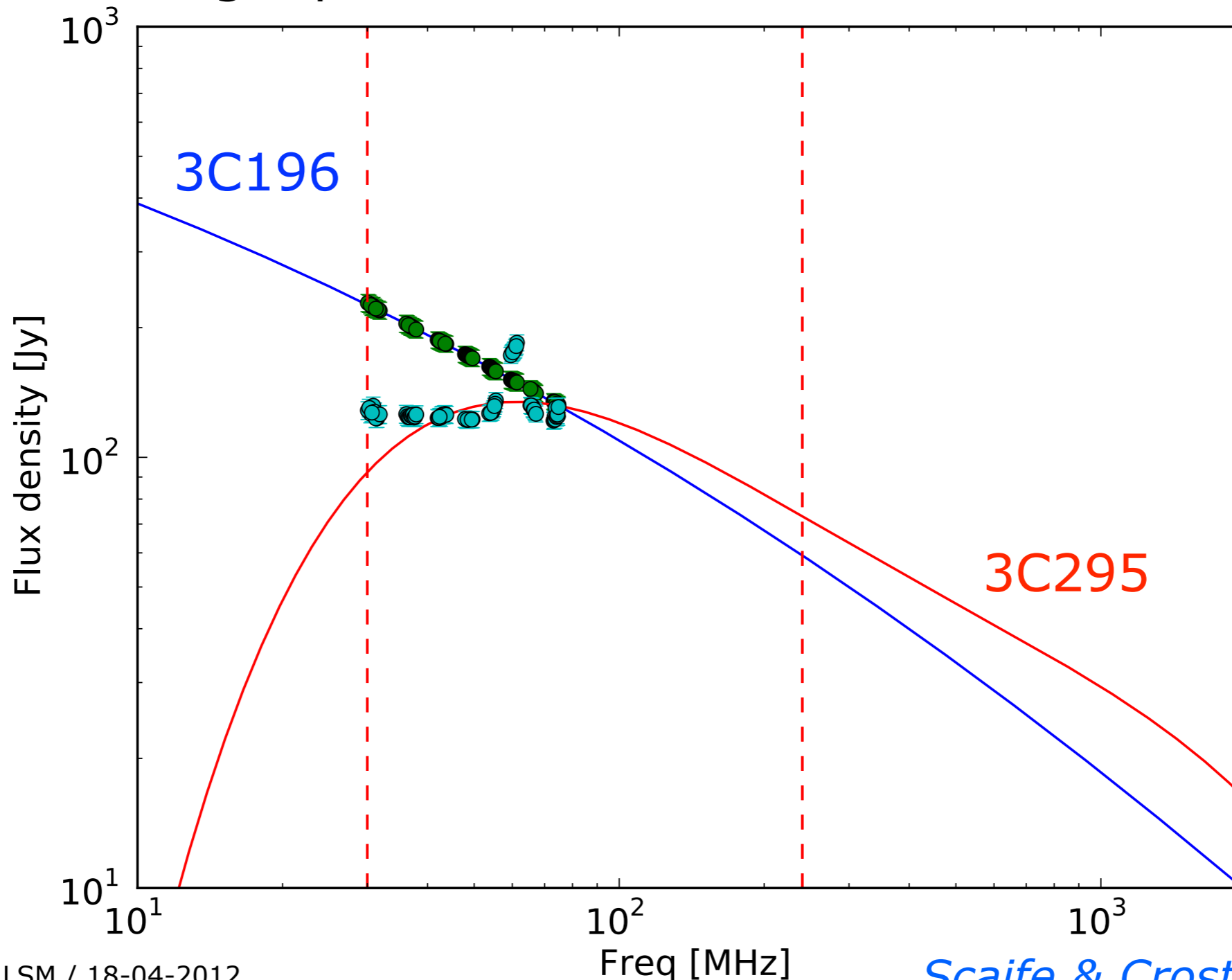


## Update on beams

George Heald  
LSM, 18 April 2012



- Can two calibrators (observed simultaneously in LBA) calibrate each other? Test done with 3C196 and 3C295 (after demixing)
- So far indicating a problem with the element beam model ..... ?



