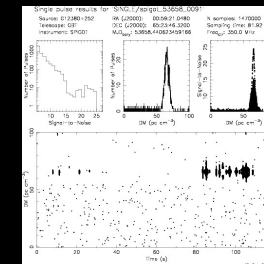
[illegible]

# FFT Search



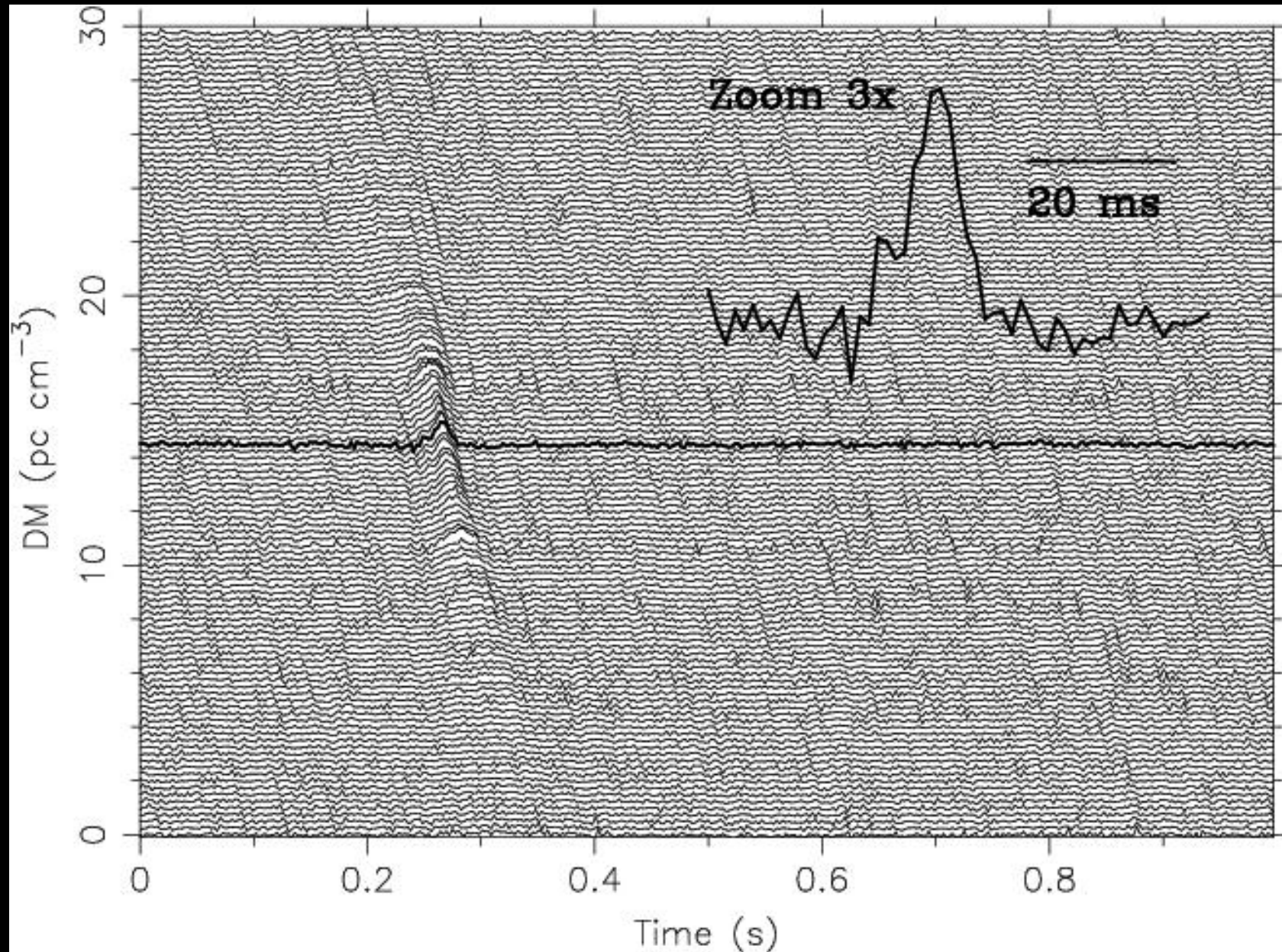
## Cand Sifting

## Single Pulse Search

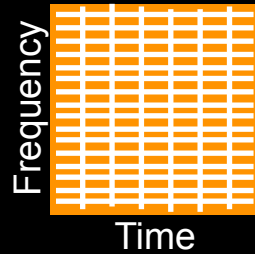


# Cand Sifting

# Searching over dispersion measure



# Standard Pulsar/Fast Transient Search



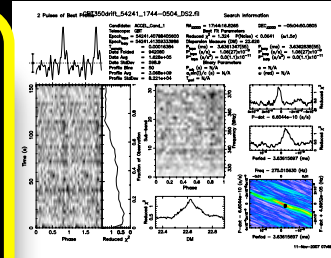
RFI  
Excision



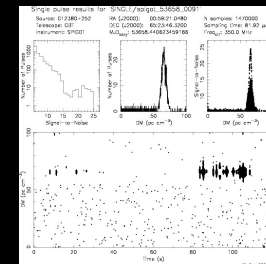
Dedispersion

FFT  
Search

Single  
Pulse  
Search

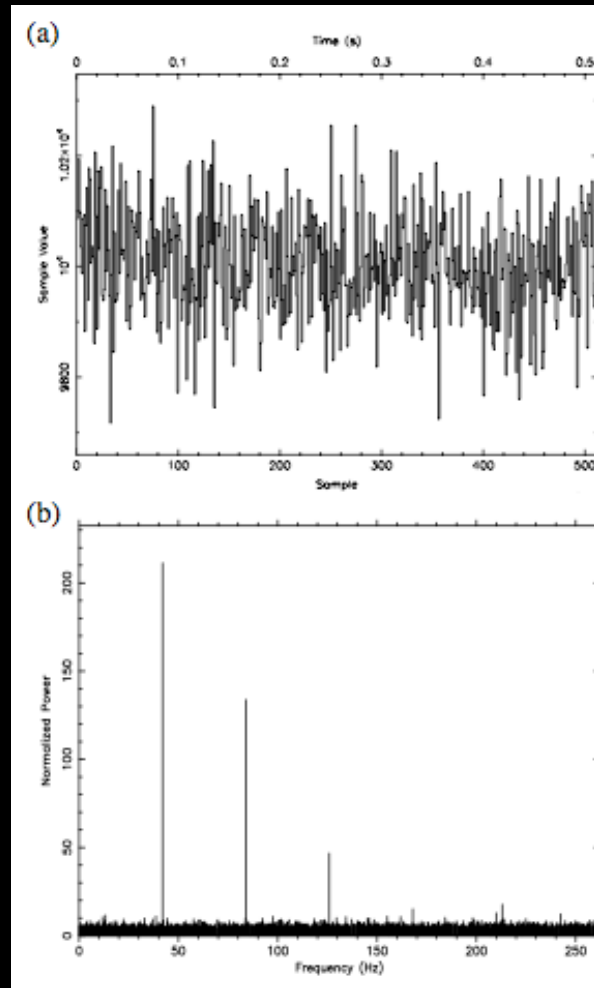


Cand  
Sifting

