

IONOSPHERIC EFFECTS

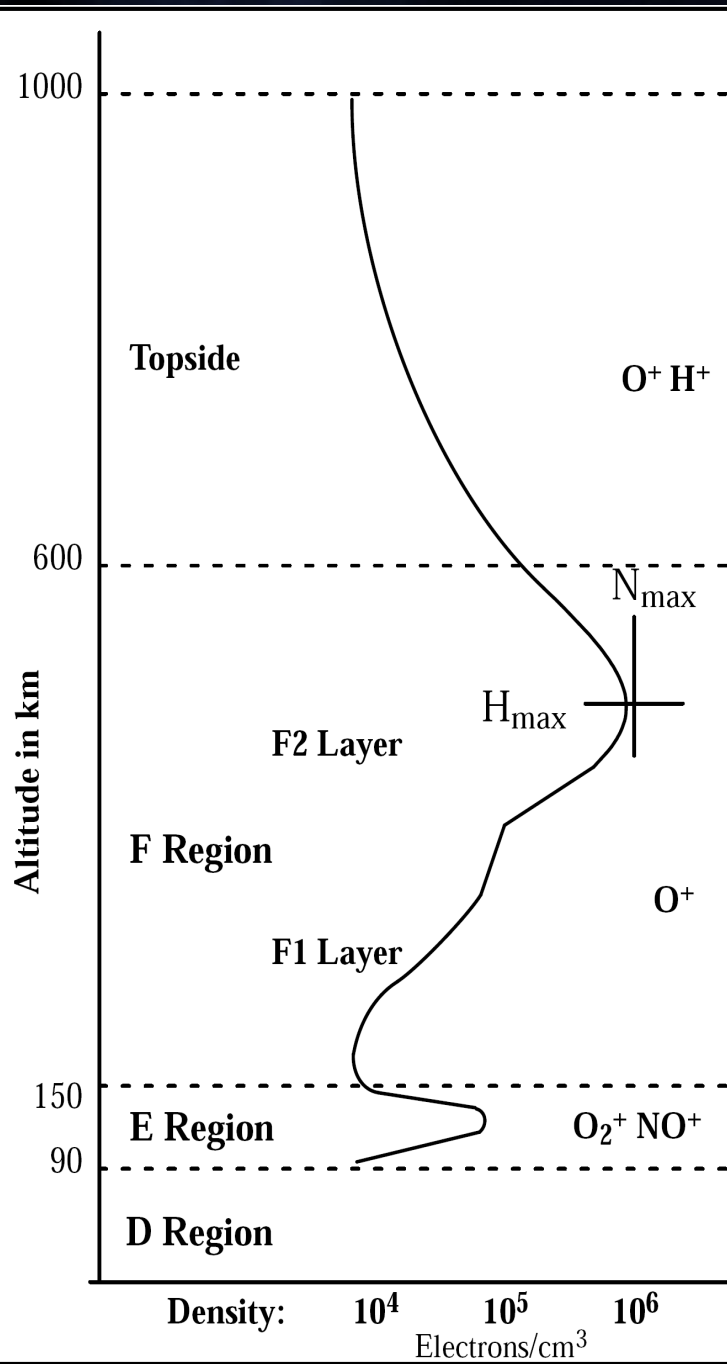
LOFAR data school 2014

M.Mevius

OUTLINE

- Introduction Ionosphere
- Electromagnetic propagation
 - dispersive delay
 - Faraday rotation
- Corrections
 - phase solutions
 - Direction Dependent Solutions
 - TECscreen
 - RM corrections
- Conclusion

Ionosphere



- Appleton 1924:
 - existence of reflecting layer (long wavelengths) in atmosphere (~125 km)
 - ionized
 - shorter wavelengths reflected @ 300-400 km
- ionospheric structure, density changes with altitude
 - height of layer changes during sunset/sunrise
 - ionization due to solar radiation

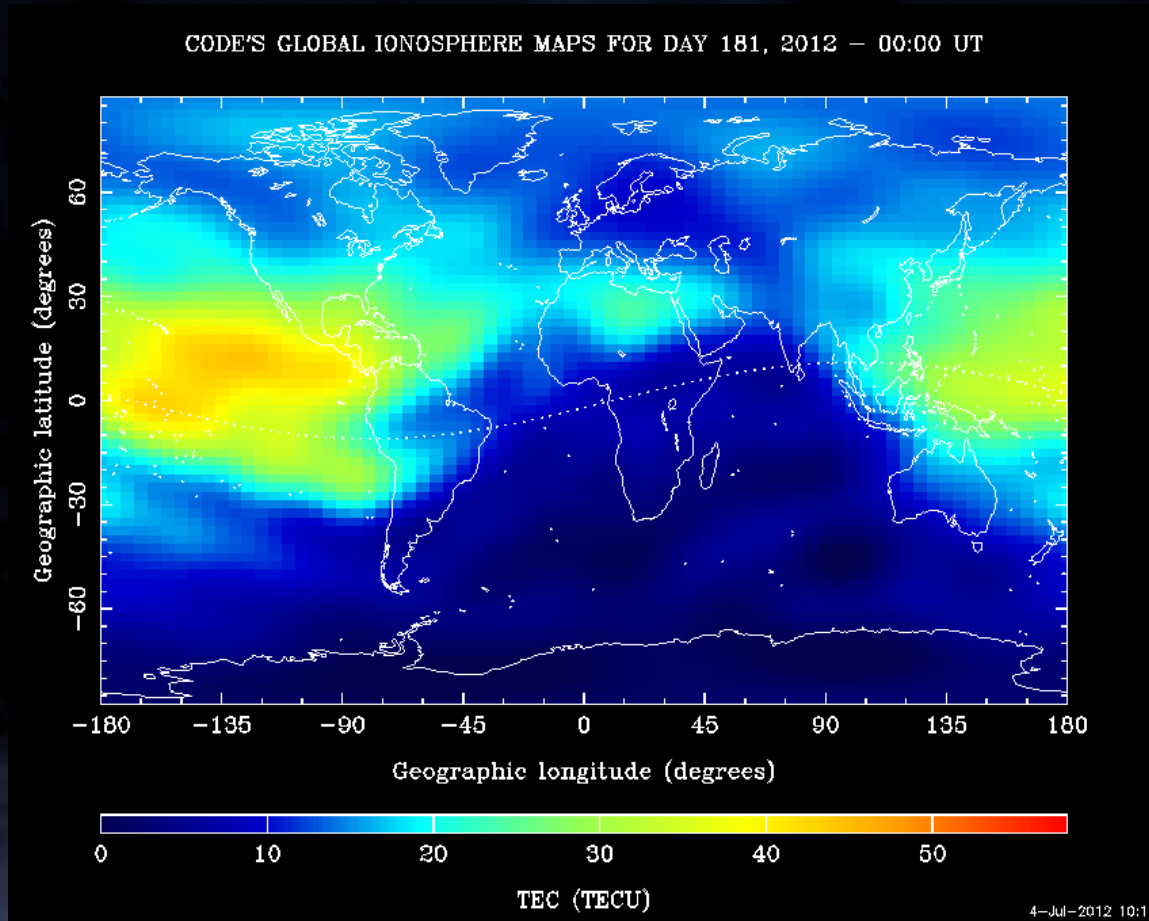
Measurements

- ionosonde: measure the structure of the different layers by investigating reflections of different wavelengths
- early radio astronomy
 - signals pass completely through
- nowadays: satellites +GPS receivers
 - GPS data online available
 - fit to GPS data of many stations also online: IONEX data
 - low time (1~2hr) and spatial (2.5 x2.5 degrees) resolution
 - thin layer approximation

CODE ionospheric data

Total Electron
Content (TEC)

Typical values @
52° for integrated
TEC along LOS:
5(night)- 50(day)
TECU (10^{16} e/m²)



Structure

The ionosphere is highly dynamic:

Ionization through solar radiation (UV+X-ray)

Recombination at night

=> diurnal pattern

Solar activity cycle

Scintillation (high turbulence):

(mostly) after sunset

Pressure + composition lower atmosphere

Travelling Ionospheric Disturbances (TIDs)

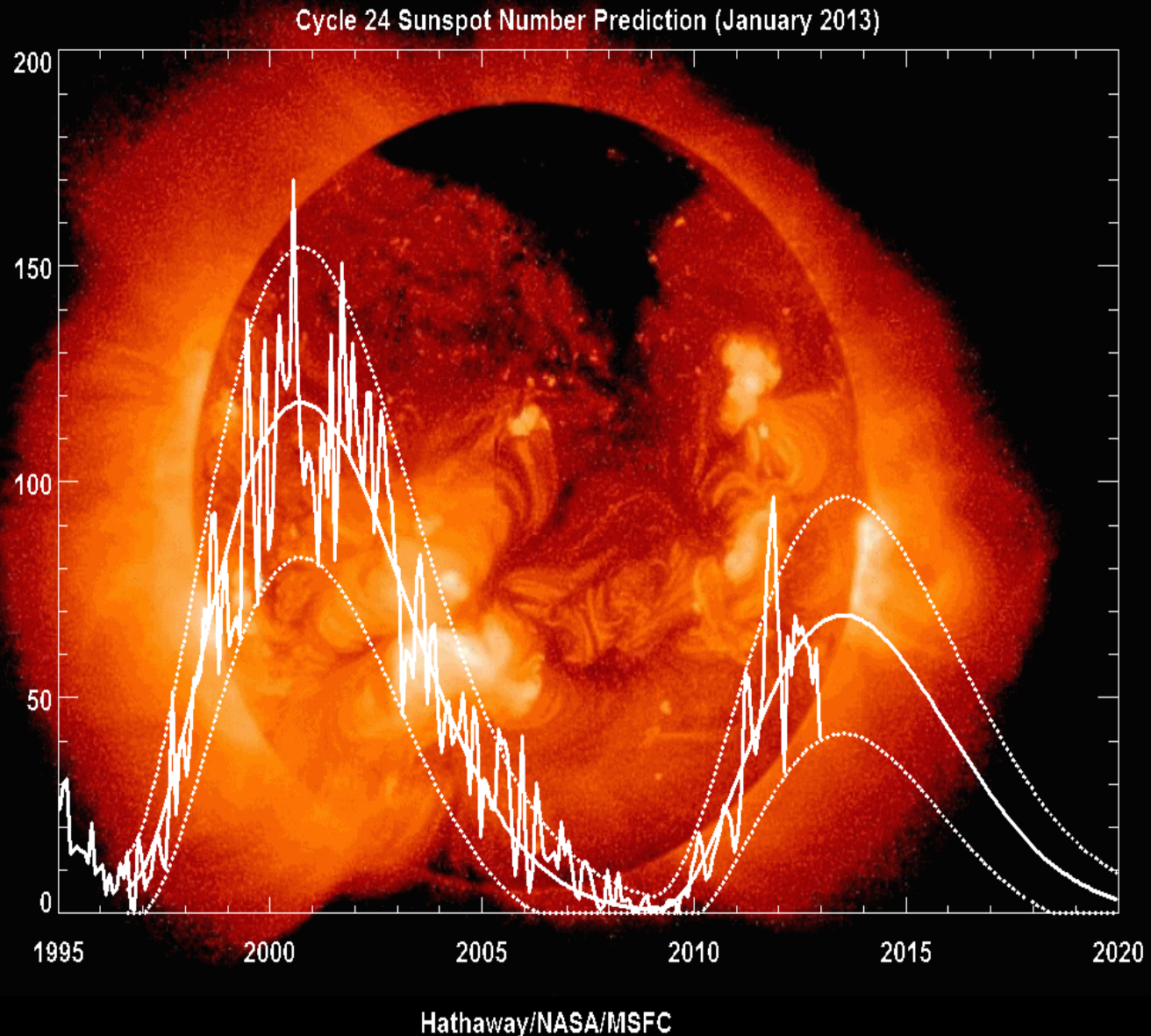
Structure: Kolmogorov turbulence

Structure

Solar activity follows a 12 year cycle:

Currently we are in a maximum

the current maximum appears to be much lower than in previous cycles.