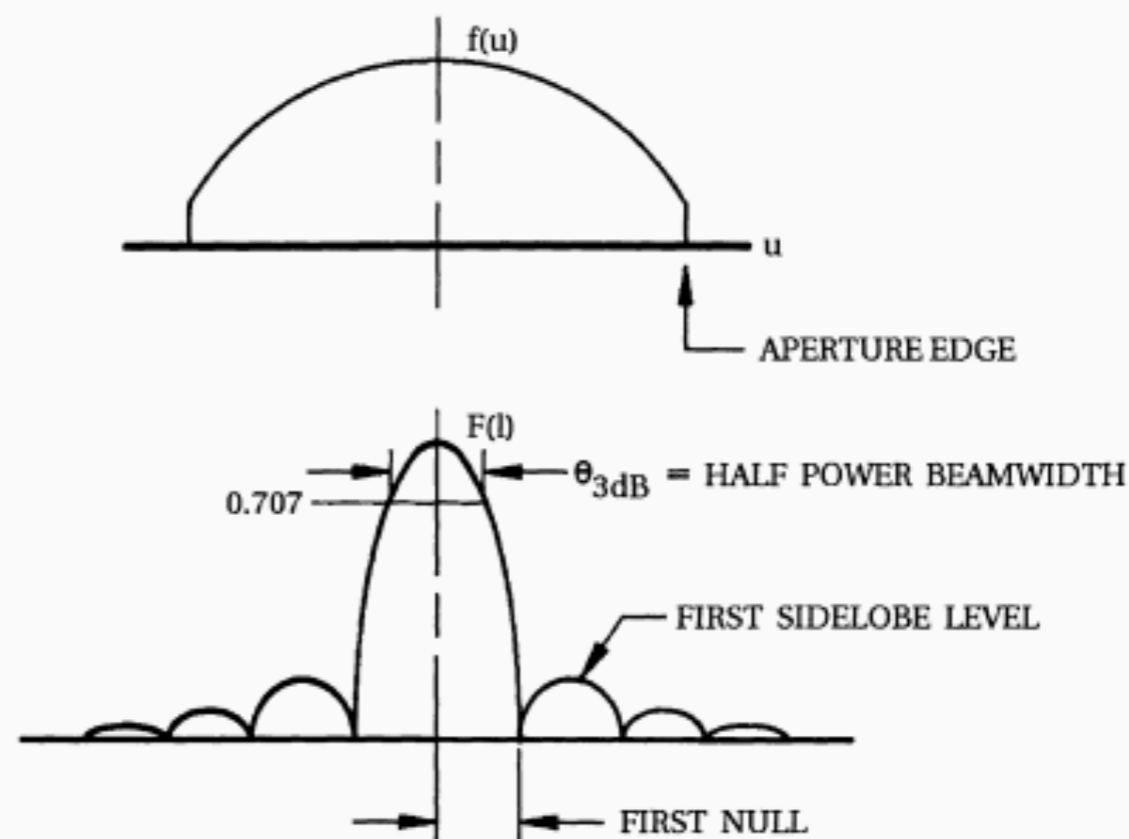
- 15x15 pointing grids centered on CygA
  - Observed so far: HBA\_DUAL (1x) and LBA\_INNER (3x)
  - Processing steps calibrate all pointings in direction of CygA; interpret gain amplitudes as (*voltage*) beam in that direction
- Range of frequencies intended to sample MSSS bands
- Gives excellent discrimination between well-behaved stations and others (mispointings and “squashed” beams)
- Can be done with short observations and quick processing
- Previously shown to give good match between observed beam patterns and prediction of beam model, for well behaved stations