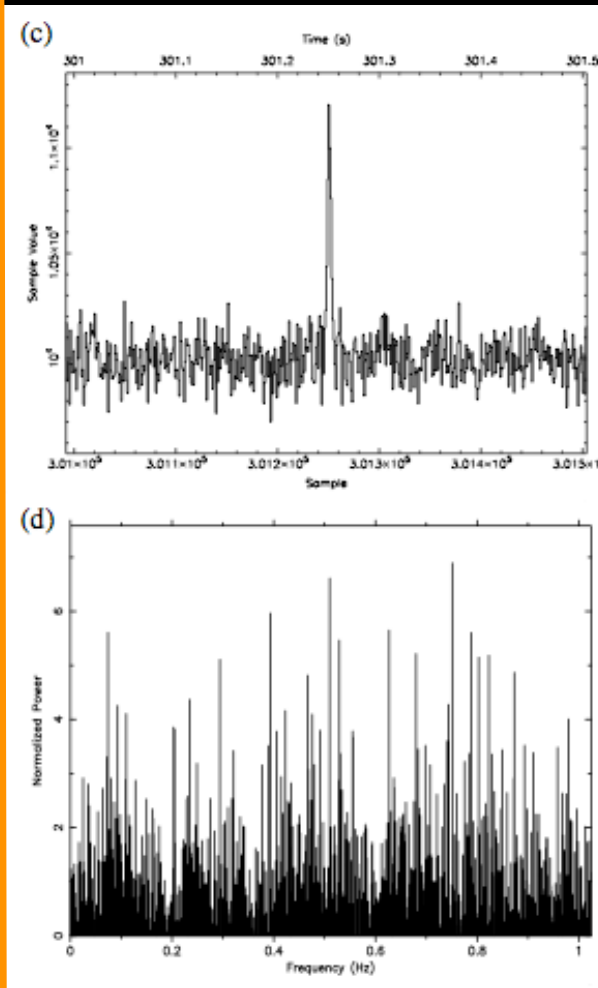


Cand  
Sifting

# Periodic signals vs. bursts



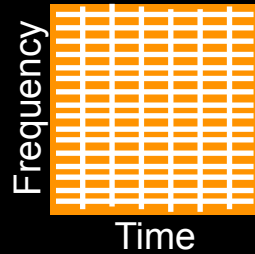
Fourier techniques



Time-series techniques



# Standard Pulsar/Fast Transient Search



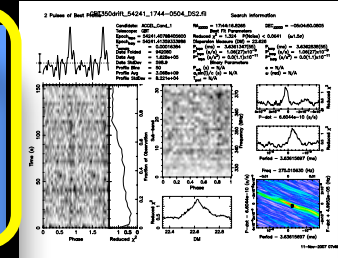
RFI  
Excision



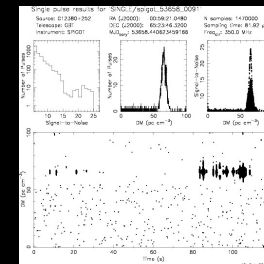
Dedispersion

FFT  
Search

Single  
Pulse  
Search



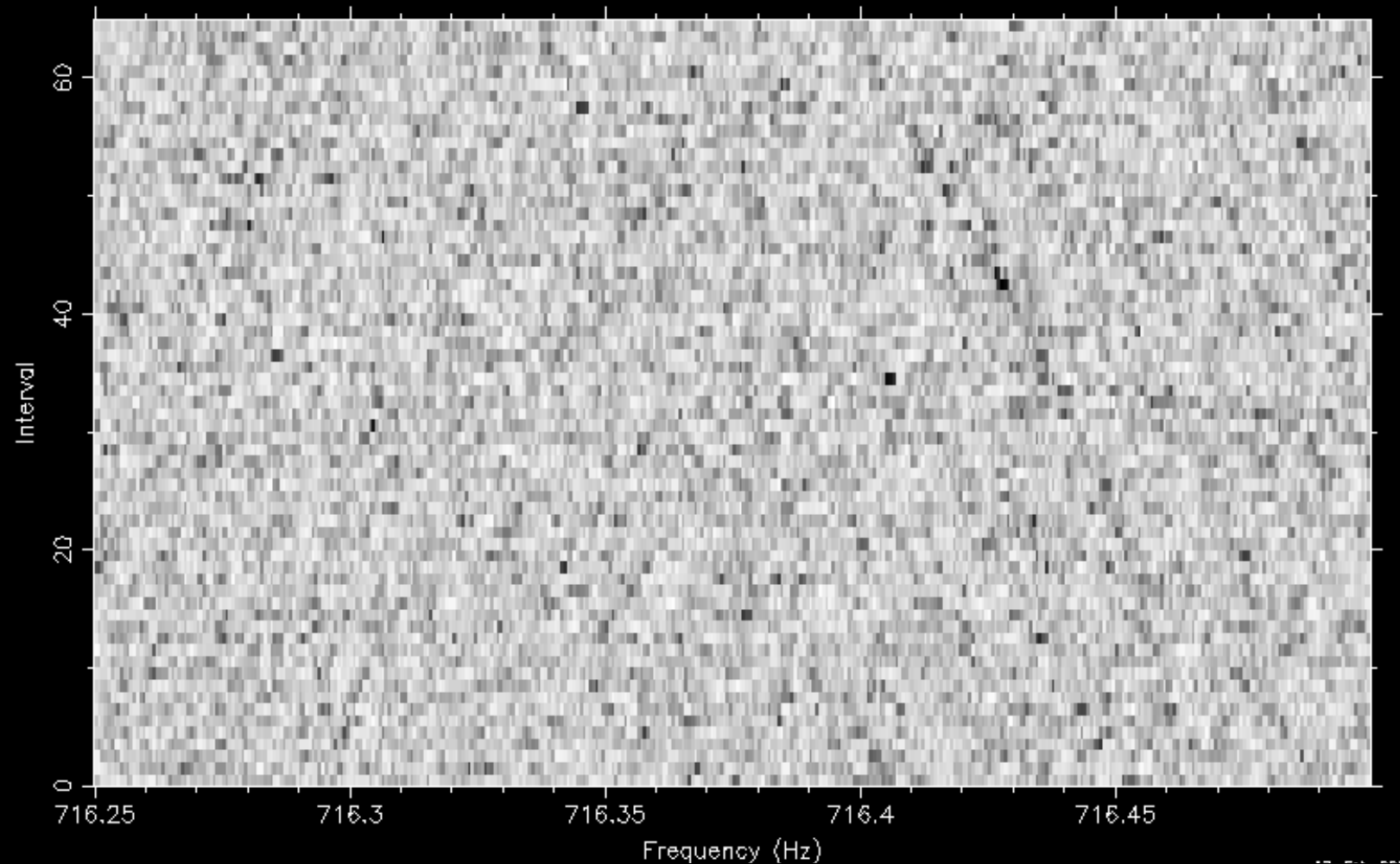
Cand  
Sifting



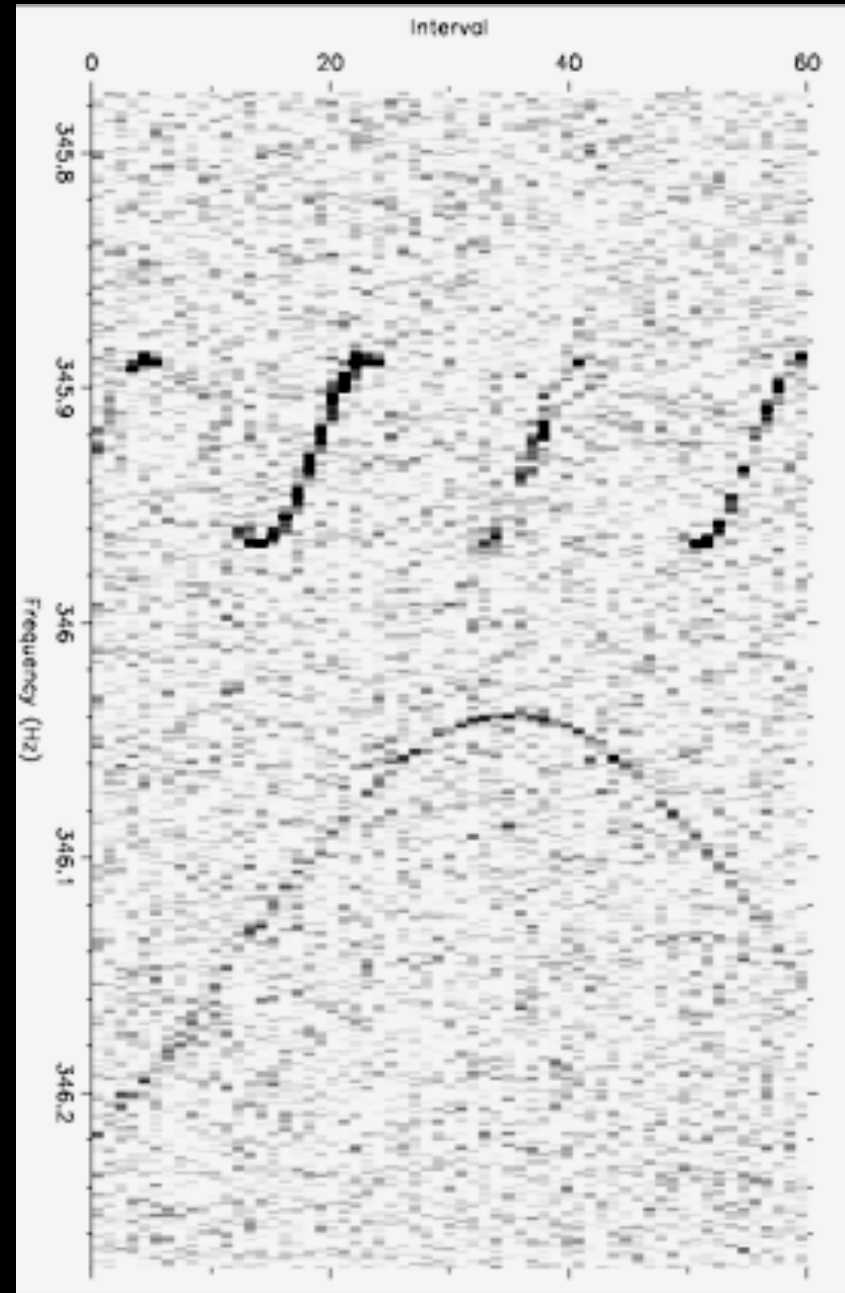
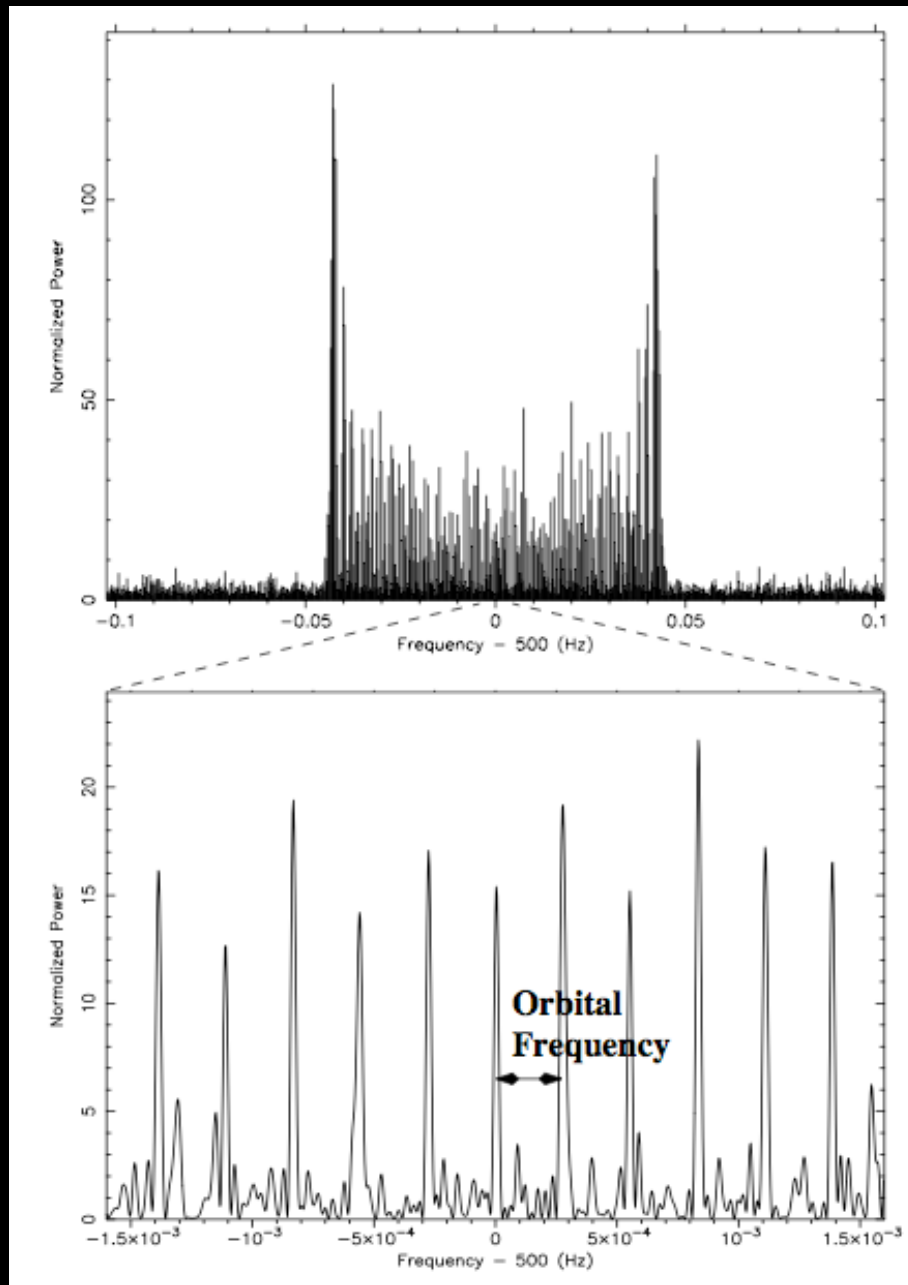
Cand  
Sifting