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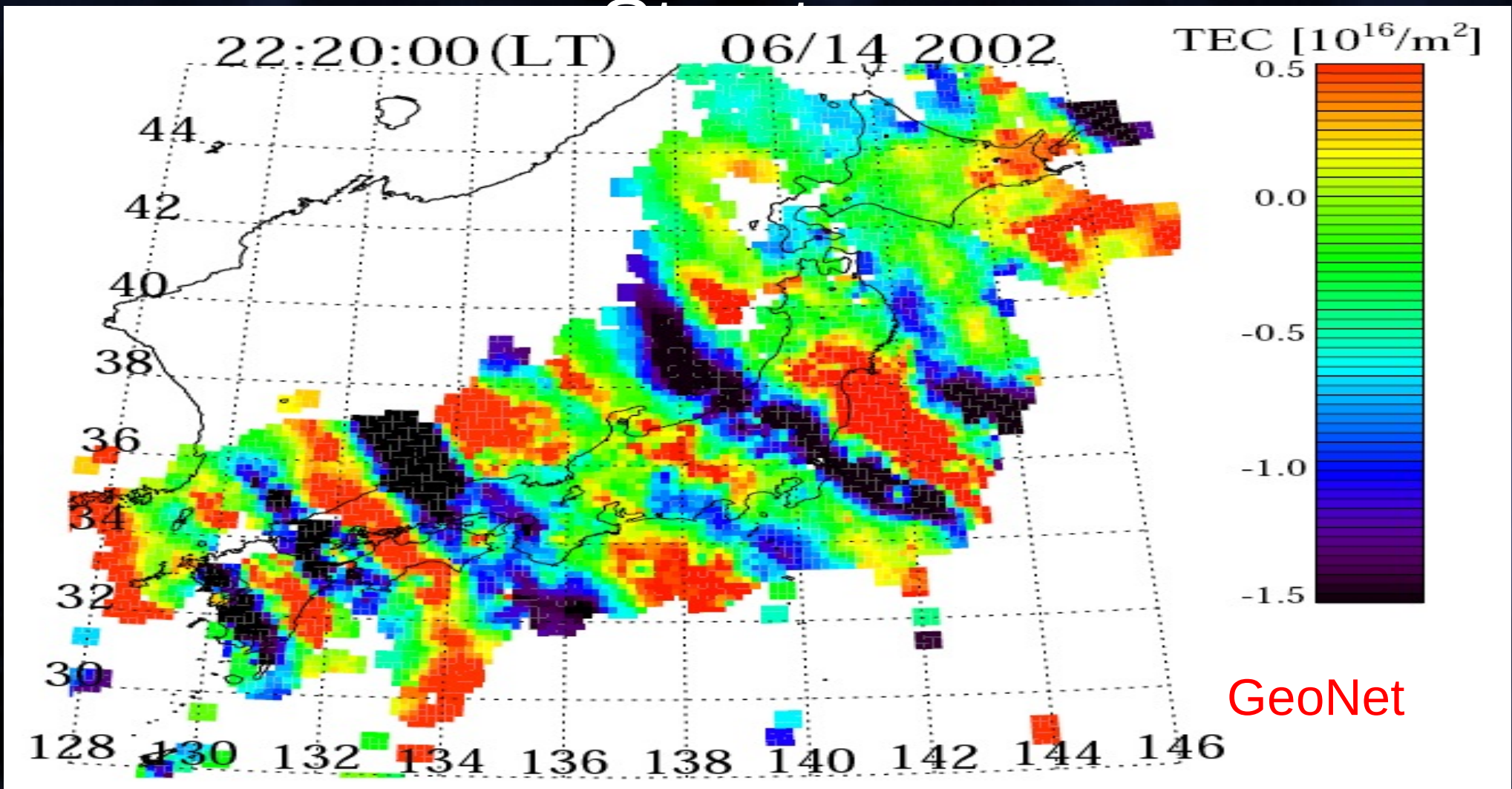
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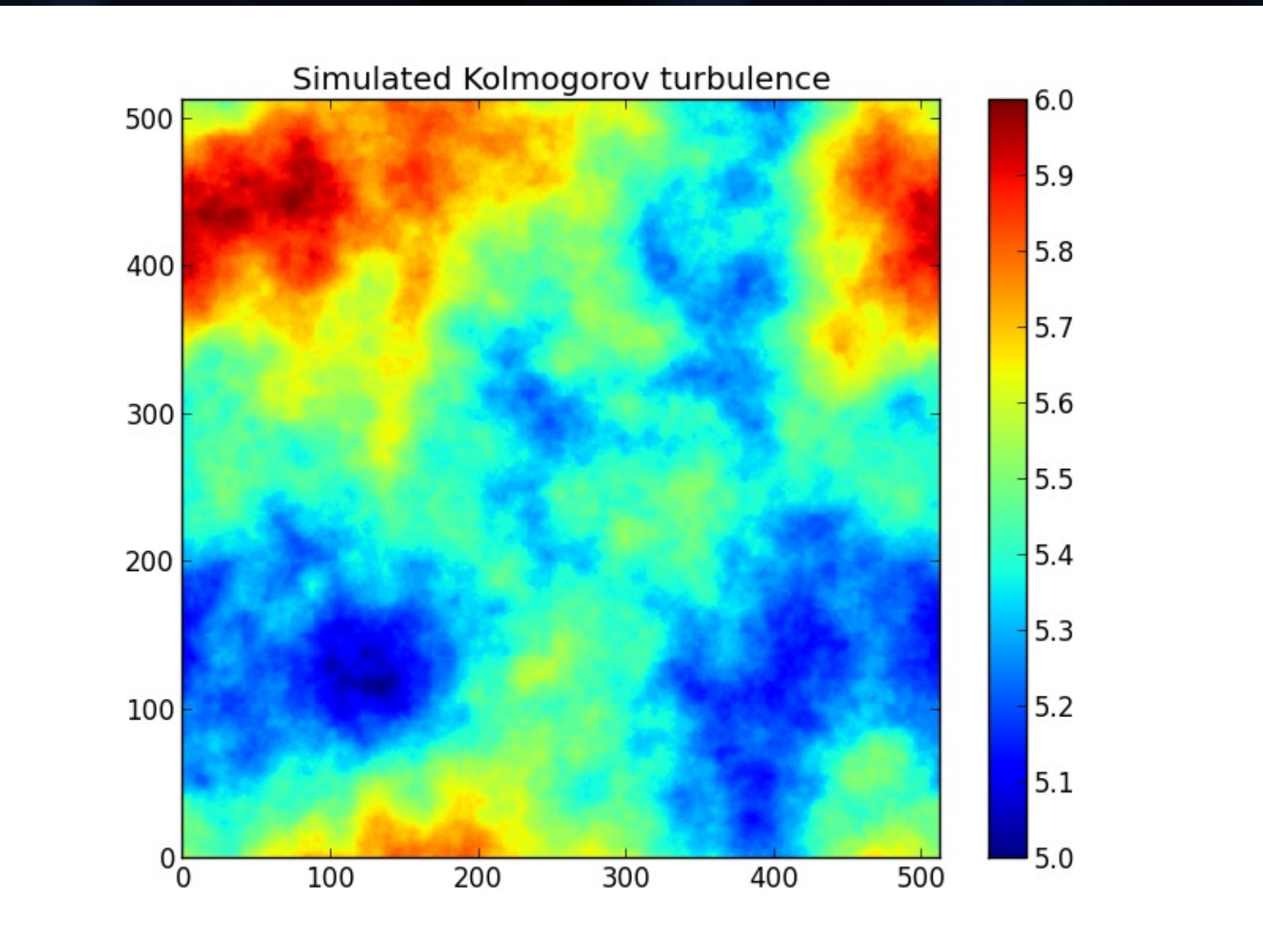
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Travelling Ionospheric Disturbances (TIDs)

Structure: Kolmogorov turbulence

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Travelling Ionospheric Disturbances (TIDs)

Structure: Kolmogorov turbulence

Electromagnetic Propagation

refractive index in ionized plasma:

$$n_{ph} = \sqrt{1 - \left(\frac{f_p}{f}\right)^2} \approx 1 - \frac{1}{2} \left(\frac{f_p}{f}\right)^2 = 1 - \frac{40.3}{f^2} N_e$$

if frequency f (ν) \gg plasma frequency f_p (~ 10 MHz)

N_e = electron density

excess path length

$$40.3/\nu^2 \cdot \int N_e dl$$

phase error: $\varphi_{ion} \approx 8.45e9$ dTEC/ ν

dTEC in TECU (10^{16} e/m²)

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dispersive

Faraday Rotation

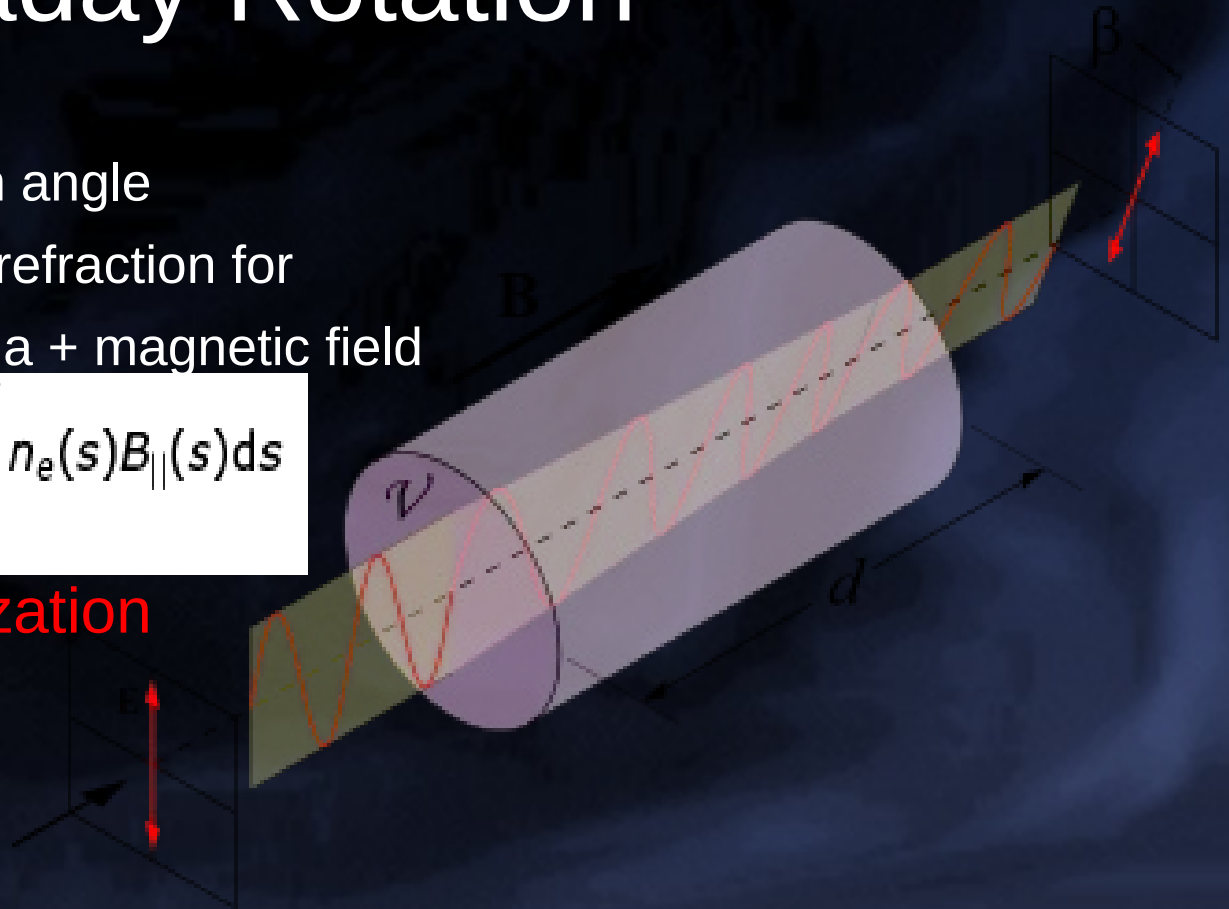
Rotation of linear polarization angle

Due to difference in index of refraction for

R and L polarization in plasma + magnetic field

$$\beta = RM\nu^{-2}, \quad RM = \frac{e^3}{8\pi^2\epsilon_0 m^2 c^3} \int_0^d n_e(s) B_{||}(s) ds$$

see presentation on polarization
(Thursday, M. Brentjens)



Typical Rotation Measure:

0.5 rad/m² for ~10 TECU

Depending on viewing direction (parallel B-field)

Absolute TEC can be determined from polarized source (with known intrinsic RM) and Earth Magnetic Field

Differential Faraday Rotation also significant effect on longer baselines (>10 km)

Effects on radio propagation

- Dispersive delays
 - Direction dependent/frequency dependent effect on differential phases
 - Sensitive to differential TEC
- Faraday Rotation
 - Rotation of polarization angle of polarized signal
 - Sensitive to absolute TEC
 - Differential Faraday Rotation:
 - Sensitive to relative TEC and (relative) B-field
- Differential refraction (second order)
 - Displacement of relative source positions due to refraction
 - absolute TEC

Dispersive delays @ LOFAR

phase error: $\varphi_{\text{ion}} \approx 8.45 \cdot 10^9 \text{ dTEC}/\nu$

typical variation LOFAR (NL) 80 km: 0.5- 1TECU

within a single HBA beam: ~ 0.1 TECU

110-180 MHz (HBA): 1 full 2π rotation @ 0.2 TECU

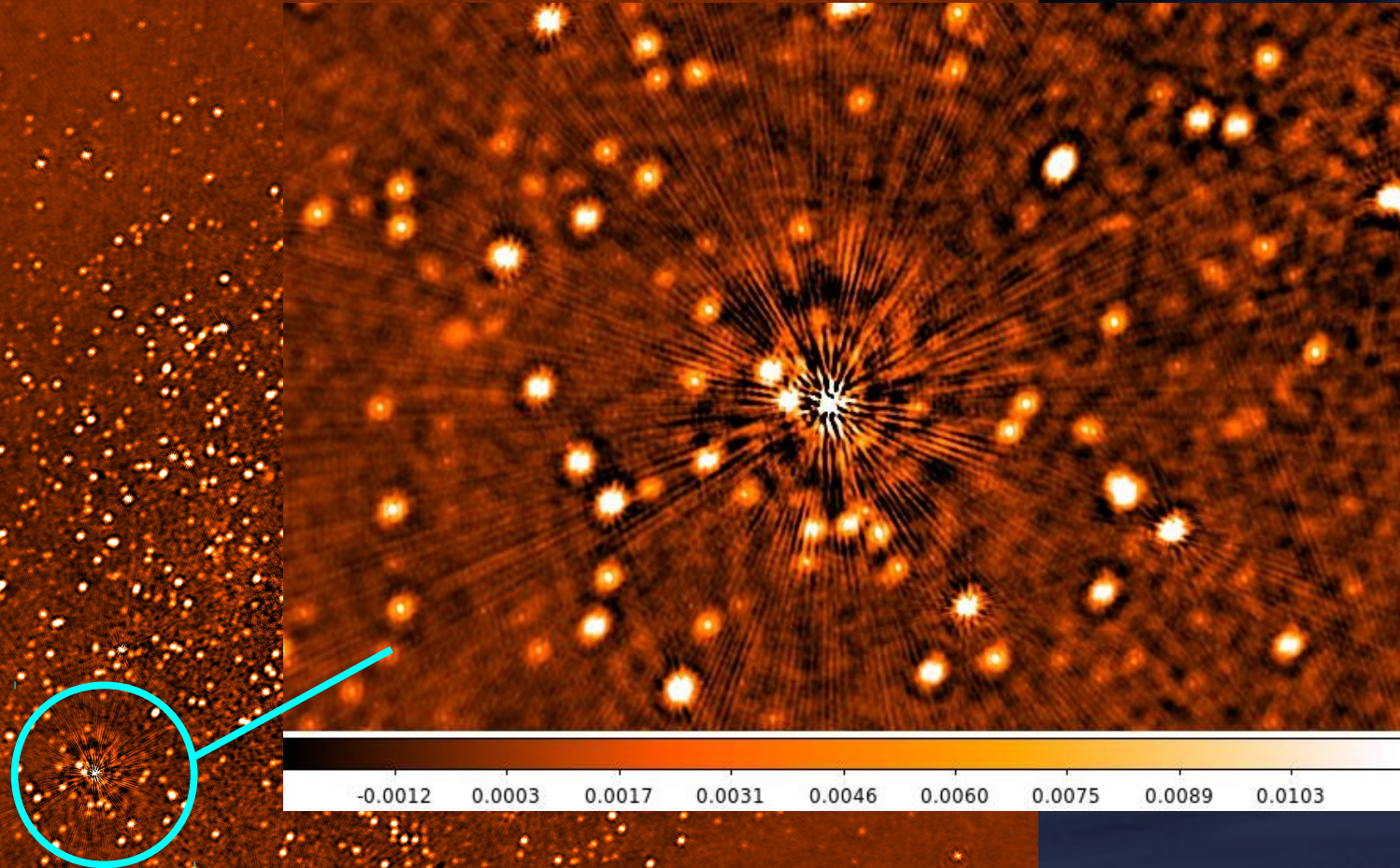
30-80 MHz (LBA): 1 full 2π rotation @ 0.035 TECU

time variability of ionosphere:

- mTIDs ~ 15 min
- moving turbulence: smaller amplitude, but much faster variations

high time and frequency resolution needed for phase solutions

image: V. Pandey



ionospheric effects in images:
phase errors result in shifted
positions (time varying) or
distorted sources

Dispersive Delay Correction

selfcal phases contain different phase effects

@ LOFAR 2 dominant sources:

- drifting clock errors
- ionospheric phases

use frequency dependence + wide frequency range for clock/TEC separation on phase solutions:

- calibrator: apply clocks only (since ionosphere is different in target field)
- use ionospheric phases to generate phasescreen for interpolation (direction dependent correction)
- inspect ionospheric conditions of observation

Clock/TEC separation

Start from selfcal phases over wide frequency range.