- For a uniformly illuminated aperture, expect the beam pattern to behave like

$$F(u) = \frac{J_1(\pi D u)}{u}$$

- This case has

$$\text{FWHM} = 1.02 \lambda/D$$

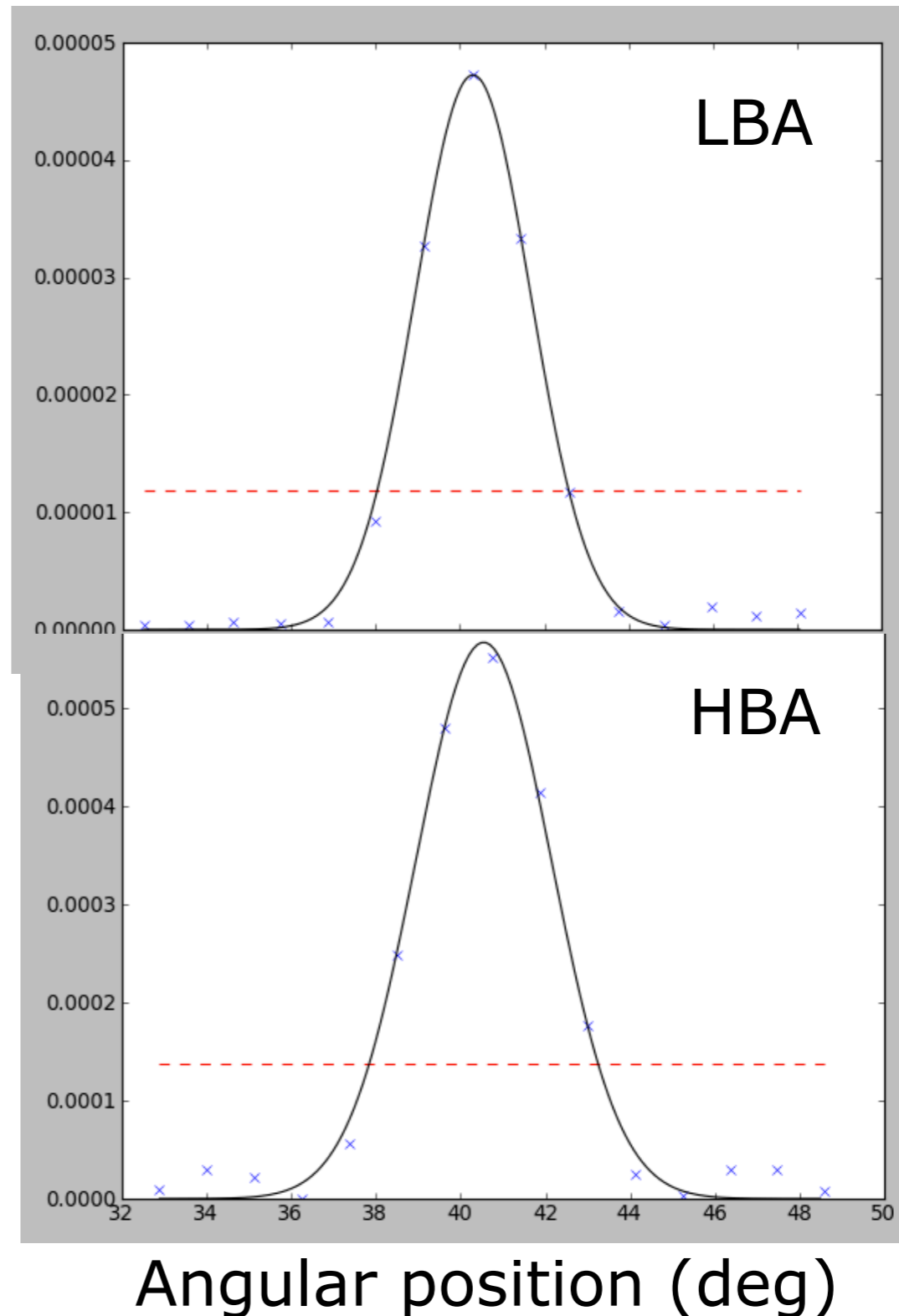
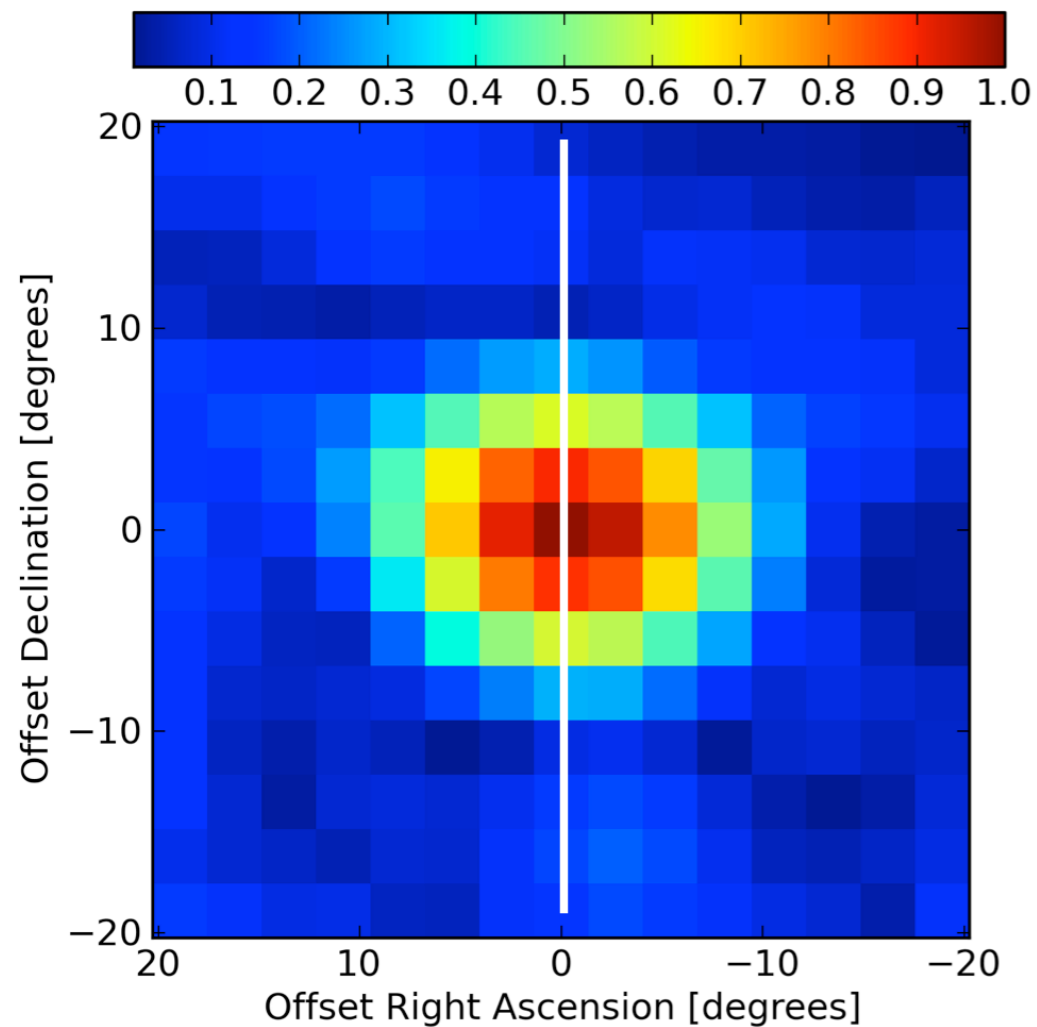