# Detecting Binary Pulsars

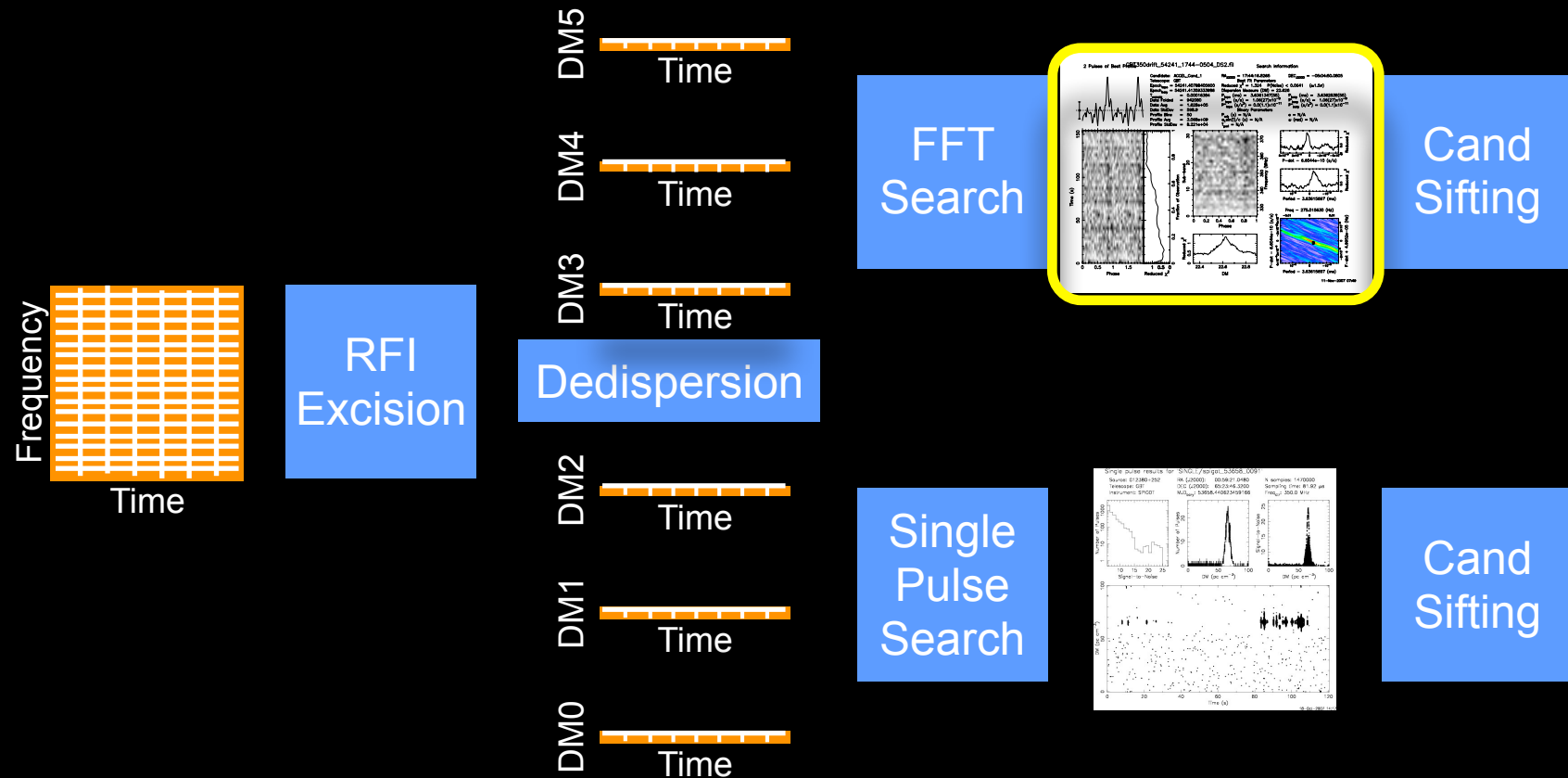
Dynamic Spectrum: SPIGOT\_Ter5\_080204\_topo\_DM235.60.dat



# Detecting Binary Pulsars



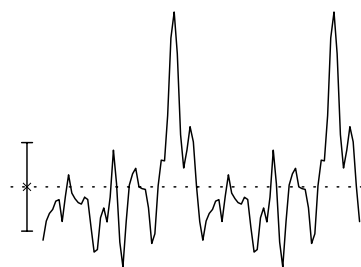
# Standard Pulsar/Fast Transient Search



# FFT (acceleration) searches

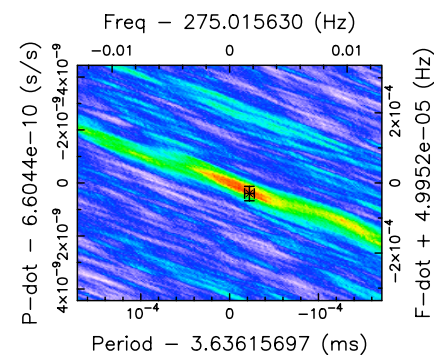
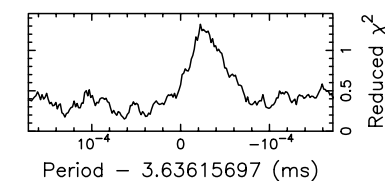
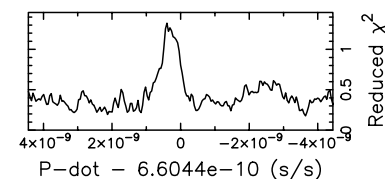
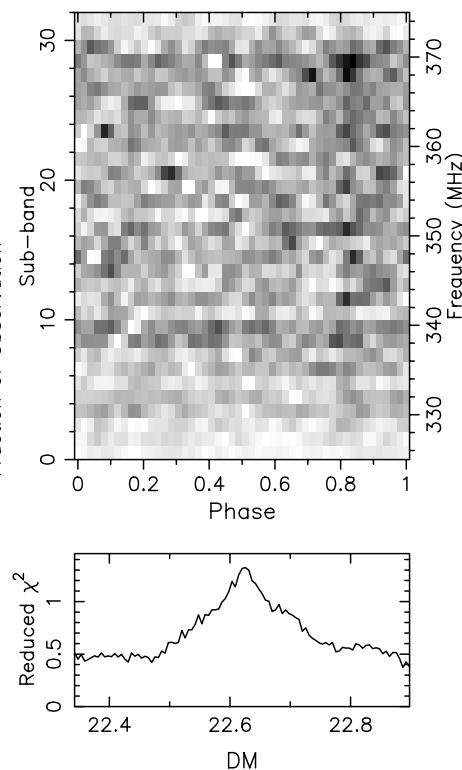
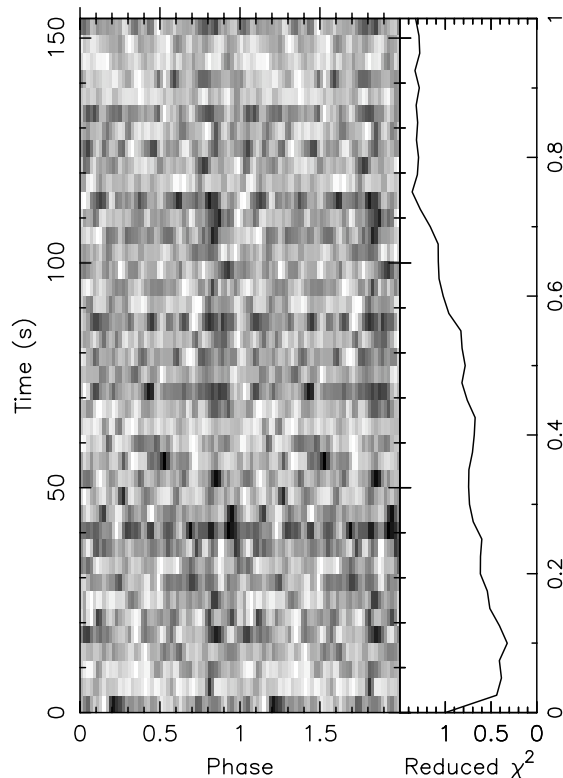
2 Pulses of Best Profile GBT350drift\_54241\_1744-0504\_DS2.fil

Search Information



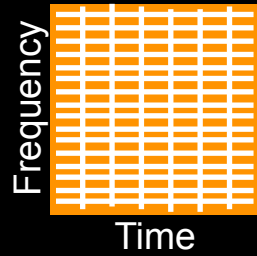
Candidate: ACCEL\_Cand\_1  
 Telescope: GBT  
 Epoch<sub>topo</sub> = 54241.40788405600  
 Epoch<sub>bary</sub> = 54241.41359333986  
 T<sub>sample</sub> = 0.00016384  
 Data Folded = 942080  
 Data Avg = 1.628e+05  
 Data StdDev = 598.9  
 Profile Bins = 50  
 Profile Avg = 3.068e+09  
 Profile StdDev = 8.221e+04