Fit for A(clock) and B(TEC) in:

$$\Delta\phi(\nu) = A \cdot 2\pi\nu + B \cdot 8.4479745 \cdot 10^9 / \nu$$

Complication 2π ambiguities:

if ϕ is a solution so is $\phi + 2\pi$

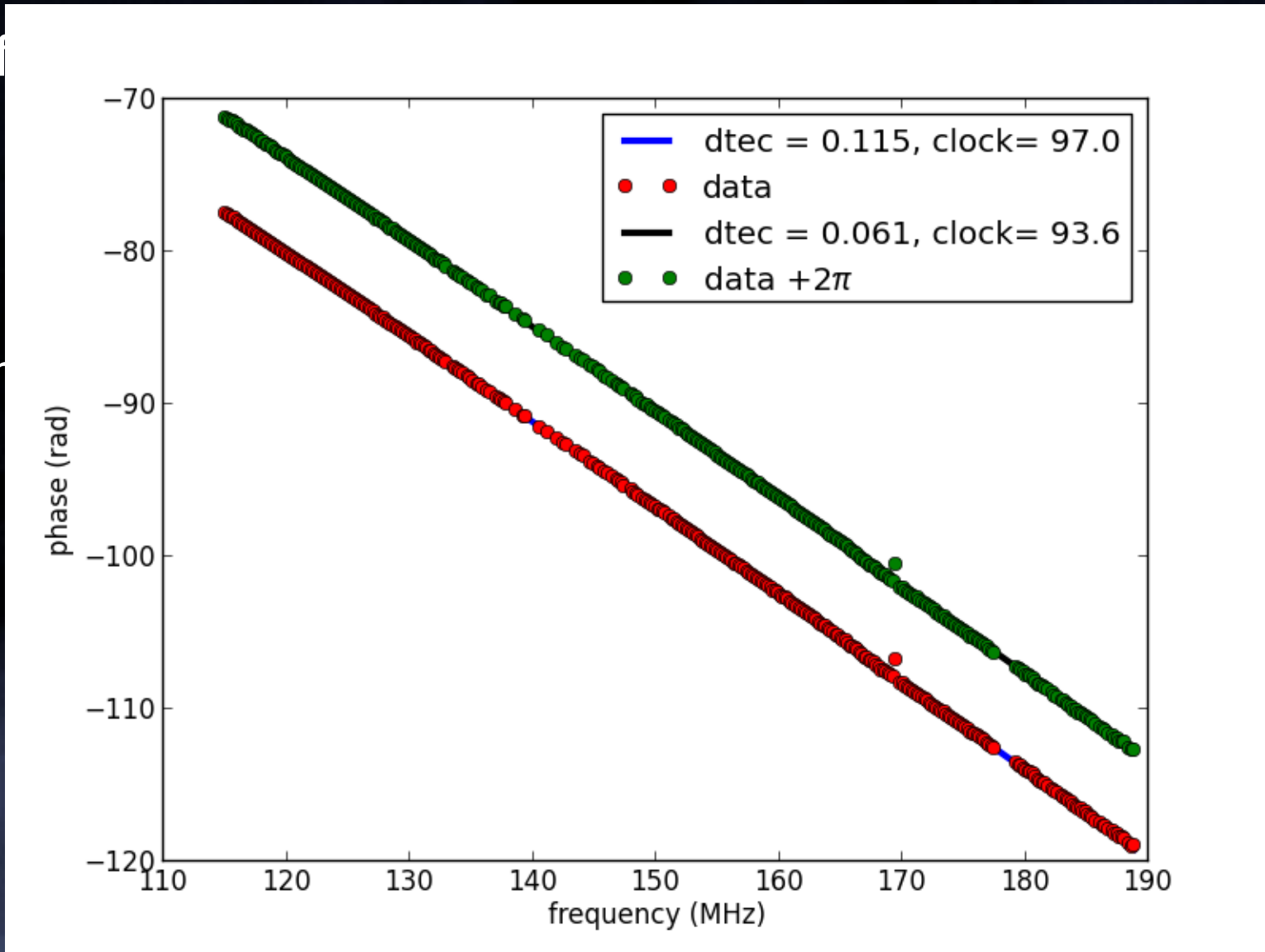
corresponds to fixed offset in clock and TEC

Clock/TEC separation

Start from selfcal phases over wide frequency range.

Fit f

Cor

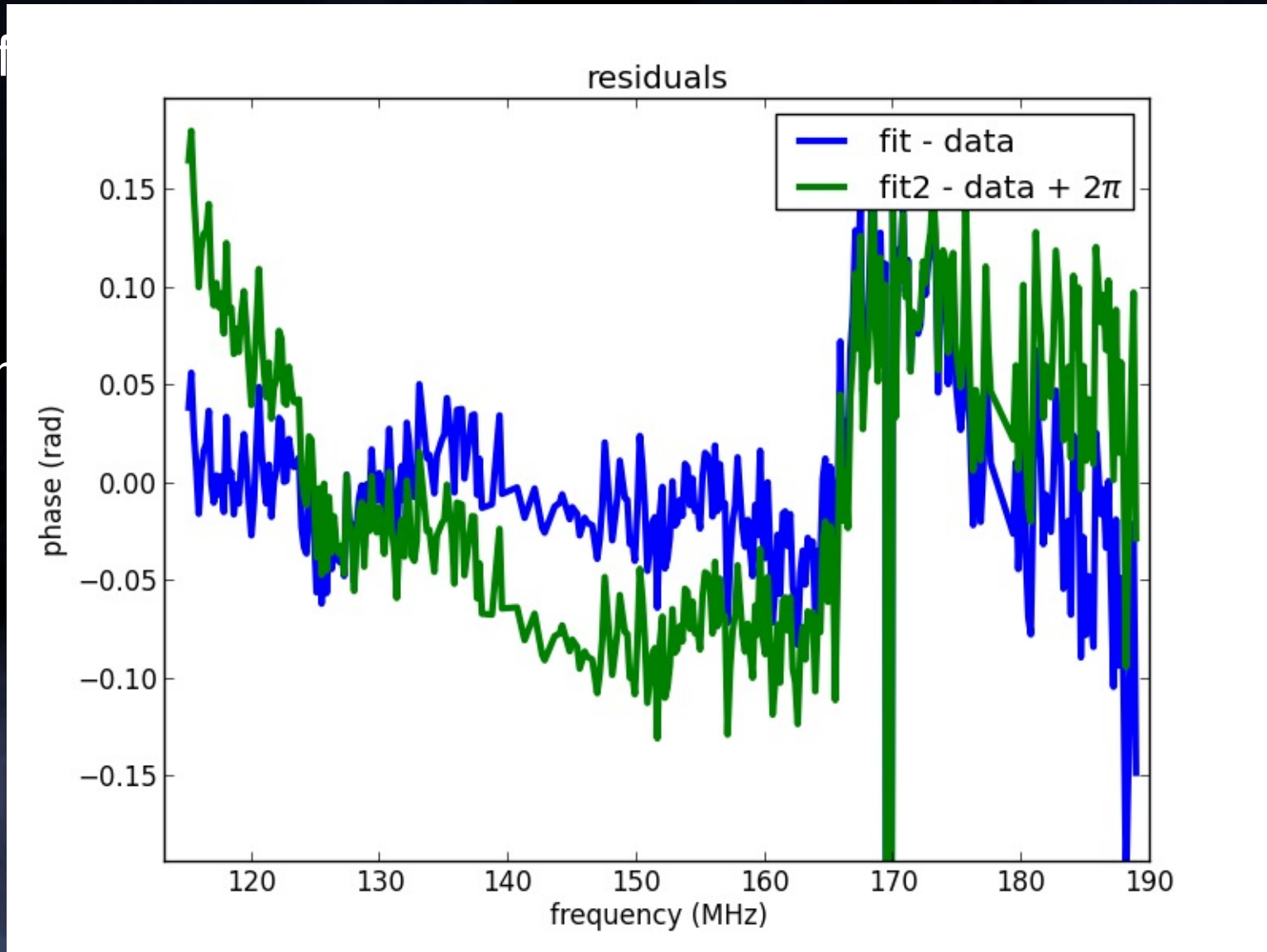


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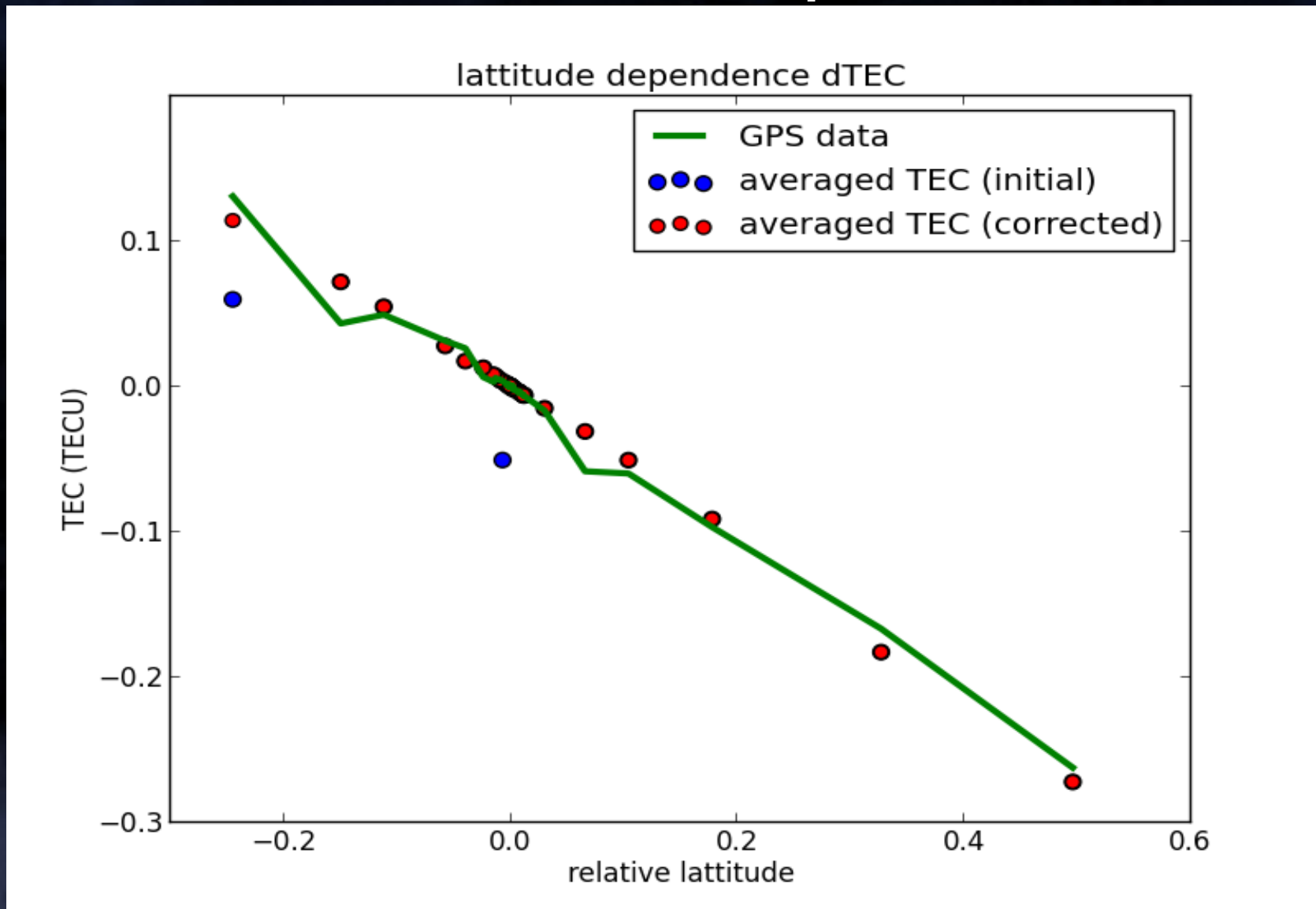
corresponds to fixed offset in clock and TEC

Slow variation of clock/TEC solutions in time:

start with good solution for first timeslot, initialize subsequent with previous solutions

Correct remaining wraps by inspecting residuals/spatial correlation

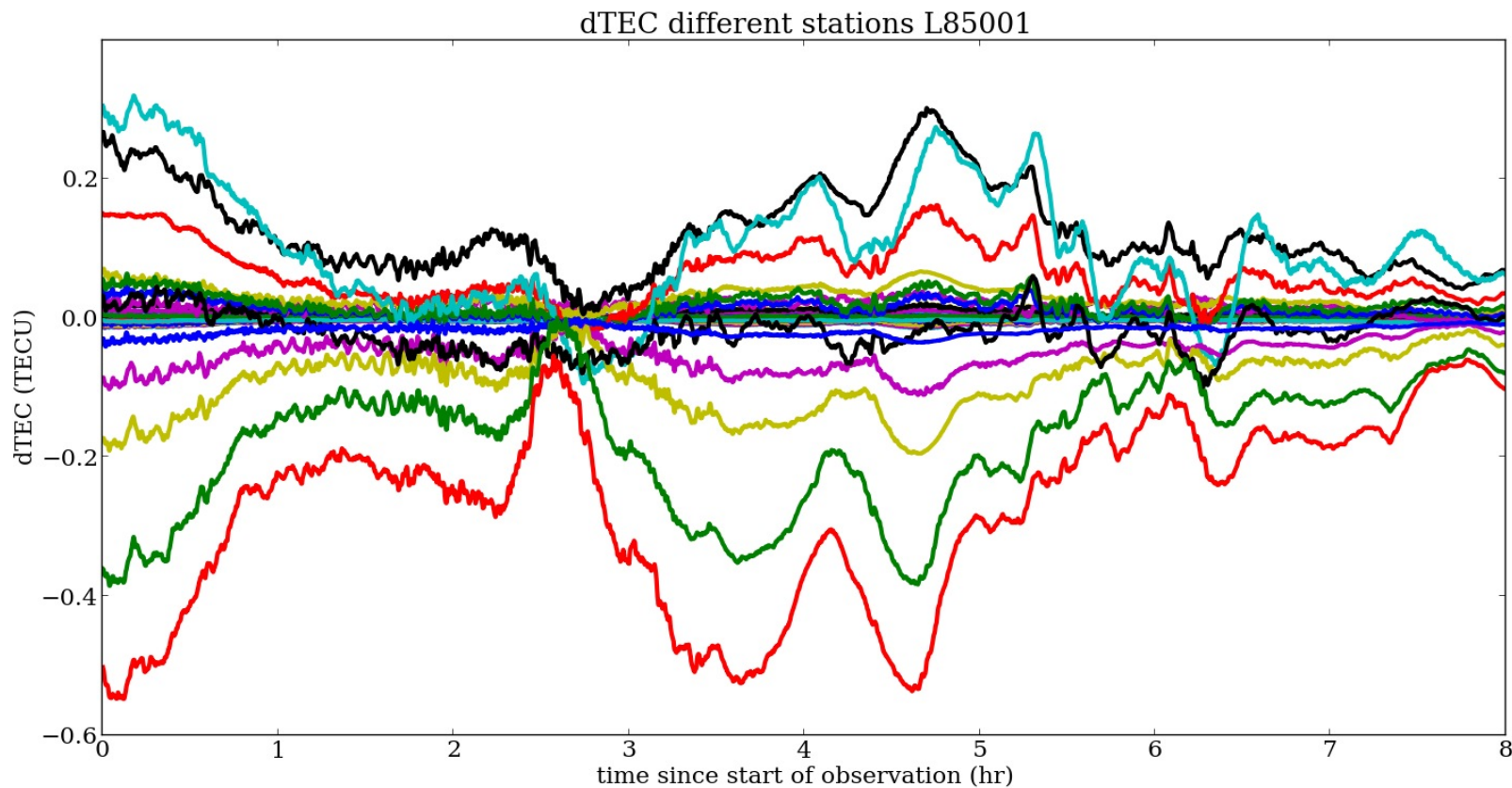
Clock/TEC separation



Correct remaining wraps by inspecting residuals/spatial correlation

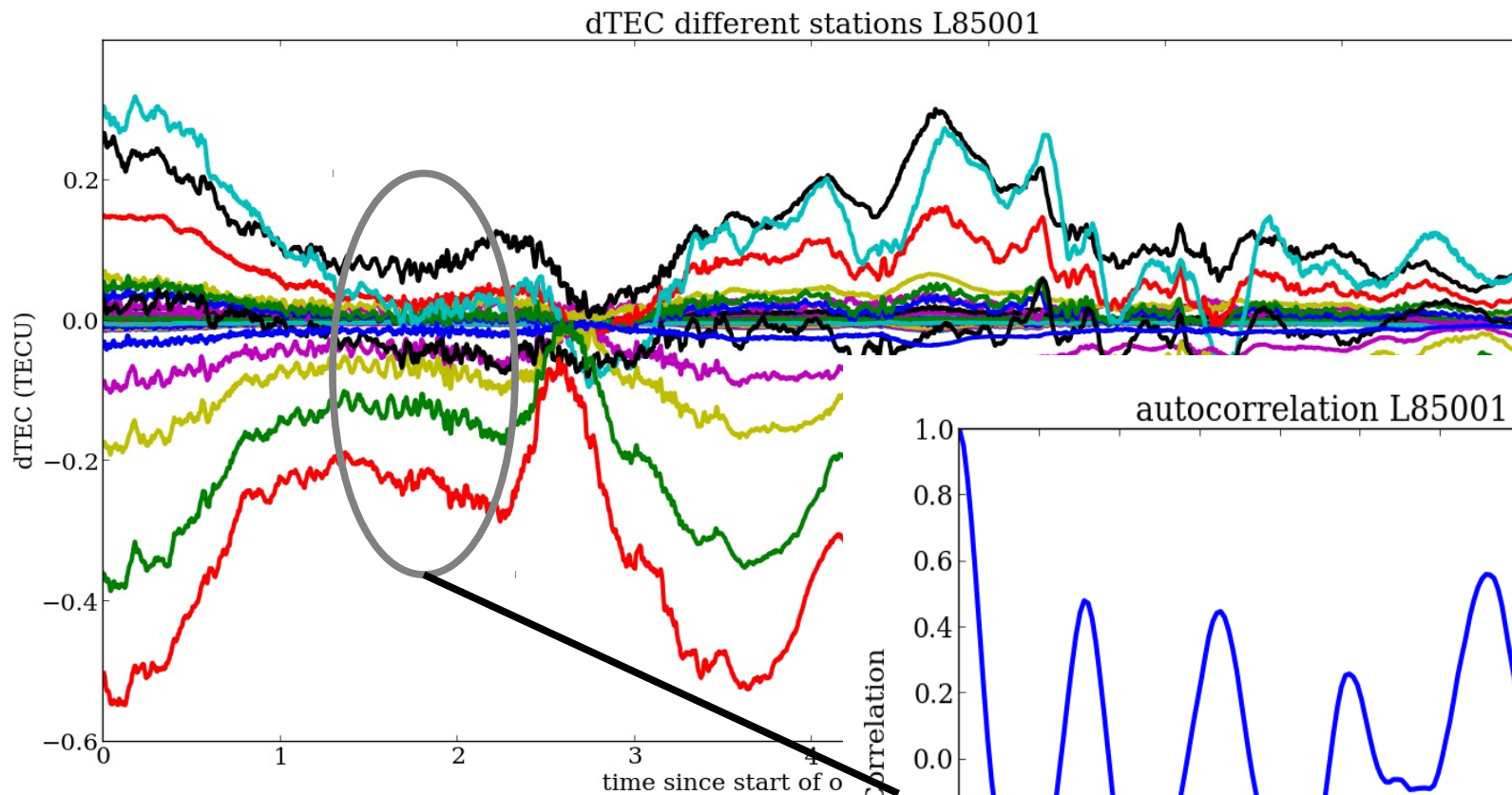
TEC solutions

dTEC solutions versus time, HBA all stations



TEC solutions

dTEC solutions versus time, HBA all stations



timescale ~5 min

Structure function

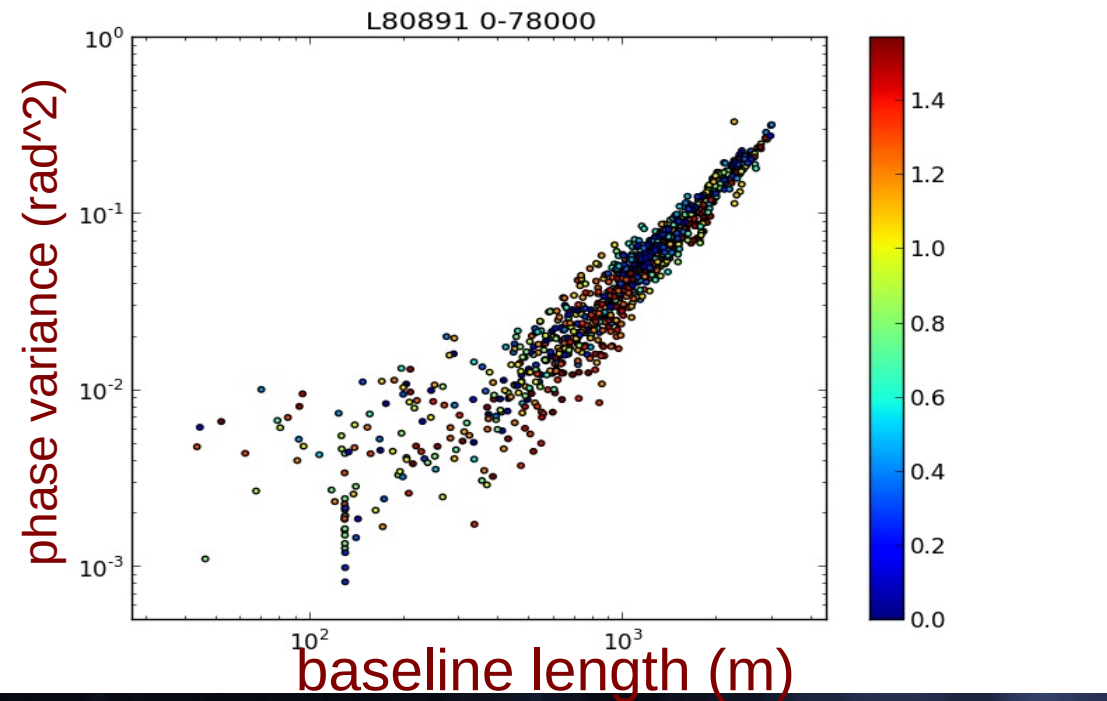
Spatial fluctuations:

$$D_{\phi}(\|r_1 - r_2\|) = \langle (\phi_1 - \phi_2)^2 \rangle$$

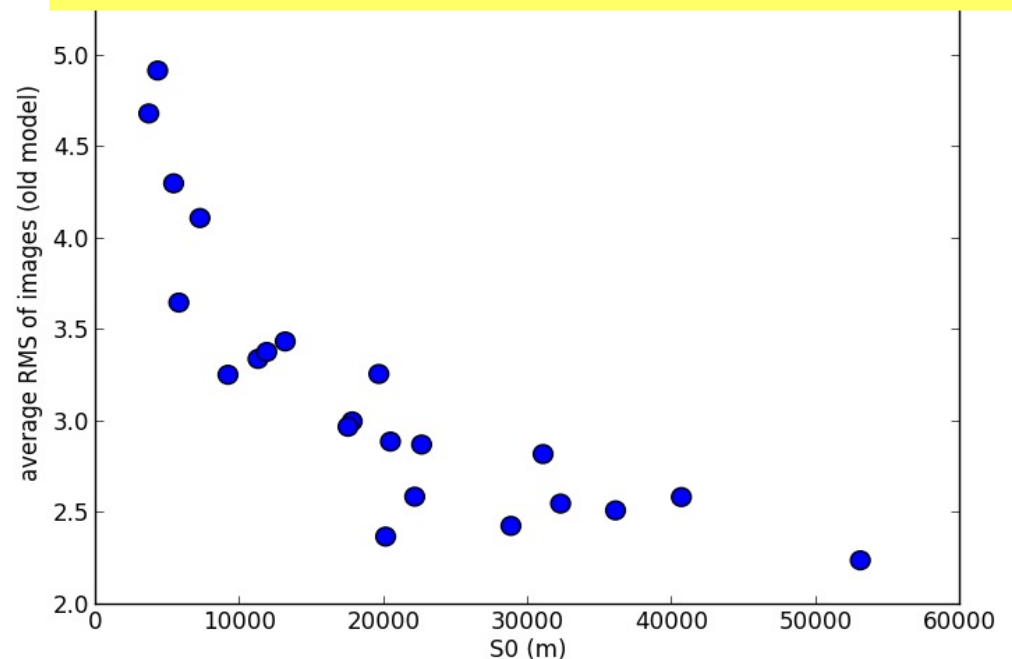
Kolmogorov turbulence,
thin layer approximation:

- $D_{\phi}(\mathbf{r}) = (\mathbf{r} / s_0)^{\beta}$
- $\beta = 5/3,$
- s_0 : field coherence scale, $D_{\phi}(s_0) = 1 \text{ rad}^2$

Typical nighttime S_0 values
@150 MHz: 2-40 km
scintillation conditions $S_0 < 2\text{km}$

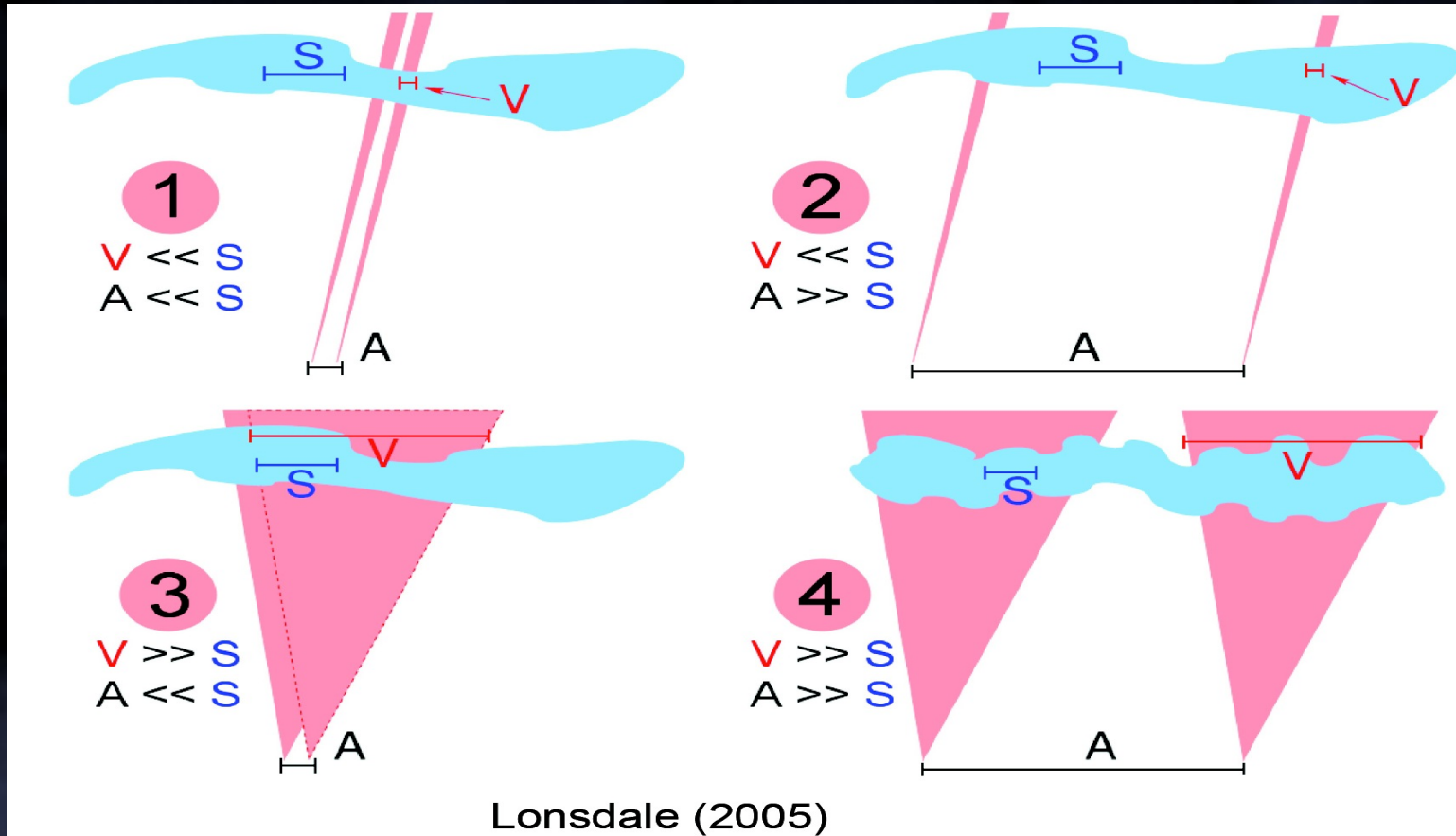


Correlation image noise S_0



Lonsdale regimes

clock/TEC separation: direction independent phases
spatial structure ionosphere:



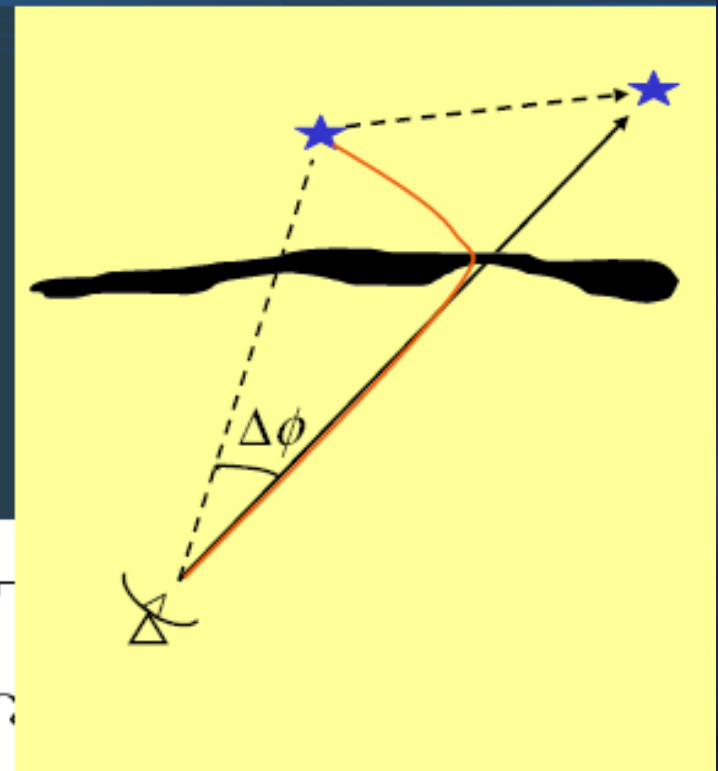
standard selfcal works only in regime 1 or 2