RA<sub>J2000</sub> = 17:44:16.8265  
 DEC<sub>J2000</sub> = -05:04:50.0805  
 Best Fit Parameters  
 Reduced  $\chi^2$  = 1.324 P(Noise) < 0.0641 ( $\approx 1.5\sigma$ )  
 Dispersion Measure (DM) = 22.626  
 P<sub>topo</sub> (ms) = 3.6361347(55) P<sub>bary</sub> (ms) = 3.6362838(55)  
 P'<sub>topo</sub> (s/s) = 1.06(27) $\times 10^{-9}$  P'<sub>bary</sub> (s/s) = 1.06(27) $\times 10^{-9}$   
 P''<sub>topo</sub> (s/s<sup>2</sup>) = 0.0(1.1) $\times 10^{-11}$  P''<sub>bary</sub> (s/s<sup>2</sup>) = 0.0(1.1) $\times 10^{-11}$   
 Binary Parameters  
 P<sub>orb</sub> (s) = N/A e = N/A  
 a<sub>1</sub>sin(i)/c (s) = N/A  $\omega$  (rad) = N/A  
 T<sub>peri</sub> = N/A





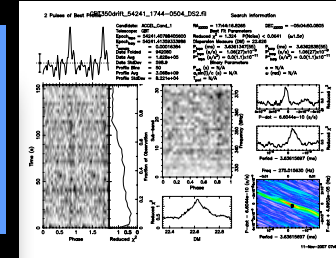
# Standard Pulsar/Fast Transient Search



## RFI Excision

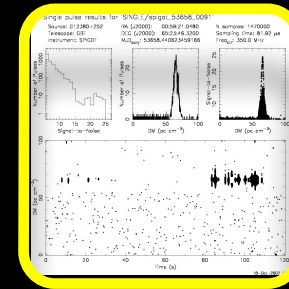