LOFAR: direction dependent effect

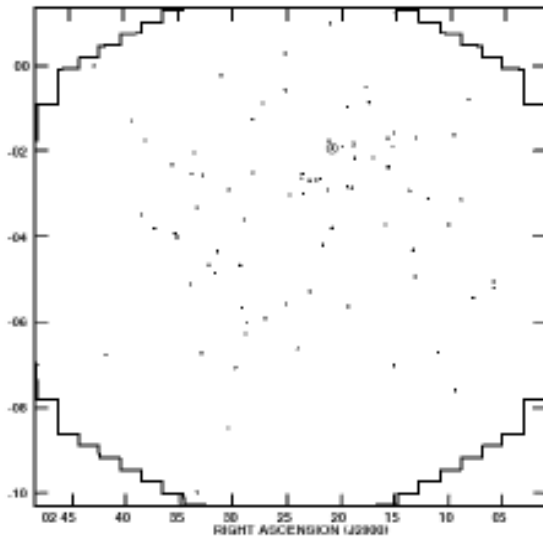
Direction dependent correction methods

- Field based calibration *B. Cotton et. Al (2004)*
 - works for linear gradients, higher order effects distort the source

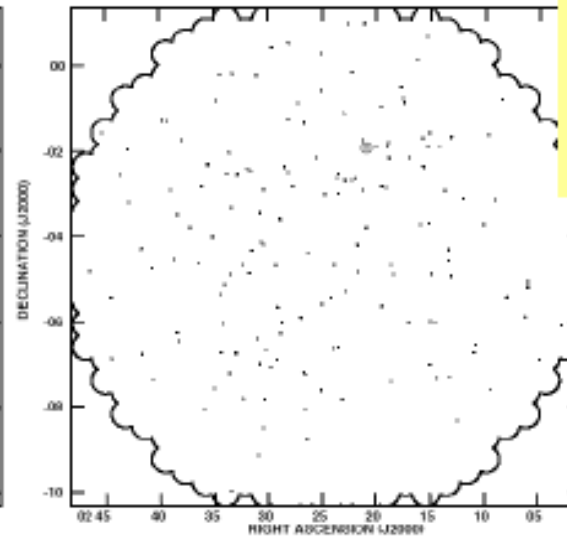
Determine phase offsets from position shifts
Fit Zernike polynomials
Correct the data per facet for imaging
1st order effects only



Self-Calibration



Field-Based Calibration



Direction dependent correction methods

Methods that involve direction dependent calibration

(separate gain/phase solutions in direction of several sources/clusters)

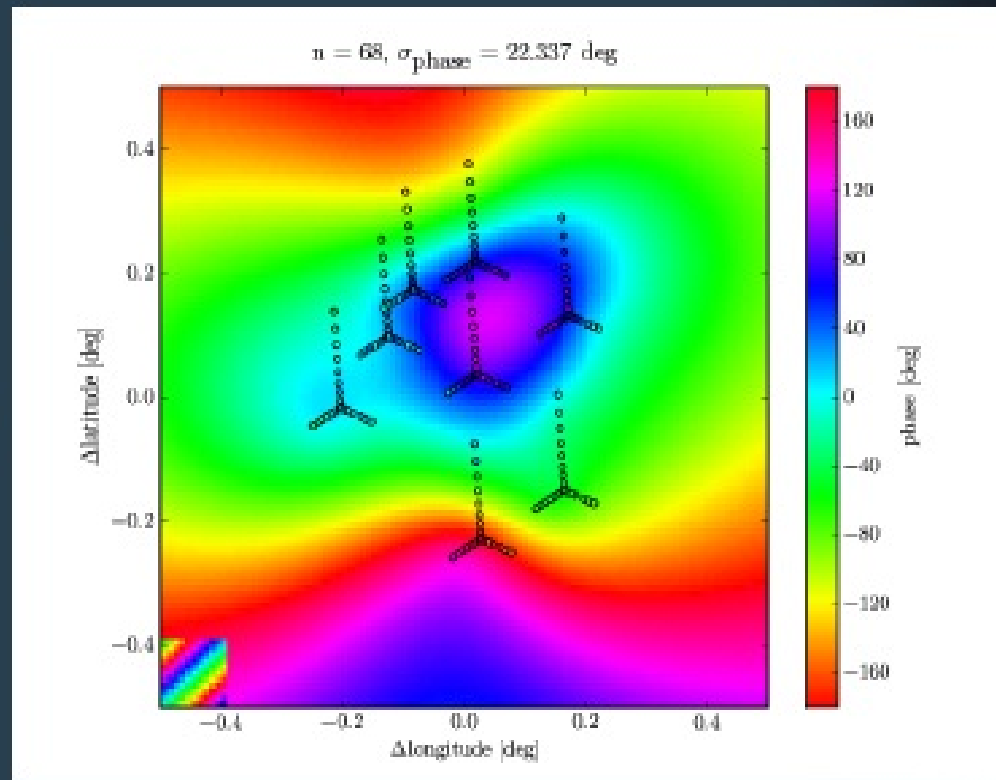
- Multi direction solve + subtract sources with their own solutions (eg. Sagecal):
 - No correction for residuals
- Phasescreen methods:
 - every station-direction pair corresponds to a *piercepoint* on 1 (or more) thin layers
 - fit 2D function on piercepoint solutions and interpolate to get phases in unknown directions
 - apply solutions:
 - facet imaging
 - subtract sky model with interpolated phase correction
 - A projection: apply screen during imaging step

See Wide Field imaging (S. vd. Tol, Wednesday)

Phasescreen examples: SPAM

Source Peeling & Atmospheric Modeling

Get $\varphi_{obs}(t)$ from peeling of calibrators
Fit model on KL basis
Correct each facet with model phase
Make image
Not limited to gradients only

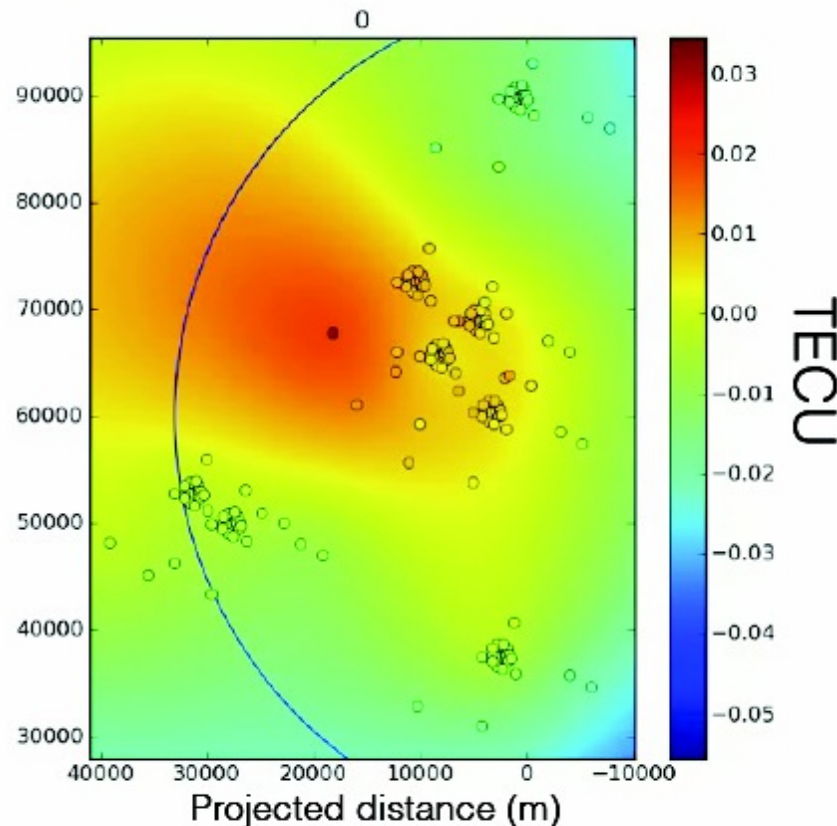


SPAM + facet imaging *Intema et Al (2009)*

© Huib Intema

Phasescreen examples: MSSS (LBA)

- TEC value was derived for each pierce point every 10 seconds using fit to phases across all 8 bands
- Core stations + 5 remote stations were used
- 7 11-minute snapshots were used (first two snapshots not used due to poor solutions)
- AWimager used to image + apply screen

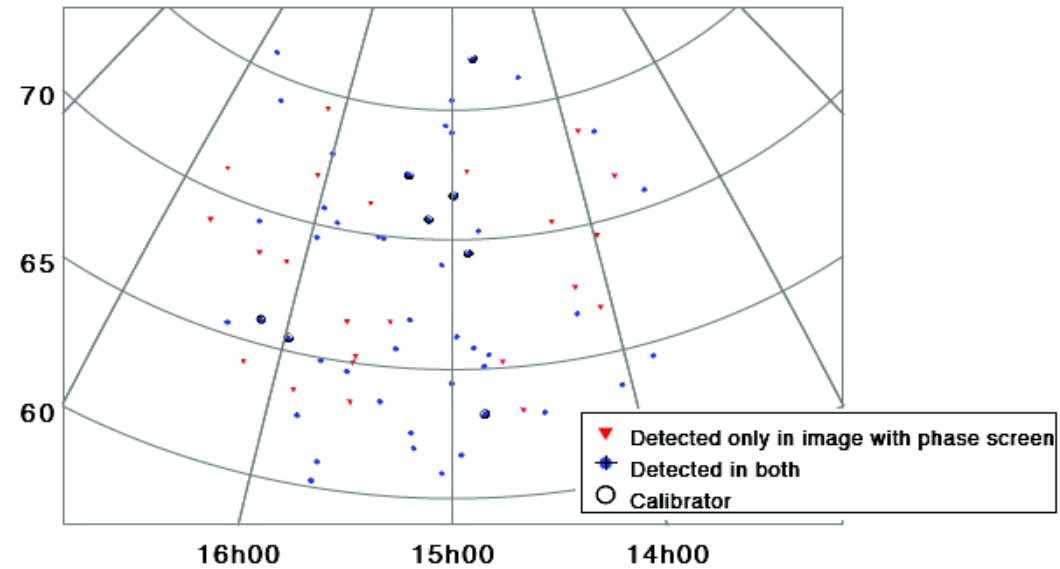


D. Rafferty + S. vd. Tol

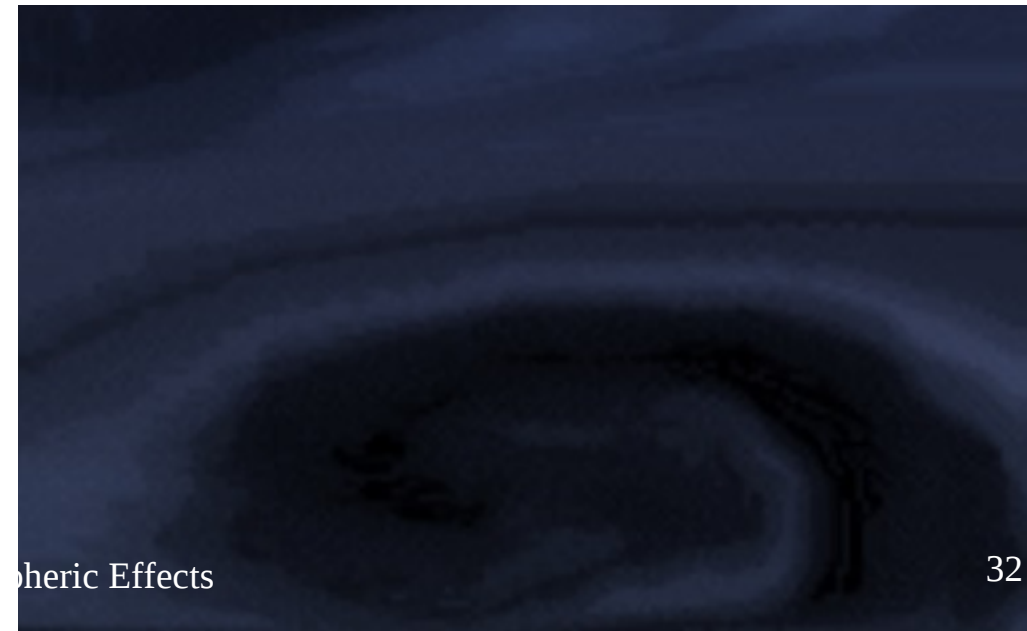
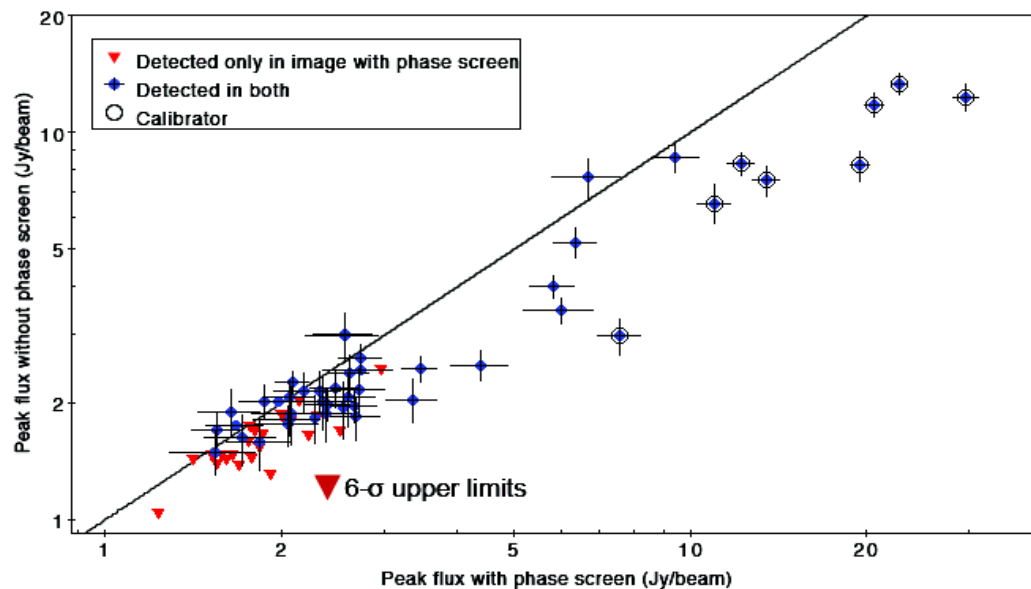
MSSS TECscreen +
A projection

solutions in 8 directions
after correction with
AWimager:
better focused + more
sources detected

Detected Sources at 30 MHz ($>6\sigma$ peak flux)



- At 30 MHz, $\sim 50\%$ more sources detected in image with phase screen ($\sim 30\%$ more at 45 MHz)



Phasescreen Methods

issues:

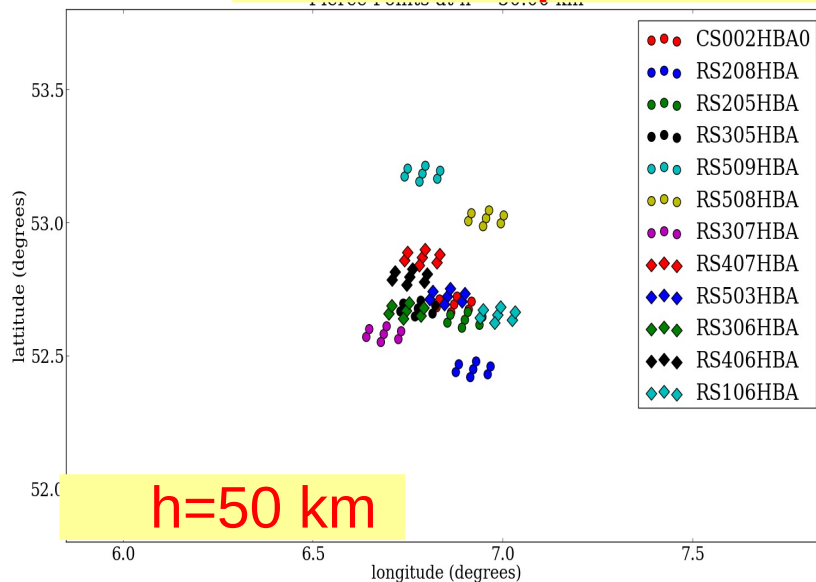
- needs several bright enough sources in FOV
- ignores 3D structure of ionosphere
 - crossing of piercepoints depends on chosen height of layer(s)

Phasescreen Methods

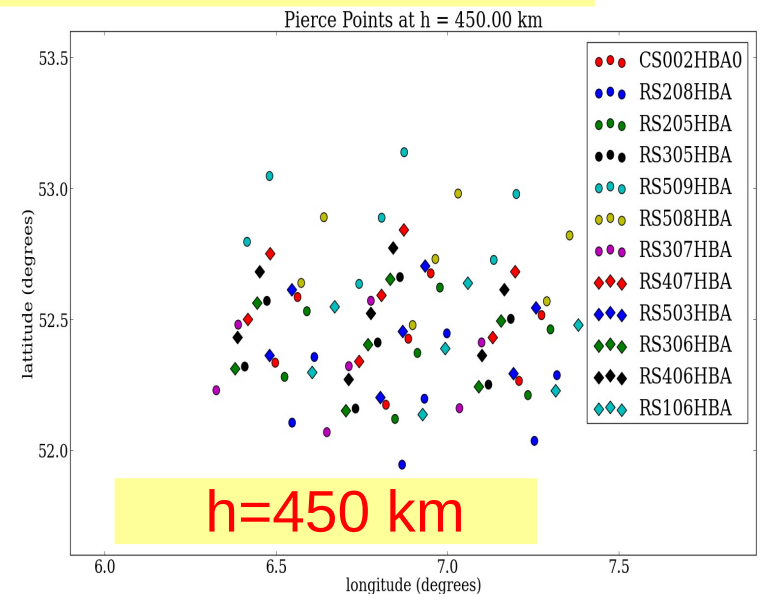
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Piercepoints 7 directions Remote stations



Ionospheric E



Phasescreen Methods

issues:

- needs several bright enough sources in FOV
 - source models
- ignores 3D structure of ionosphere
 - crossing of piercepoints depends on chosen height of layer(s)
 - 3D tomography?
- LOFAR beam errors give also direction dependent phases
 - station dependent
 - makes phasescreen fitting more difficult

Differential Faraday rotation

$$\beta = RM\nu^{-2}$$

Rotation of the signal from XX,YY to XY,YX due to different Faraday rotation angles for different antennas

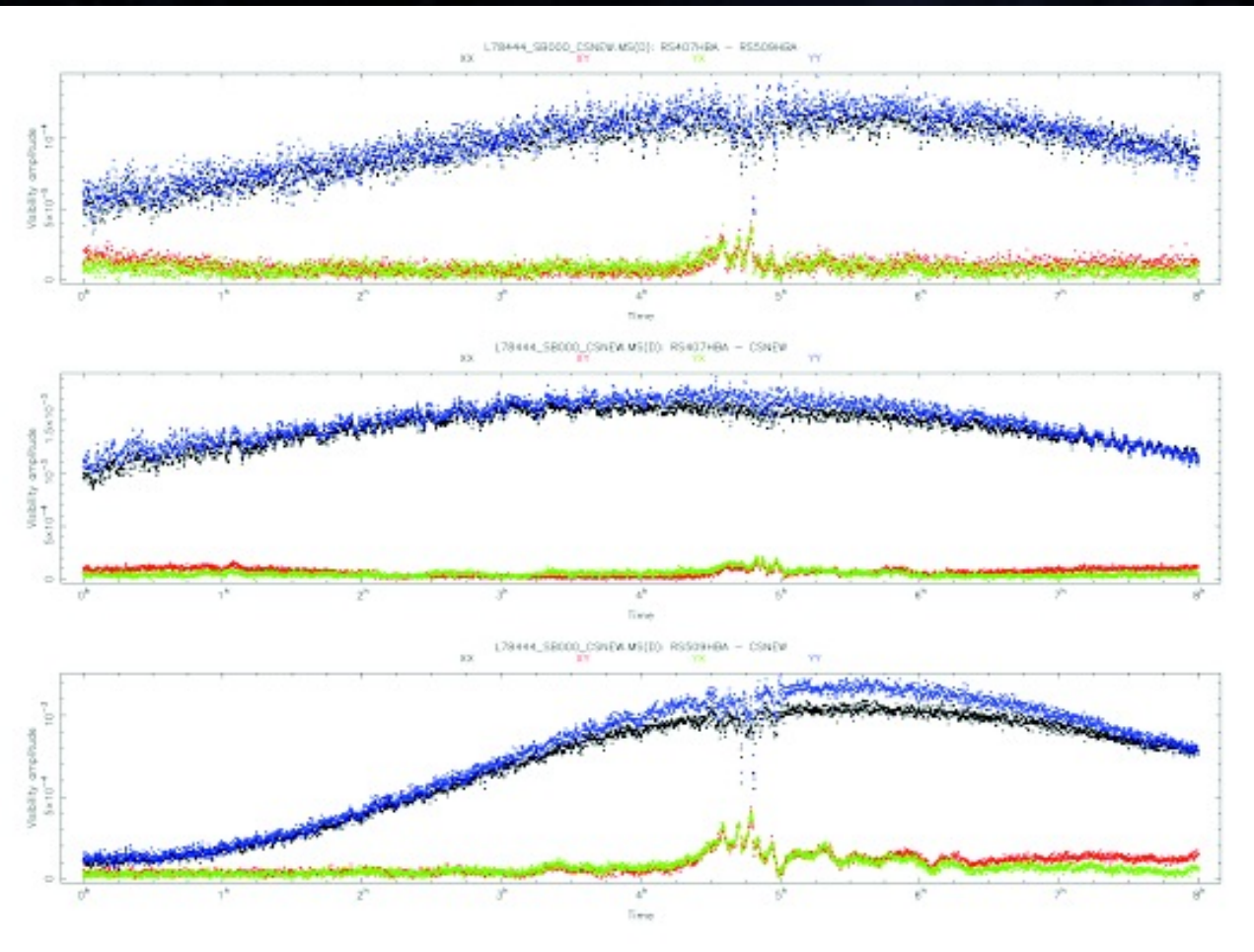
- HBA: small rotation most of the time
 - sometimes ("wild" ionosphere) visible in RAW uv data
- LBA: significant effect

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Selfcal: either solve full polarization matrix or
diagonal gains + 1 rotation matrix

Differential Faraday rotation provides clean independent measure of ionospheric fluctuations (ignoring differential B)

In principle possible to extract absolute TEC via:

$$\Delta RM = \Delta TEC \cdot B_{||} + TEC \cdot \Delta B_{||}$$

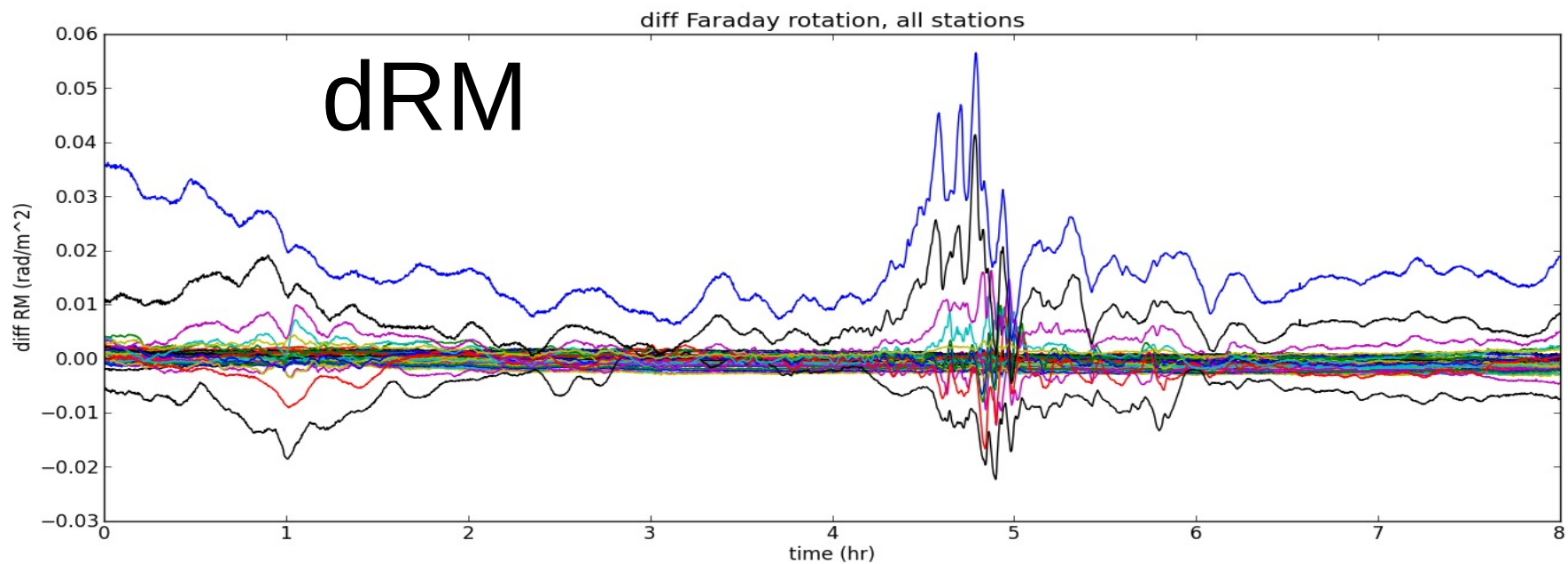
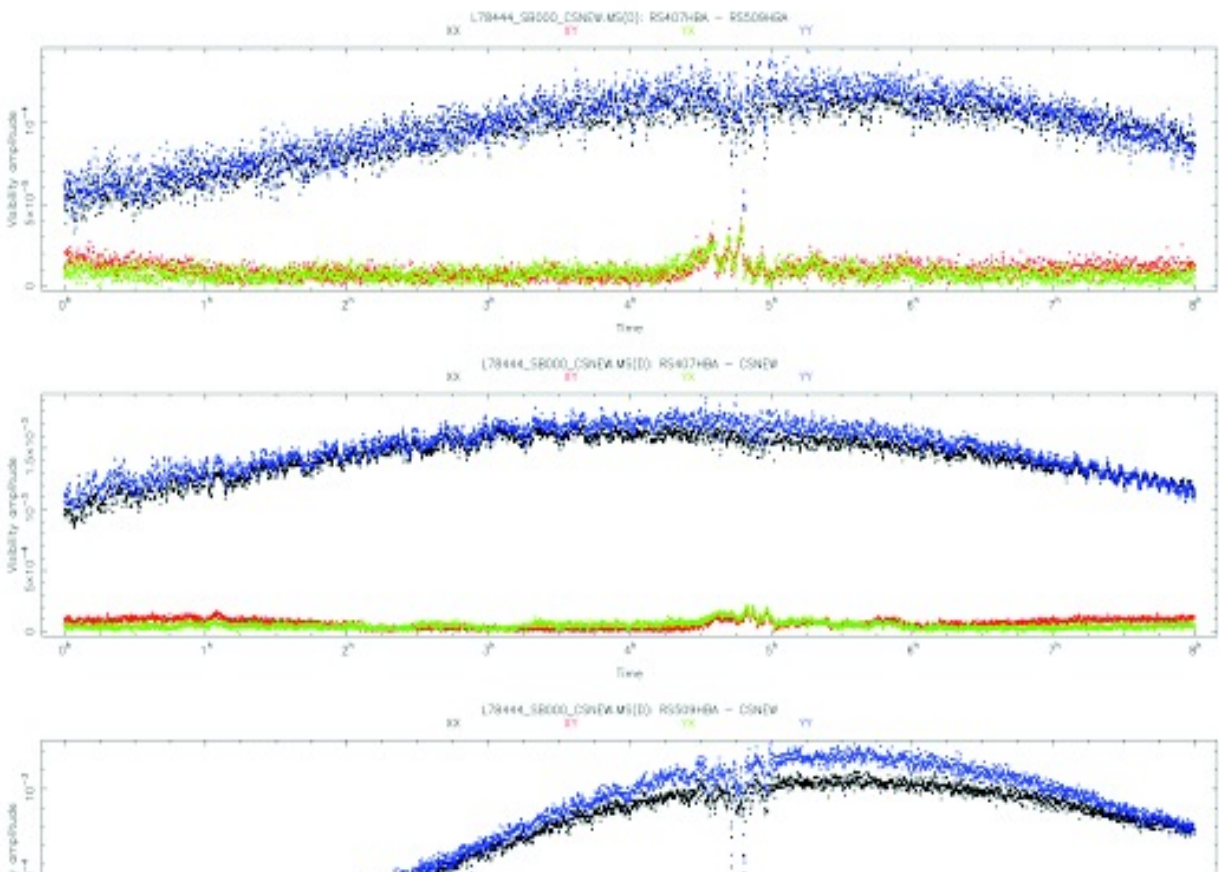
In practice large uncertainty on $\Delta B_{||}$