# Dedispersion

# FFT Search



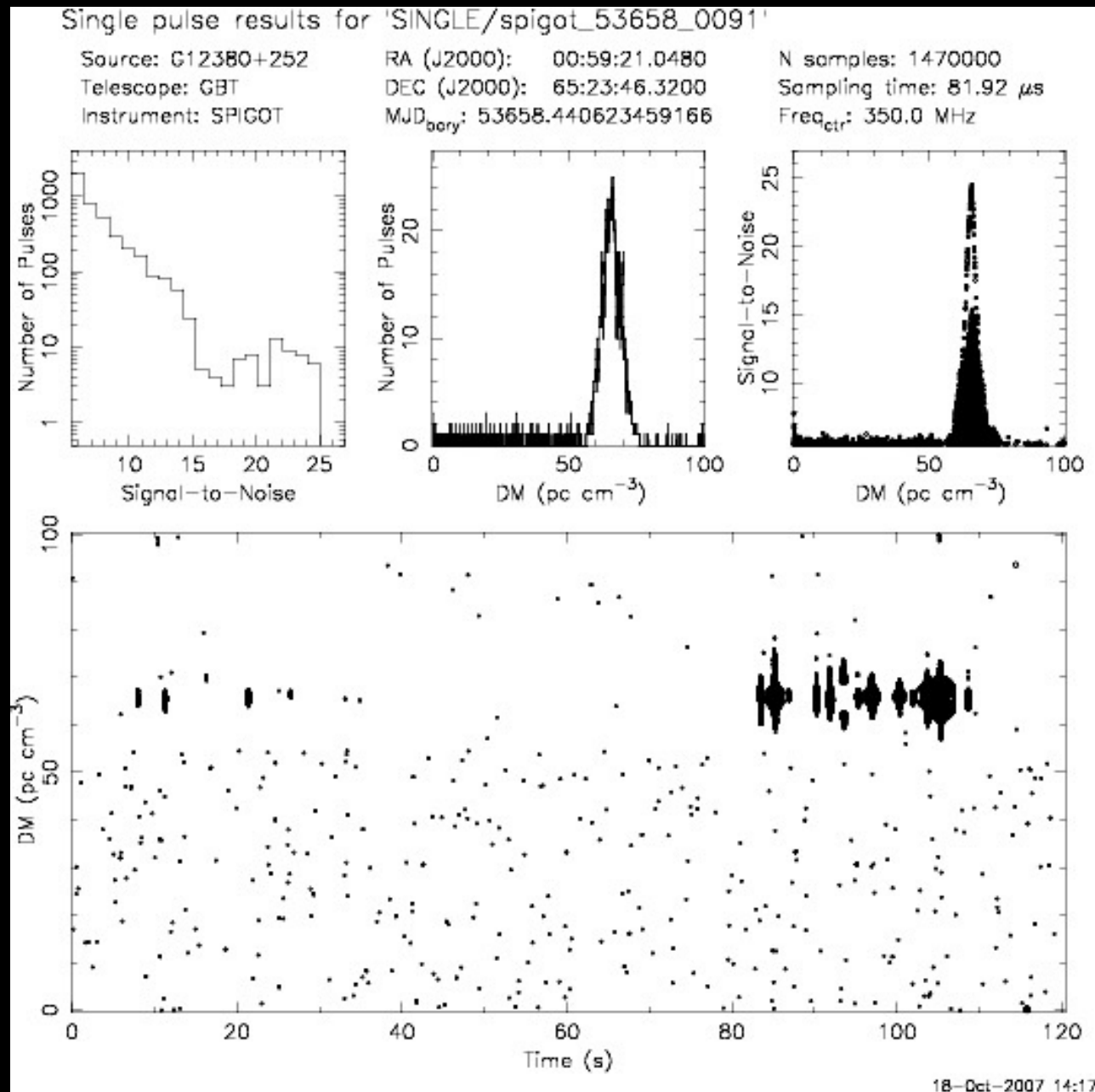
## Cand Sifting

# Single Pulse Search



## Cand Sifting

# Single pulse searches

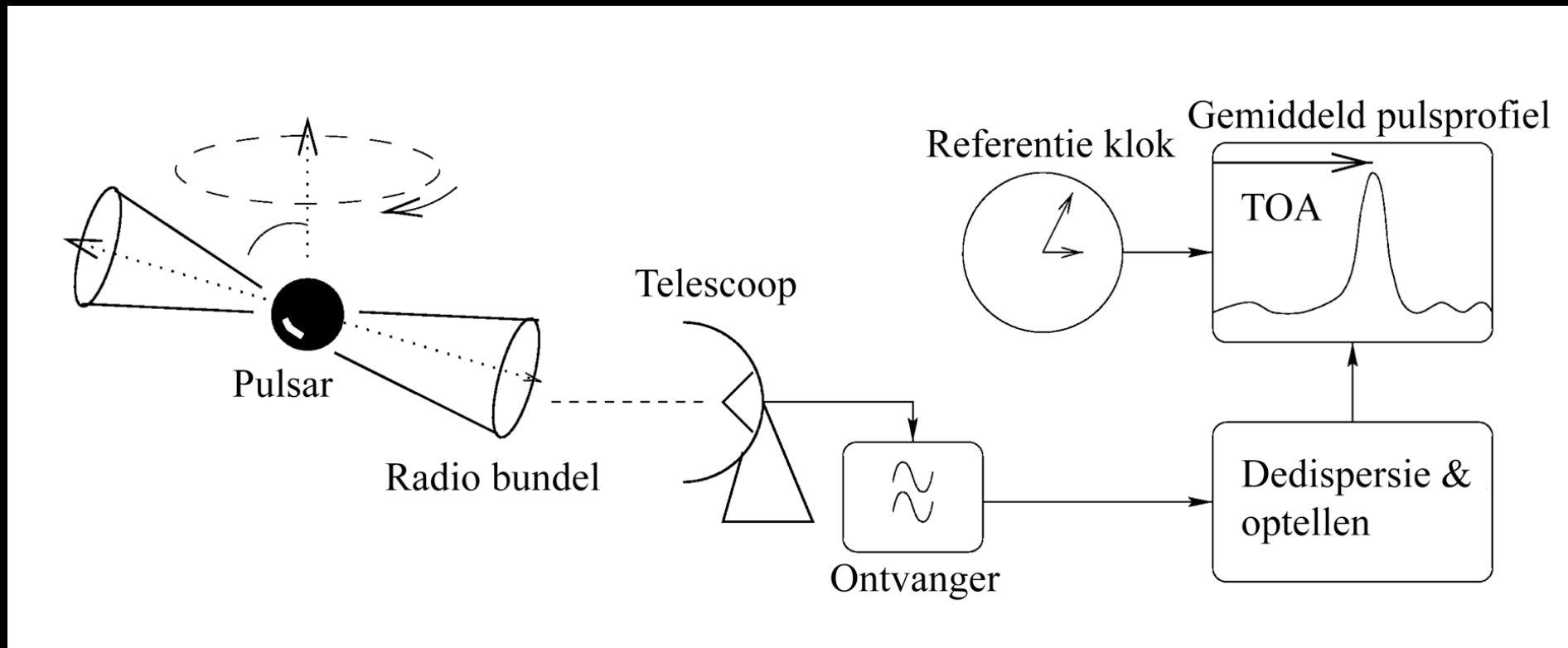


# **Appendix B:**

## **Pulsar timing**

# Basics of Pulsar Timing

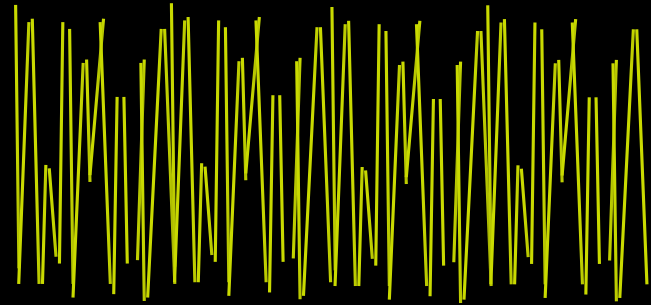
## Instrumentation



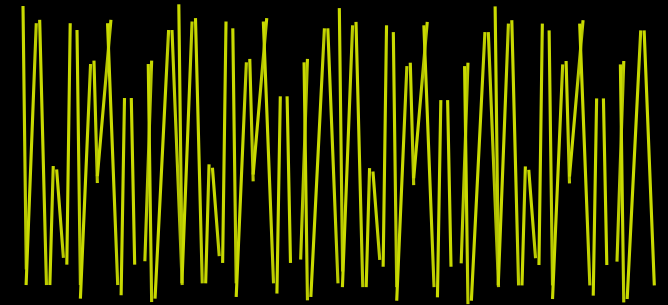
Clock corrections are essential

Also need to transfer to the SSB

# Basics of Pulsar Timing



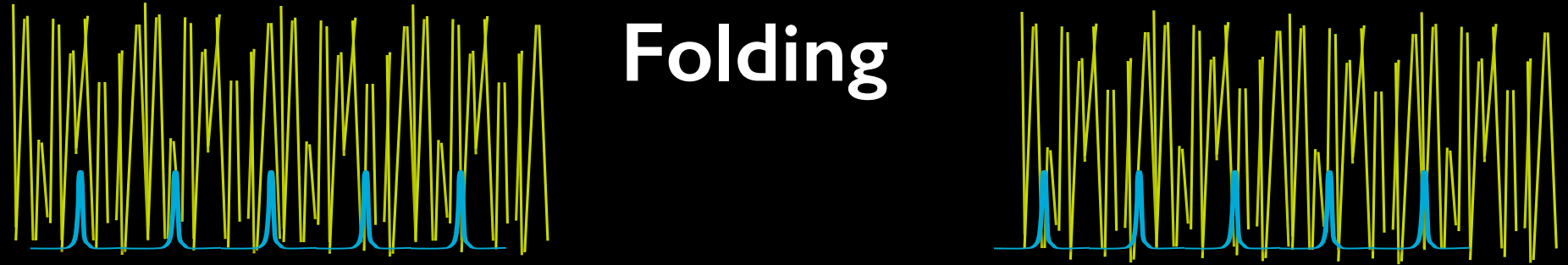
**Folding**



dedispersed data

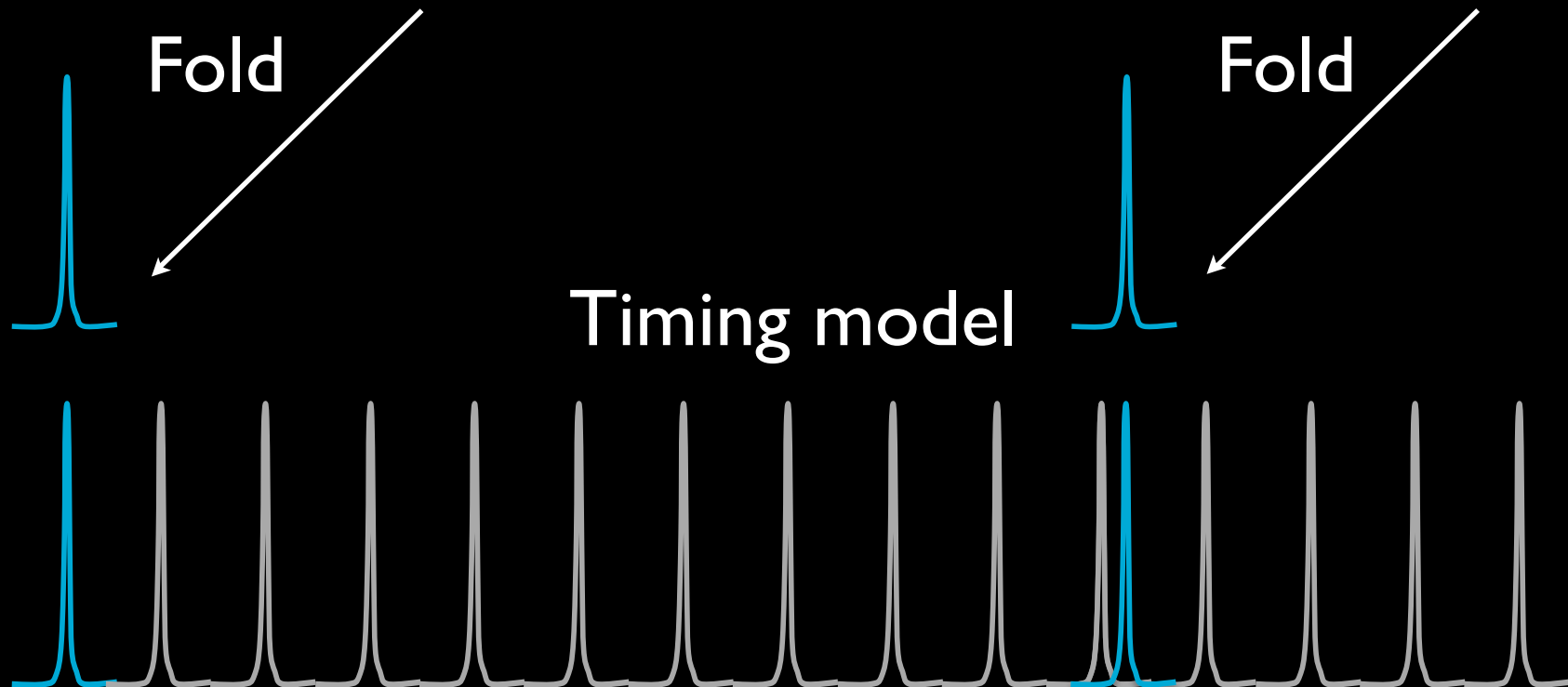


# Basics of Pulsar Timing



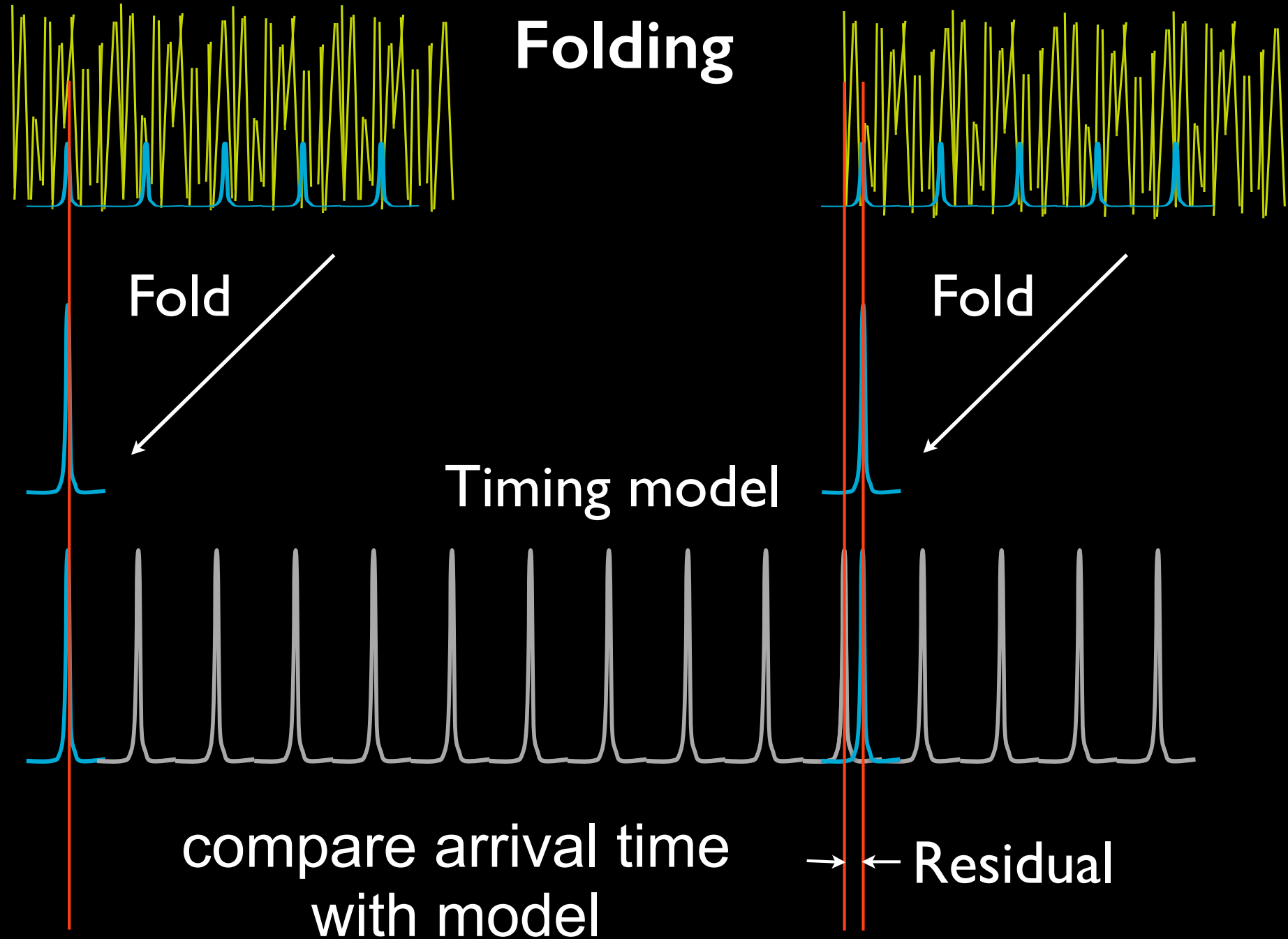
individual pulses are buried in the noise

# Basics of Pulsar Timing



how many rotations are there between observations?

# Basics of Pulsar Timing



# Pulsar Timing Model

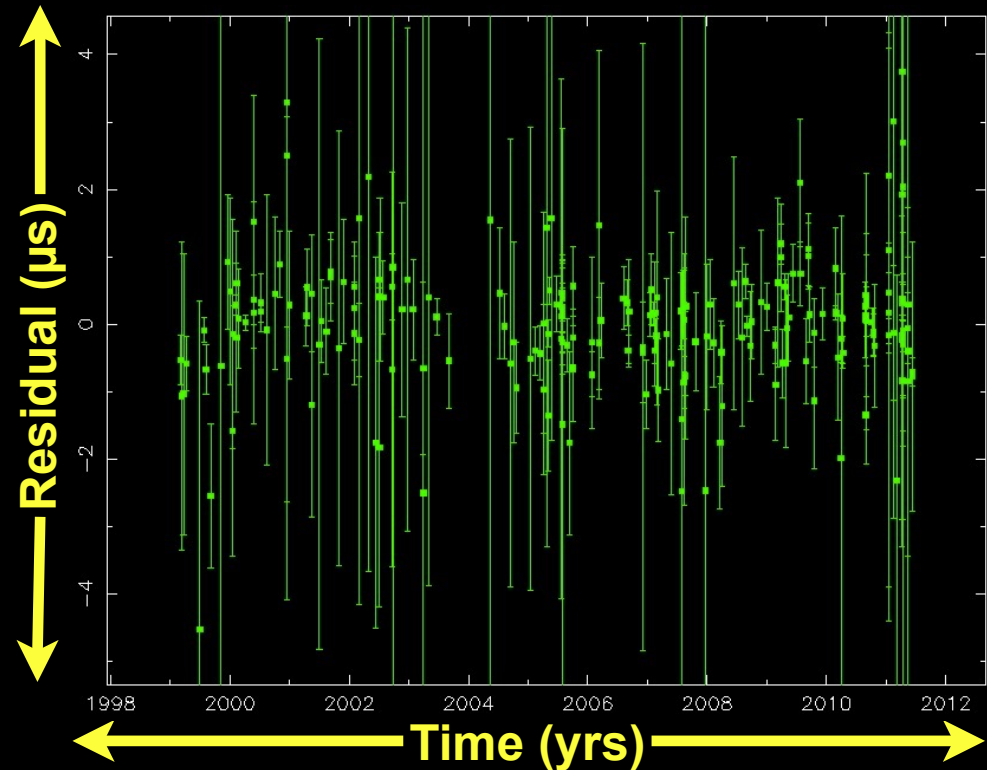
Basic Method:

Actual Pulse TOA

— Theoretical Model

---

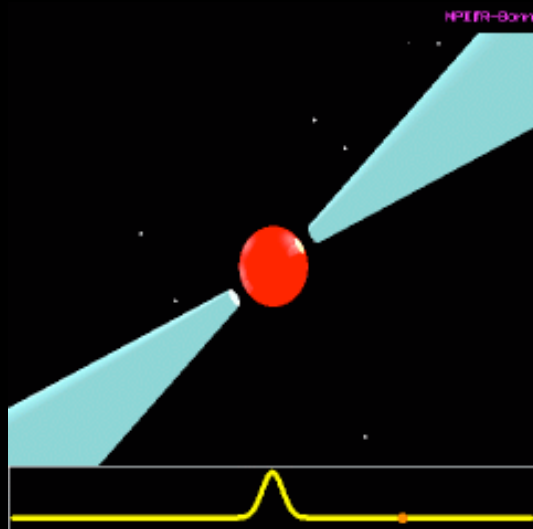
= Timing Residual



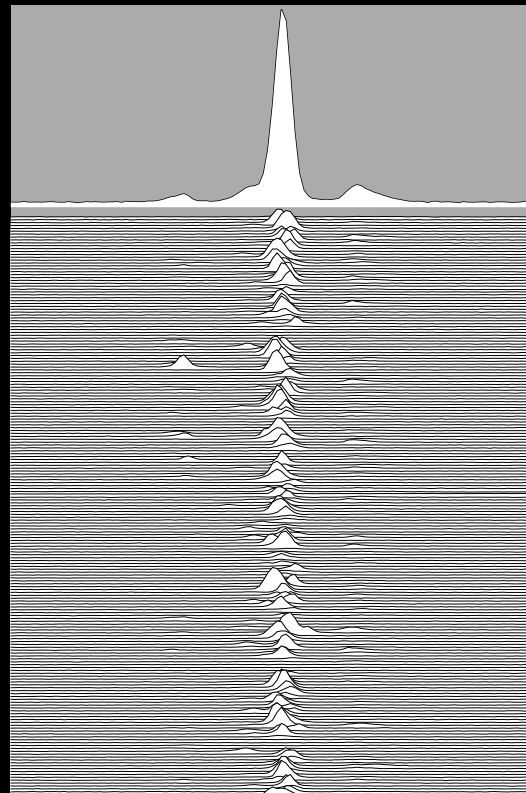
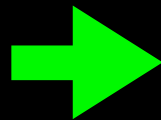
Courtesy Andrew Jameson (Swinburne)

$$T_{\text{th}} = \nu t + \frac{1}{2} \dot{\nu} t^2 + D \frac{\int_0^d n_e dl}{f^2} - \frac{1}{c} (\vec{r} \cdot \hat{s}) + \frac{V_{\text{T}}^2 t^2}{2cd} - \frac{(\vec{r} \times \hat{s})^2}{2cd} + \dots$$

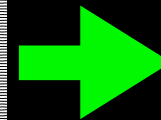
# Pulsars timing process



Collect pulses



Dedisperse, fold  
and cross-  
correlate with  
template



54255.1231254524233  
54255.2643443523453  
54255.3123524545899  
54255.3513745623467  
54255.4418456543355  
54255.5001234234688

Times of arrival  
(TOAs)

# TOA Precision

Big, Sensitive Telescope (duh)

Long Observations,  
Wide Bandwidth

Fast, Bright Pulsar

$$\sigma_{\text{TOA}} \propto \left( \frac{T_{\text{sys}}}{A_{\text{eff}}} \right) \times \left( \frac{1}{\sqrt{T_{\text{obs}} \Delta \nu}} \right) \times \left( \frac{P \delta^{3/2}}{S_{\text{PSR}}} \right)$$

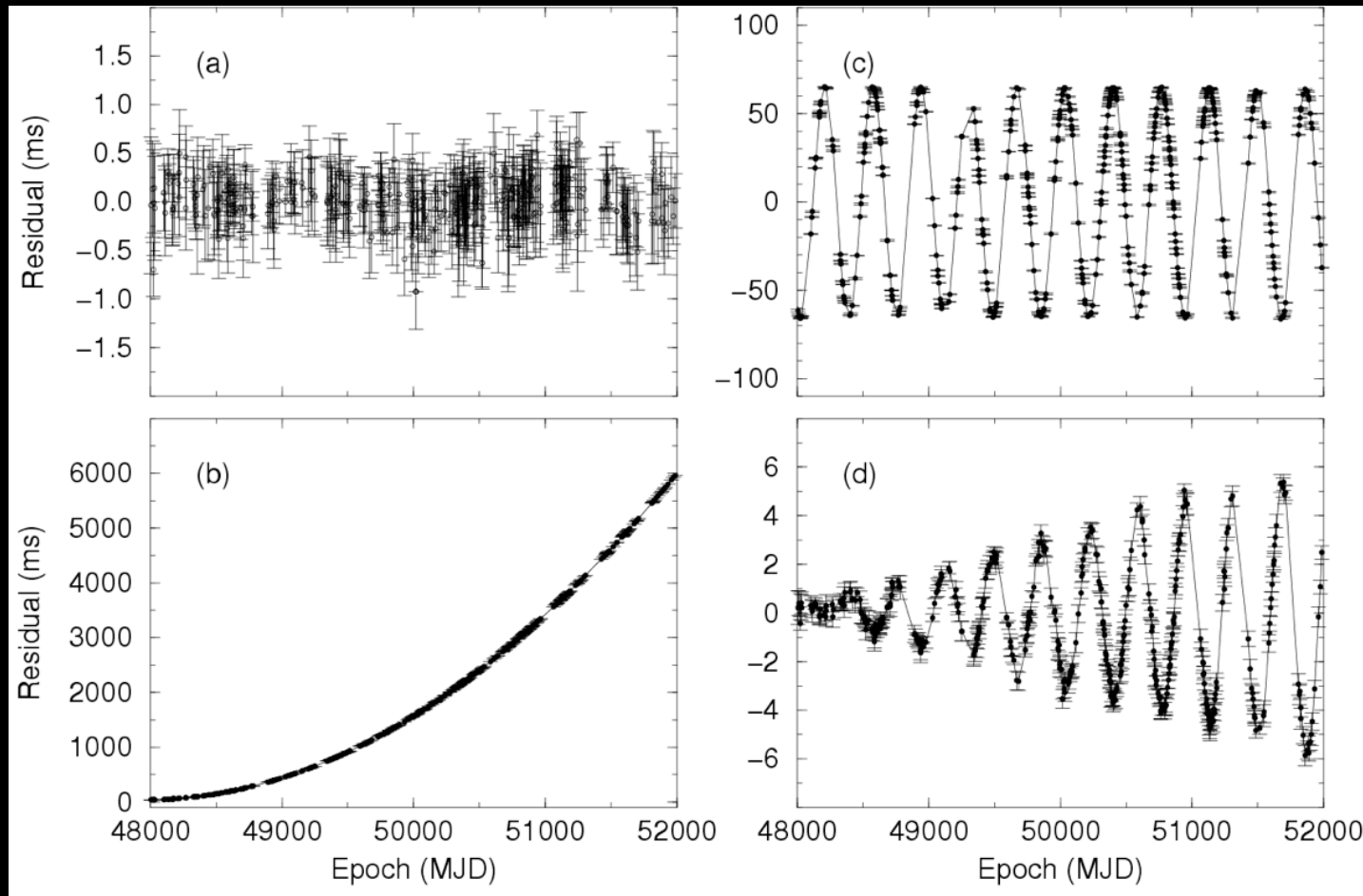
Important Note:

$$S_{\text{PSR}} \propto \nu^{\alpha}$$

$$\text{with } \alpha \approx -1.6 < 0$$



# Pulsar Timing Model



Coherent timing: use TOAs to unambiguously count every single rotation of pulsar over timescales of years.

**Warning: some parameters are covariant!!!**

# Pulsar Timing

## **“Phase connecting”**

Coherent timing: use TOAs to unambiguously count every single rotation of pulsar over timescales of years.

Rotational ephemeris can provide:

Precise astrometry (sub-arcsecond)

Proper motion

Glitches in rotation

...