xy rotation

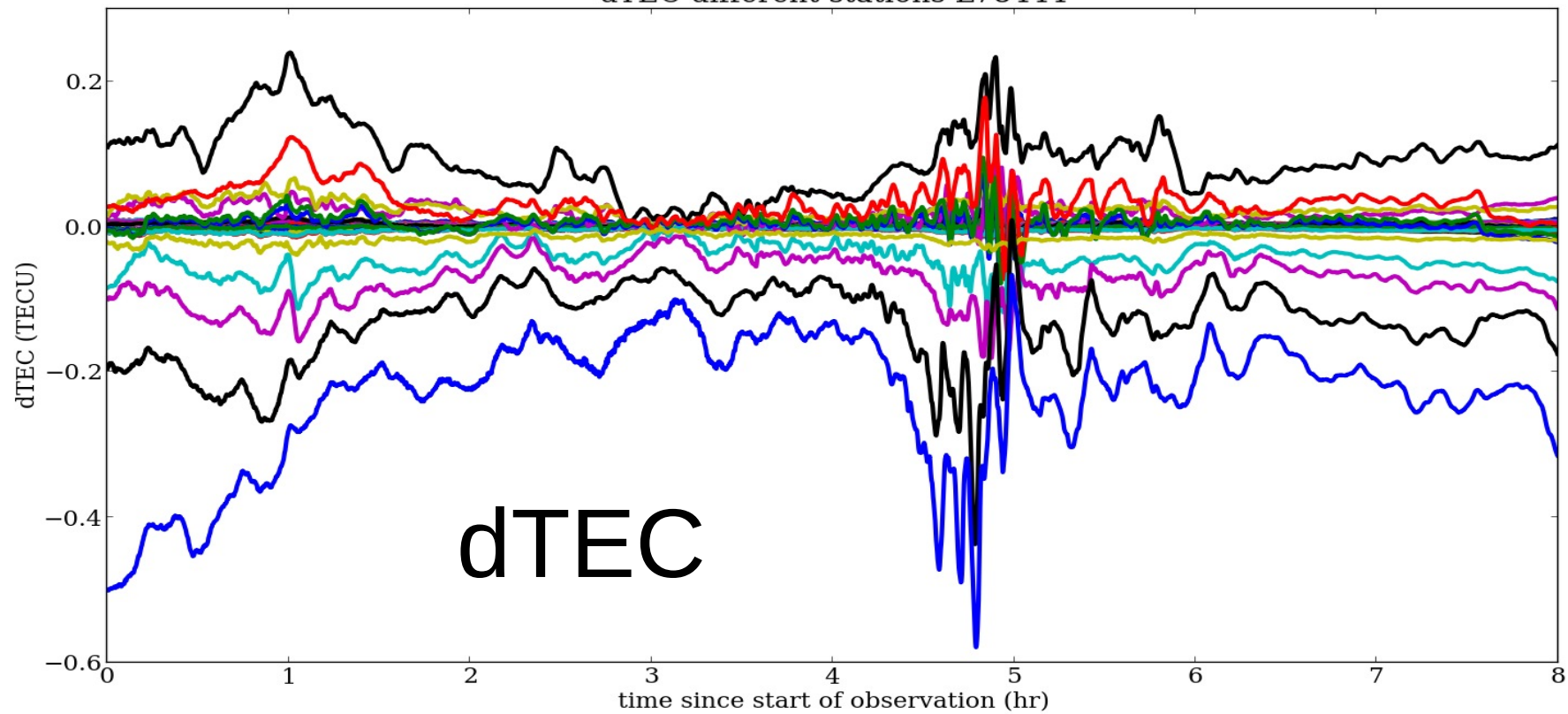
XX,YY to XY,YX due
angles for different

of the time

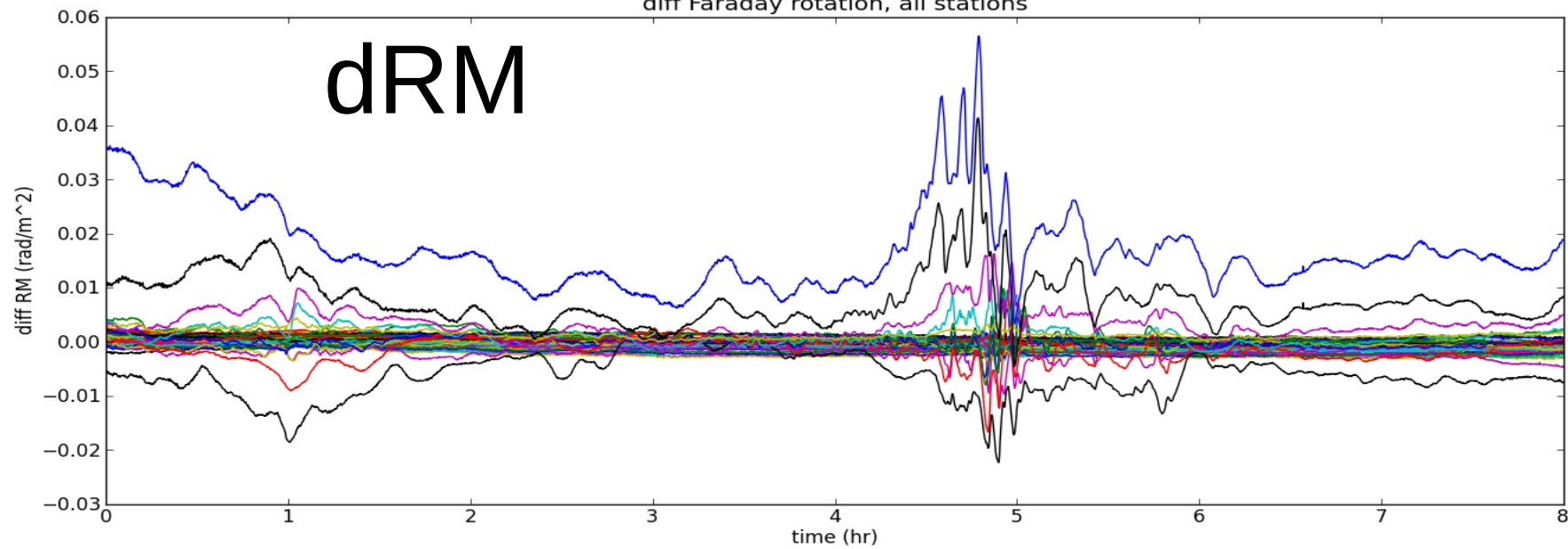
visible in RAW uv data



dTEC different stations L78444



diff Faraday rotation, all stations



Differential Faraday rotation

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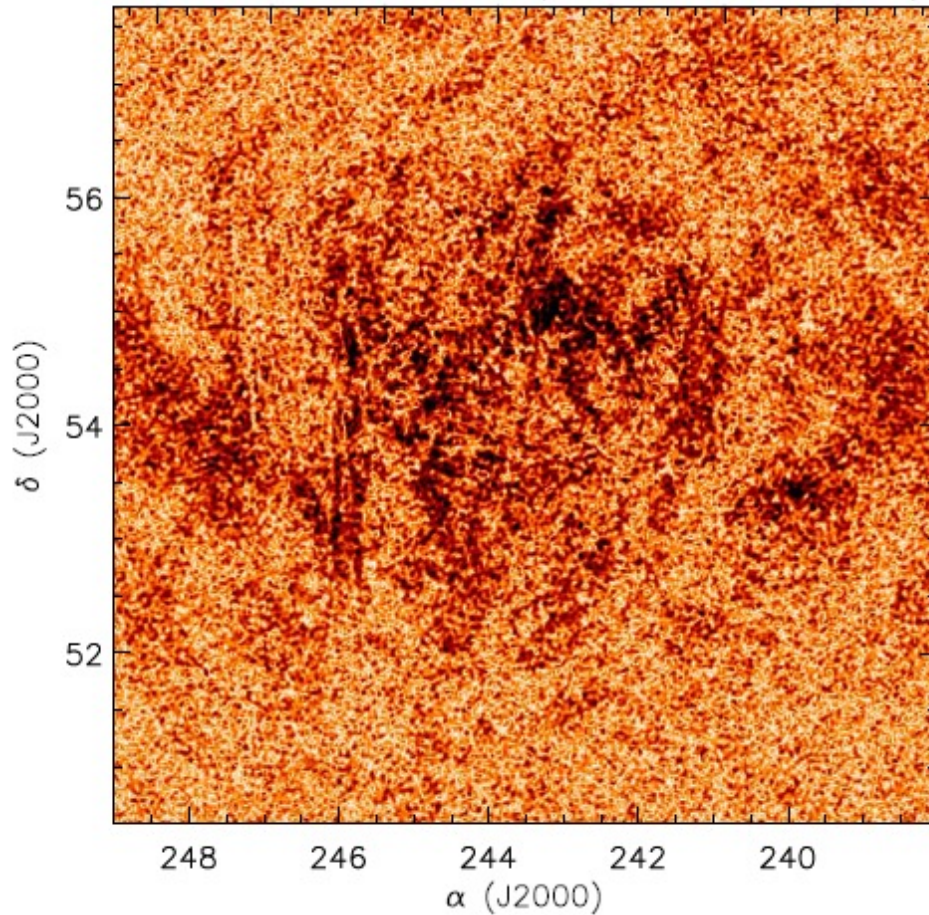
RM correction

- For polarization studies:
 - correct time variation of ionospheric Faraday rotation
- Calculate RM variation:
 - GPS data
 - Earth Magnetic Model:
 - **WMM** Maus, S., S. Macmillan, S. McLean, B. Hamilton, A. Thomson, M. Nair, and C. Rollins, 2010, The US/UK World Magnetic Model for 2010-2015, NOAA Technical Report NESDIS/NGDC.
 - **IGRF** Geophysical Journal International, Volume 183, Issue 3, pages 1216–1230, December 2010
- Correct data using single rotation matrix
 - GPS models do not provide accurate enough resolution to correct spatial variation