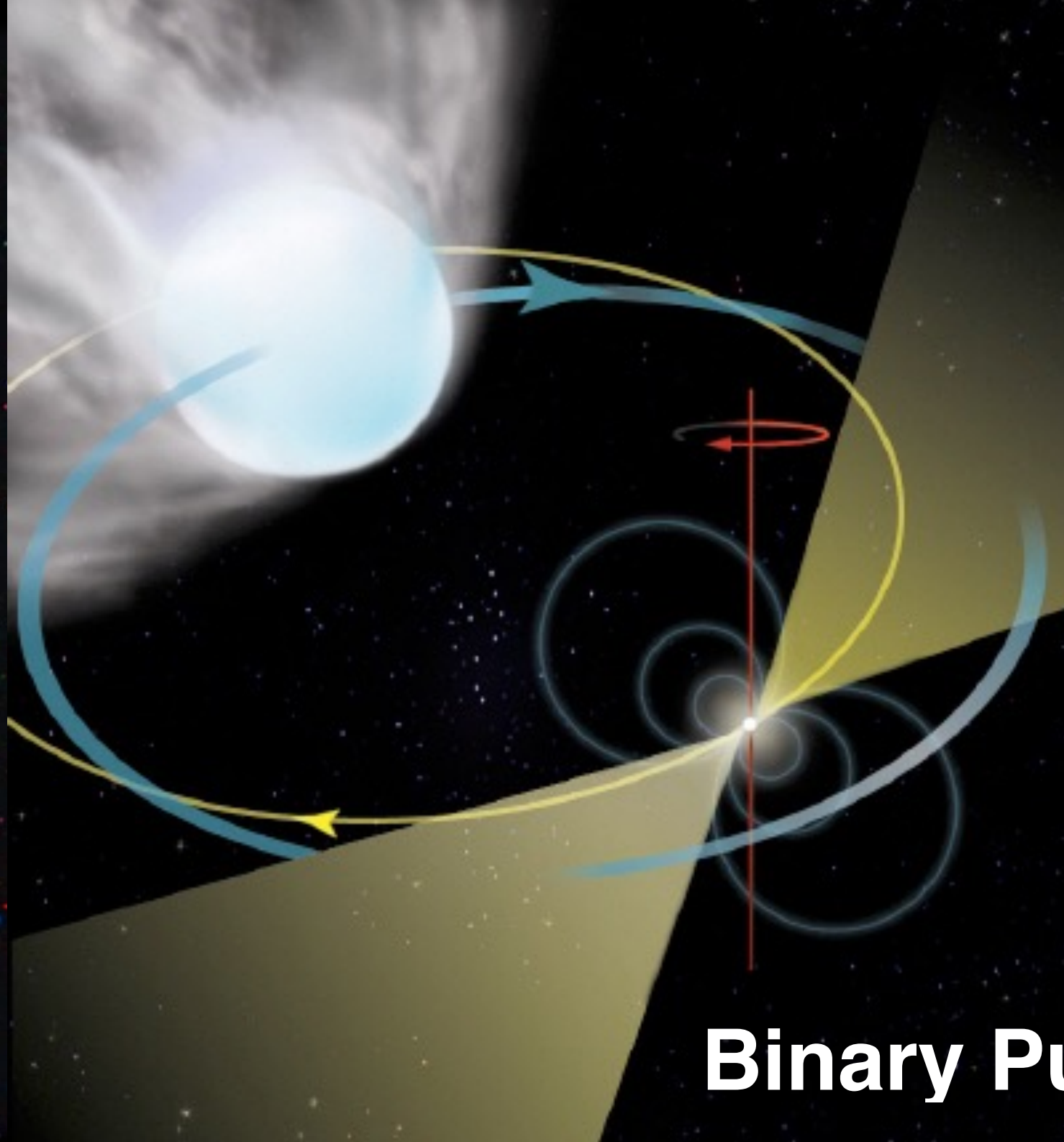
# Pulsar Timing

## “Phase connecting”

Results for PSR J1022+1001

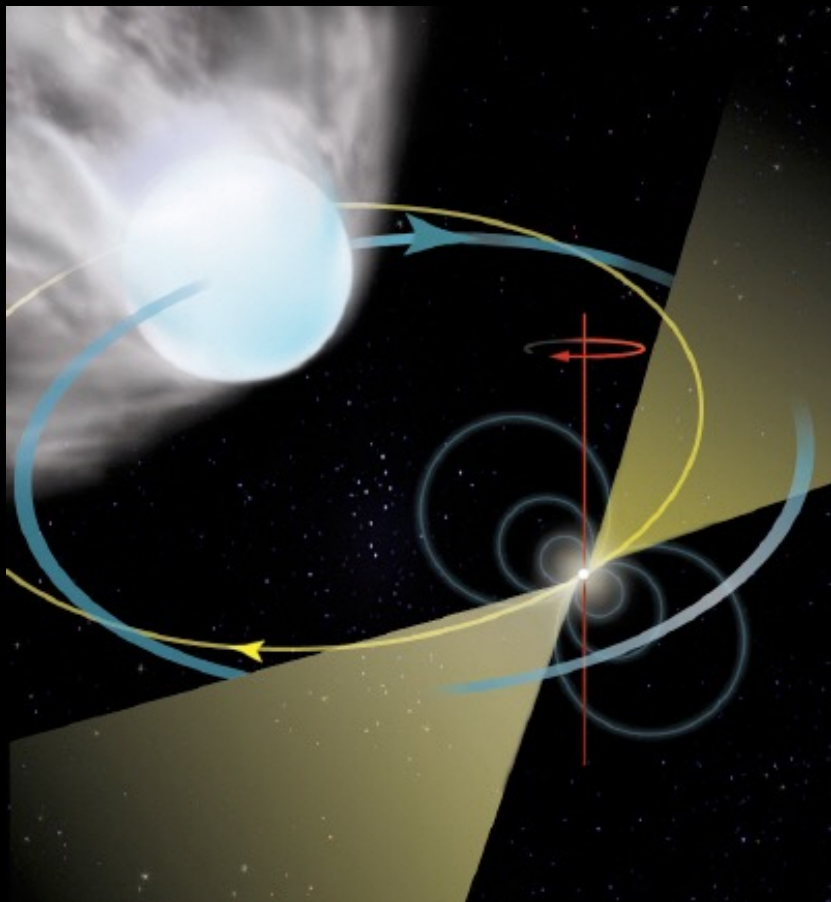
RMS pre-fit residual = 5.551 (us), RMS post-fit residual = 4.204 (us)  
 Fit Chisq = 328 Chisqr/nfree = 328.02/80 = 4.10028 pre/post = 1.32036  
 Number of points in fit = 90

PARAMETER	Pre-fit	Post-fit	Uncertainty	Difference	Fit
RAJ (rad)	2.71821351132165	2.71821366970554	4.5793e-07	1.5838e-07	Y
RAJ (hms)	10:22:58.1188834	10:22:58.1210613	0.006297	0.0021779	Y
DECJ (rad)	0.175100786106638	0.175101202092881	1.1575e-06	4.1599e-07	Y
DECJ (dms)	+10:01:57.12972	+10:01:57.21552	0.23875	0.085803	Y
F0 (Hz)	60.7794489670958	60.7794489674466	1.2099e-10	3.5076e-10	Y
F1 (s <sup>-2</sup> )	-1.69337759279488e-16	-1.70739820420136e-16	4.6312e-19	-1.4021e-18	Y
PEPOCH (MJD)	50250	50250	0	0	N
POSEPOCH (MJD)	50250	50250	0	0	N
DM (cm <sup>-3</sup> pc)	10.1340857485791	10.1323540071461	0.00032389	-0.0017317	Y
T0	50246.7162463696	50246.7162473185	8.2856e-07	9.4889e-07	Y
PB	7.80513016588816	7.80513016328438	2.1745e-09	-2.6038e-09	Y
A1	16.7654150843515	16.7654147901821	3.3958e-07	-2.9417e-07	Y
OM	97.67	97.67	0	0	N
ECC	9.73177041814313e-05	9.73614863096607e-05	4.0439e-08	4.3782e-08	Y
TRACK (MJD)	0	0	0	0	N



**Binary Pulsar**

# Pulsar Timing Orbital Parameters



## Keplerian Parameters

Projected semi-major axis ( $a \sin i$ )

Time of periastron ( $T_0$ )

Longitude of periastron ( $\omega$ )

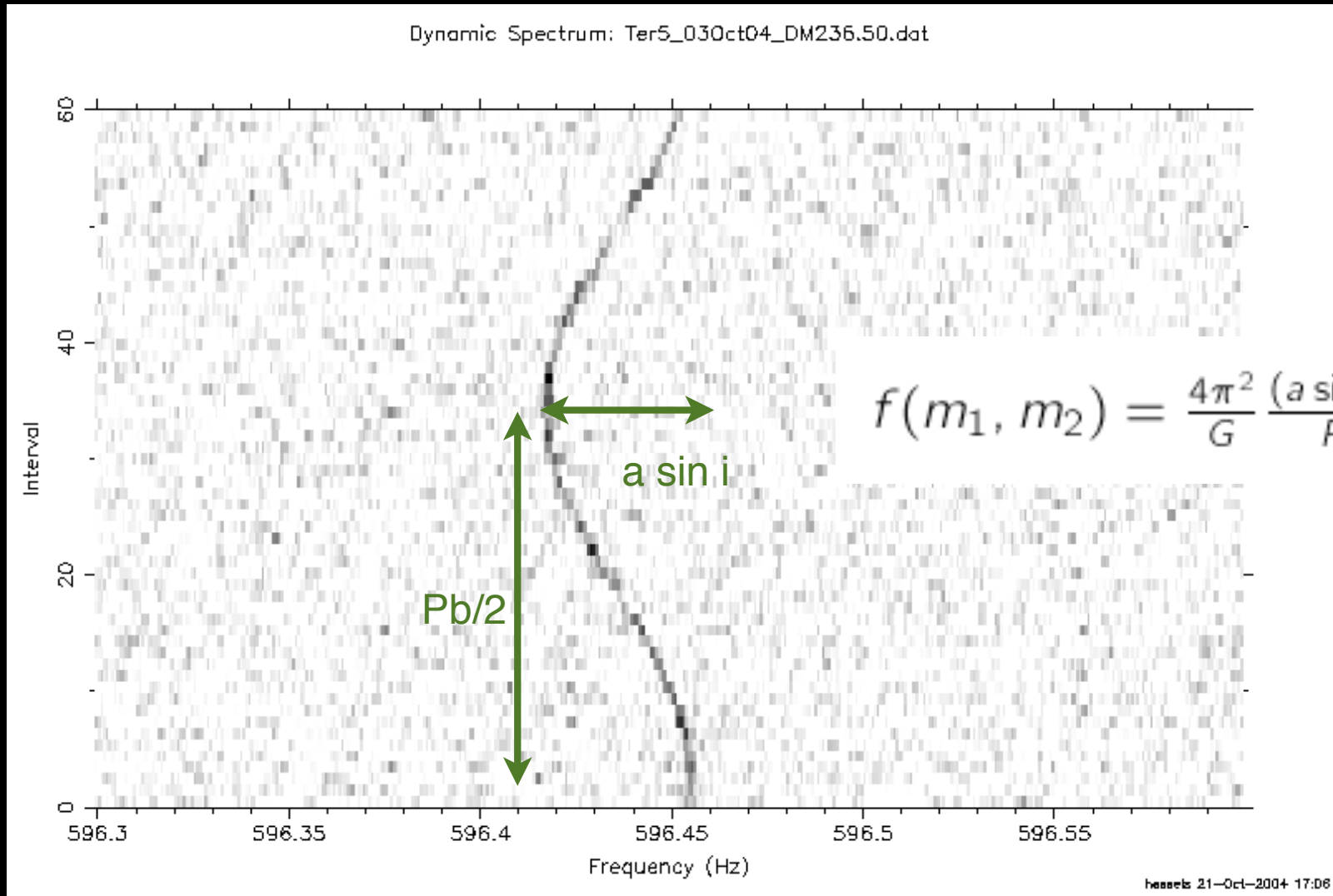
Orbital Period ( $P_b$ )