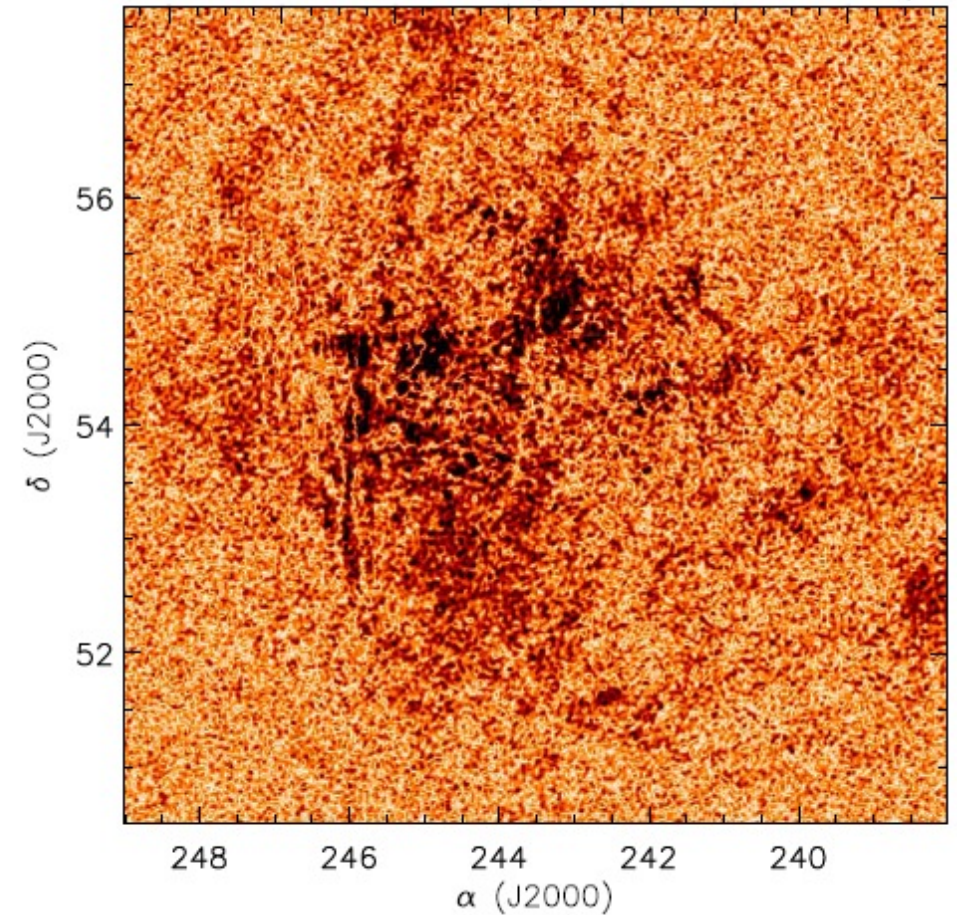
Example Elais Field



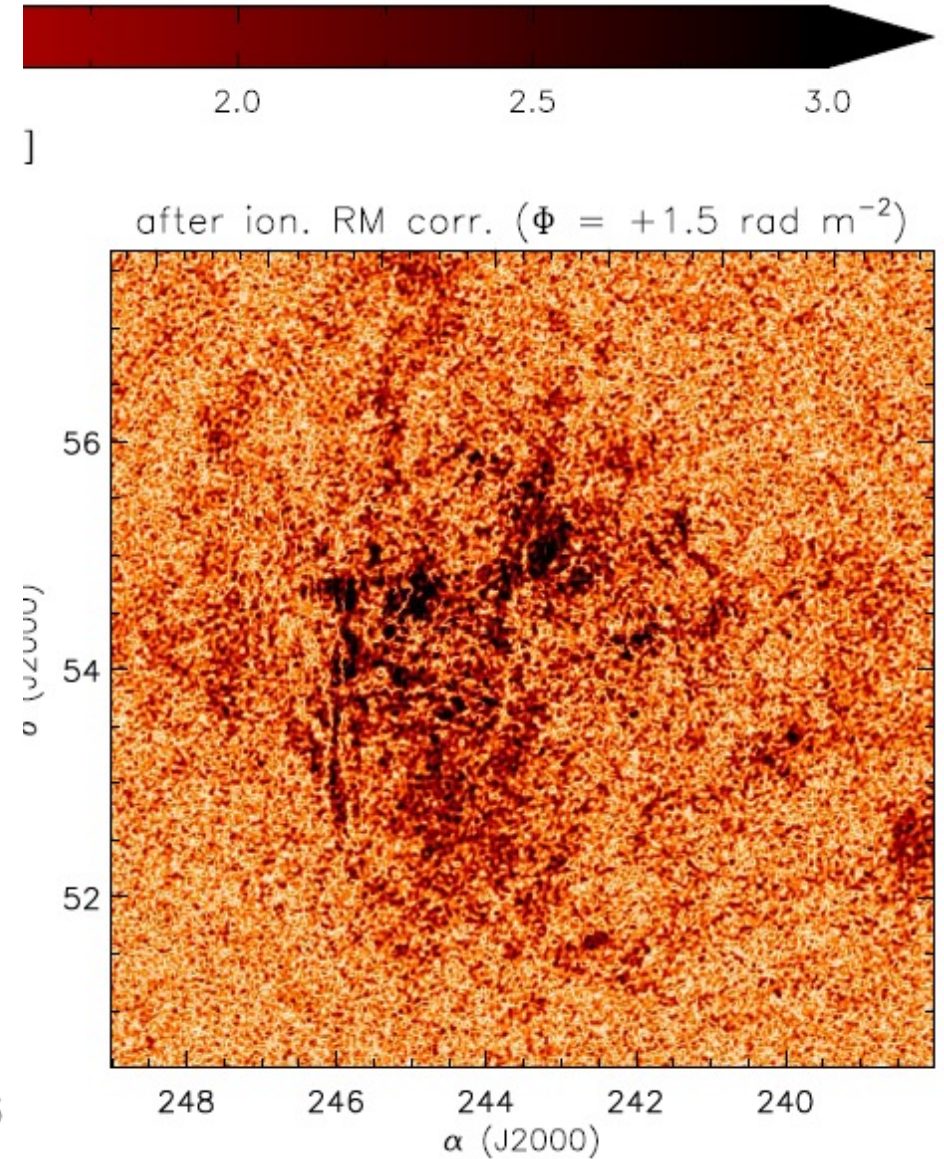
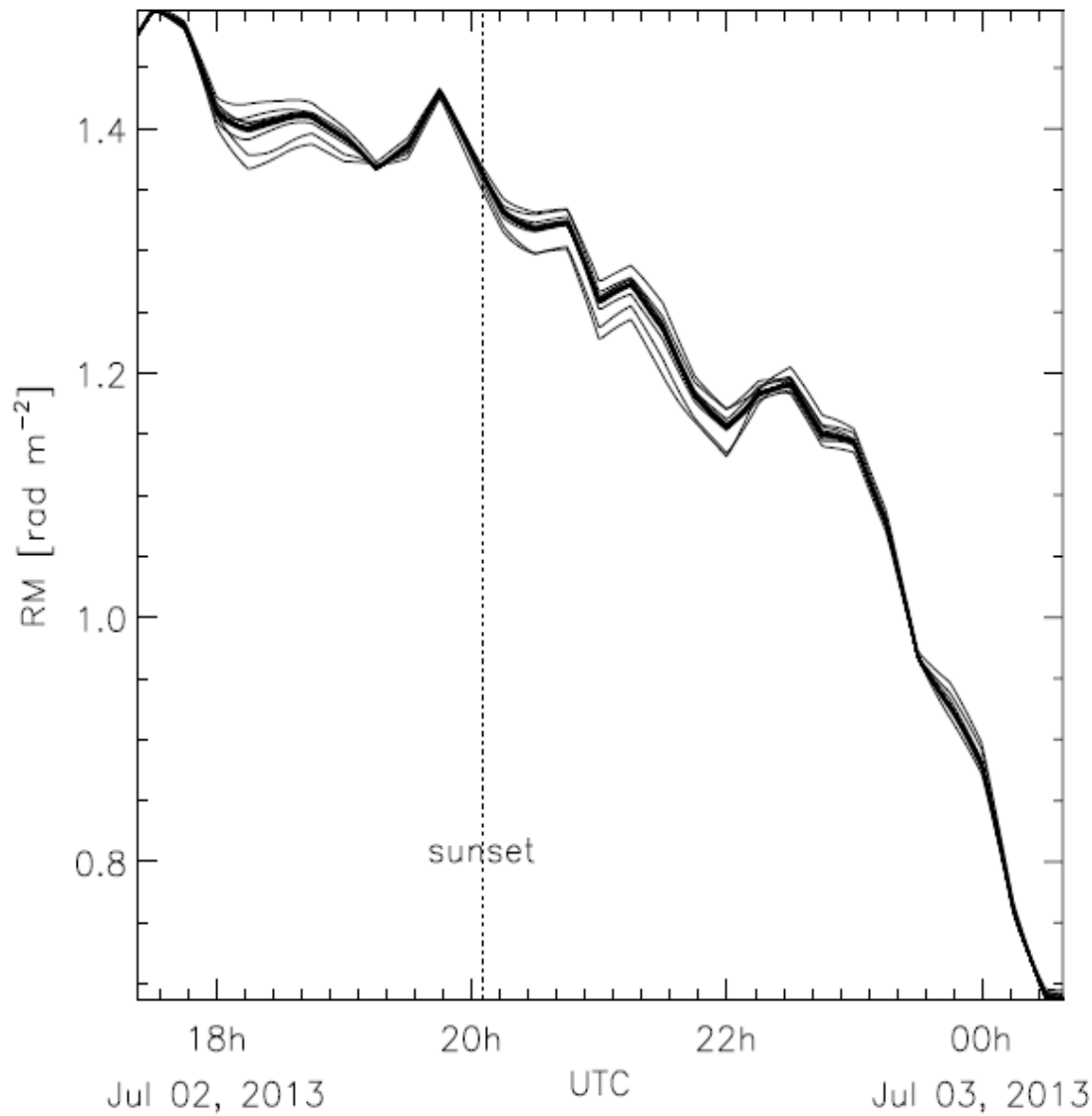
before ion. RM corr. ($\Phi = +2.5 \text{ rad m}^{-2}$)



after ion. RM corr. ($\Phi = +1.5 \text{ rad m}^{-2}$)

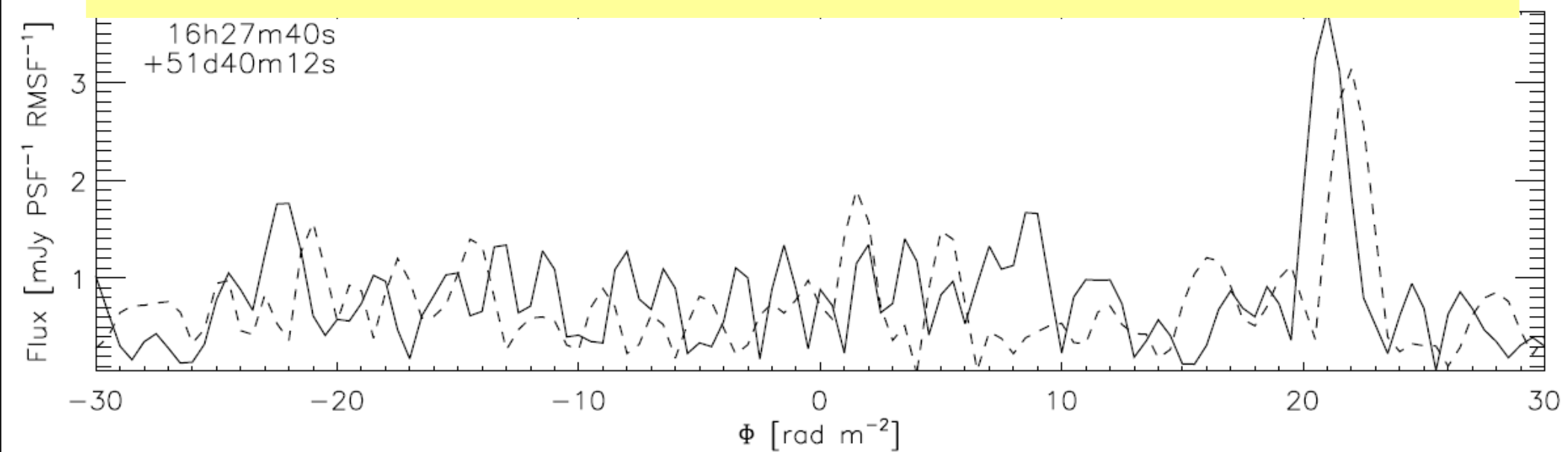


Example Elais Field



Example Elais Field

Polarized Flux before (dashed) and after (solid) RM correction

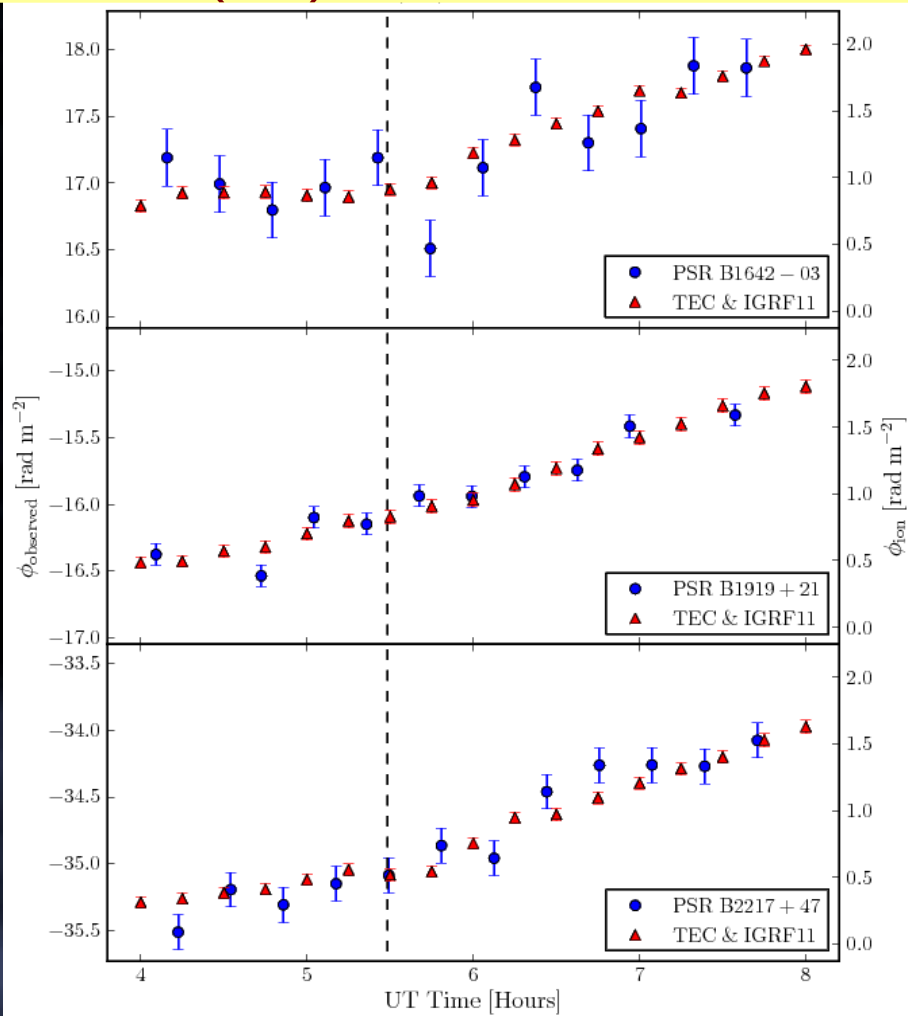


V. Jelic et al (2014)

*Initial LOFAR observations of Epoch of Reionization windows: II.
Diffuse polarized emission in the ELAIS-N1 field*

Other methods

Pulsar (blue) and GPS + IGRF(red) RM variation



use polarized source to determine ionospheric RM

Sotomayor-Beltran et al (2013)

Calibrating high-precision Faraday rotation measurements for LOFAR and the next generation of low-frequency radio telescopes

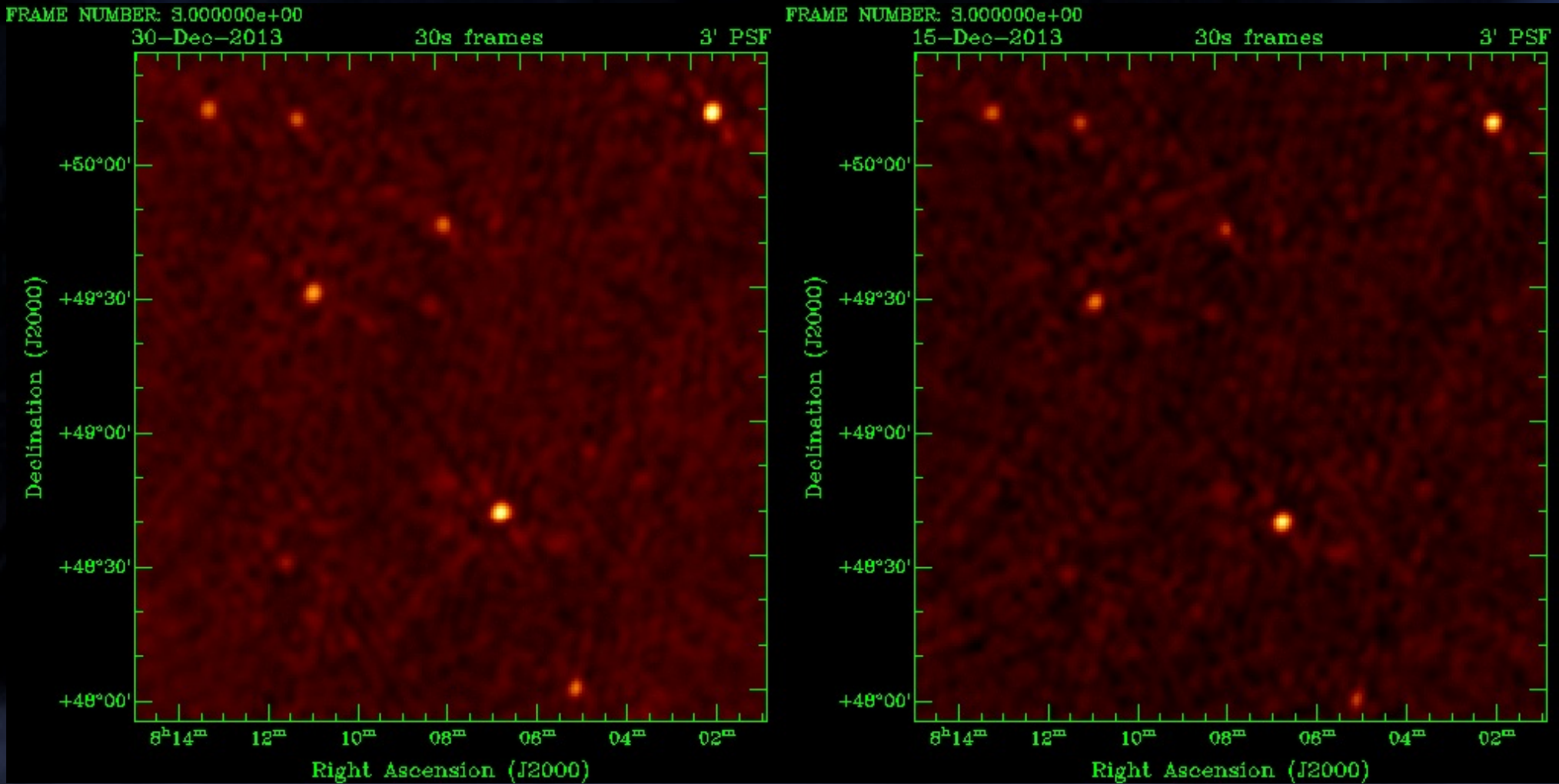
Conclusion

- Effects of ionosphere large at low frequencies
- time variation + frequency dependence requires calibration with high time and frequency resolution
- spatial variation requires direction dependent calibration
- dispersive delays sensitive to differential TEC
- interpolation to other directions via phasescreen approaches

Conclusion (2)

- Faraday rotation:
 - rotation of linear polarization angle
- Differential Faraday rotation
 - significant effect for LBA
 - needs extra rotation matrix in ME
- ionospheric RM correction:
 - using GPS data and Earth magnetic models
 - directly estimate RM from polarized sources

Scintillation



G.de Bruyn