Eccentricity ( $e$ )

$$f(m_1, m_2) = \frac{4\pi^2}{G} \frac{(a \sin i)^3}{P_b^2} = \frac{(m_2 \sin i)^3}{(m_1 + m_2)^2}$$

Mass function  
(compare with single-line  
spectroscopic binary)

# Pulsar Timing Orbital Parameters



$$f(m_1, m_2) = \frac{4\pi^2}{G} \frac{(a \sin i)^3}{P_b^2} = \frac{(m_2 \sin i)^3}{(m_1 + m_2)^2}$$

Can est.  $m_2$ 's  
min. mass

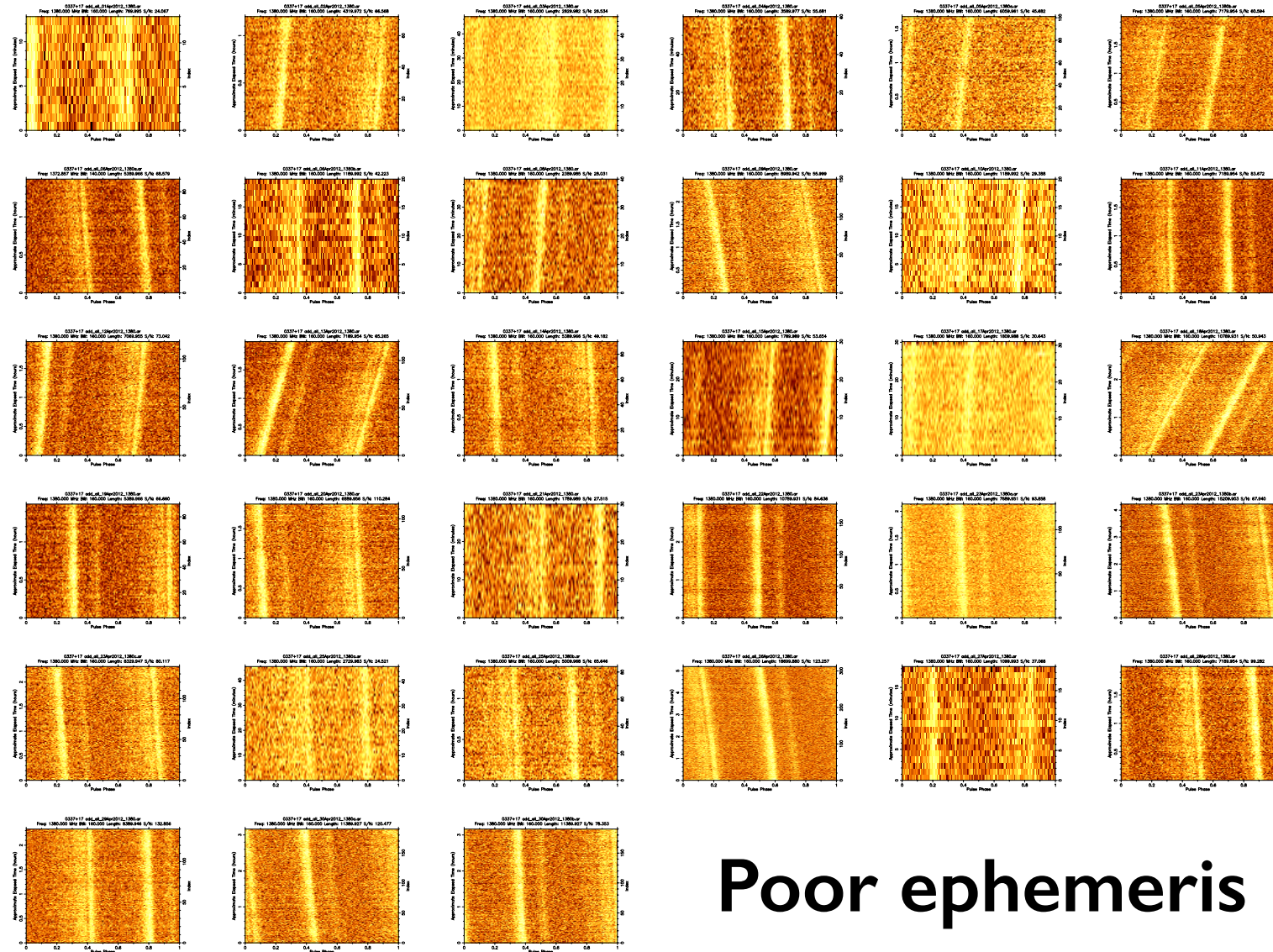
Need mass function + two other equations for  $m_1$ ,  $m_2$ , and  $i$



# Basics of Pulsar Timing

## Rotational Ephemeris

Time  
Phase

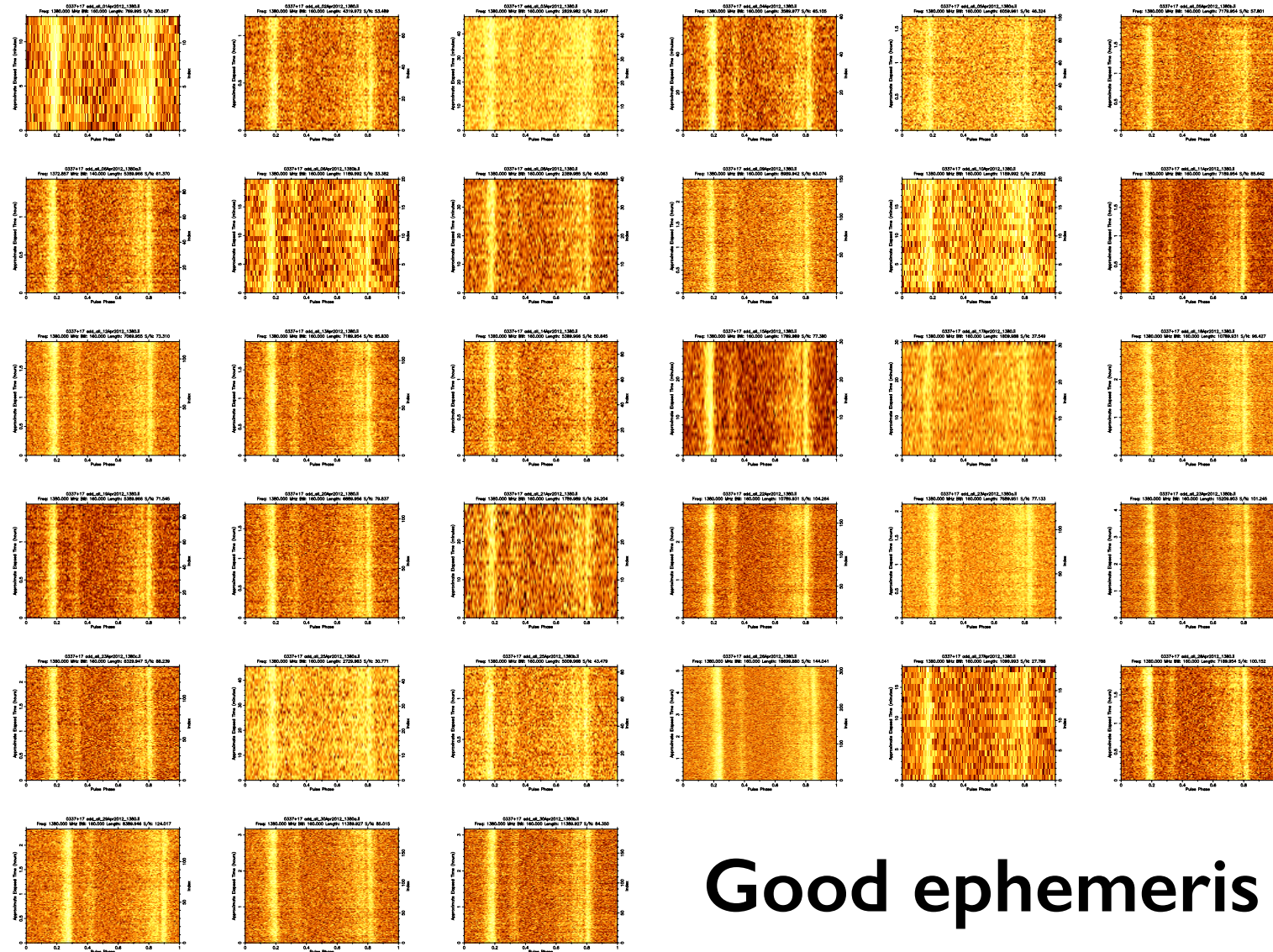


Poor ephemeris

# Basics of Pulsar Timing

## Rotational Ephemeris

Time  
Phase



Good ephemeris