**Figure 3-3.** The Fourier transform relationship between an antenna aperture distribution and its far-field radiation pattern. The form of the aperture distribution,  $f(u)$ , and the radiation pattern,  $F(l)$ , are shown for a one-dimensional example. In general both quantities are complex. Only the amplitudes are shown here.

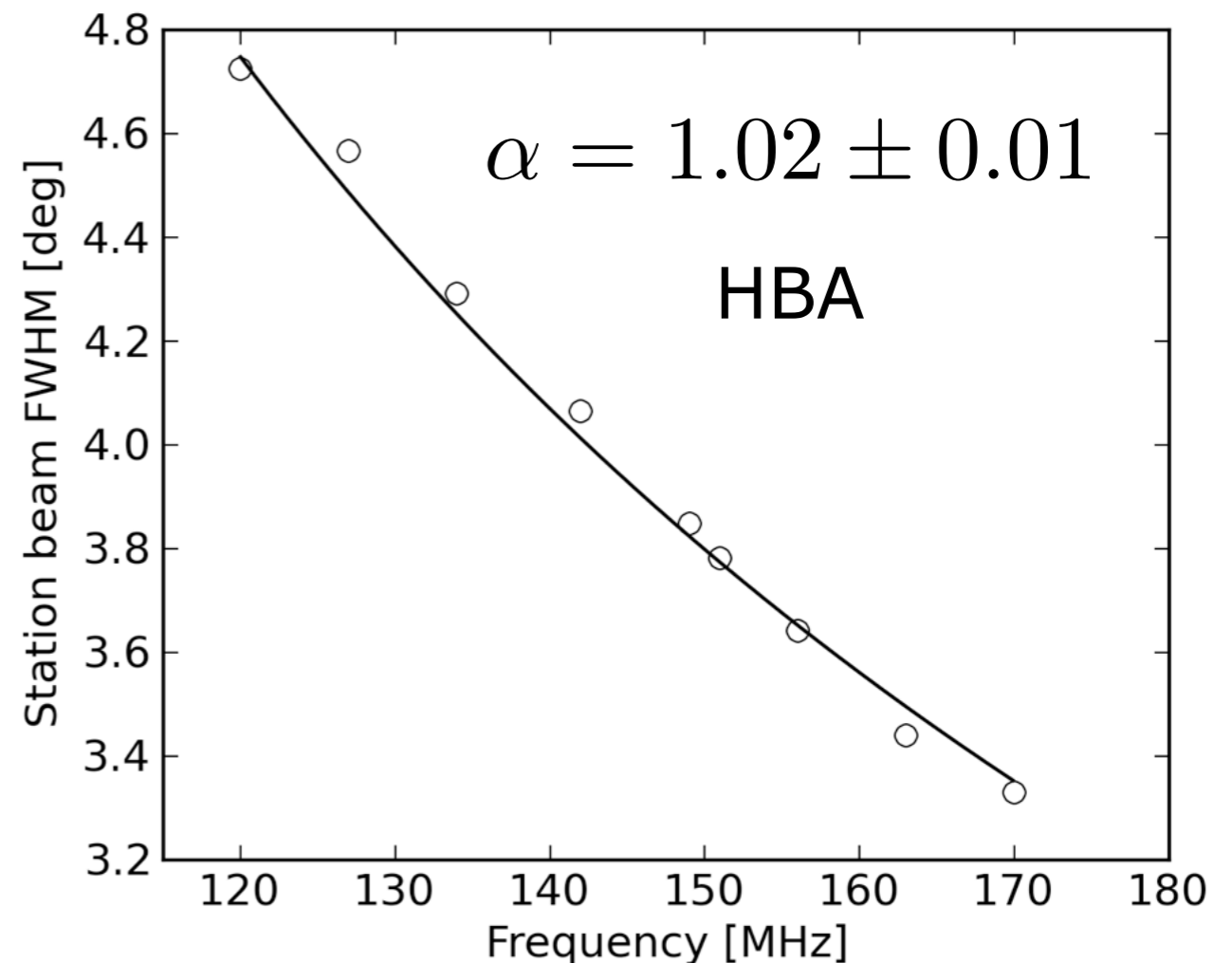
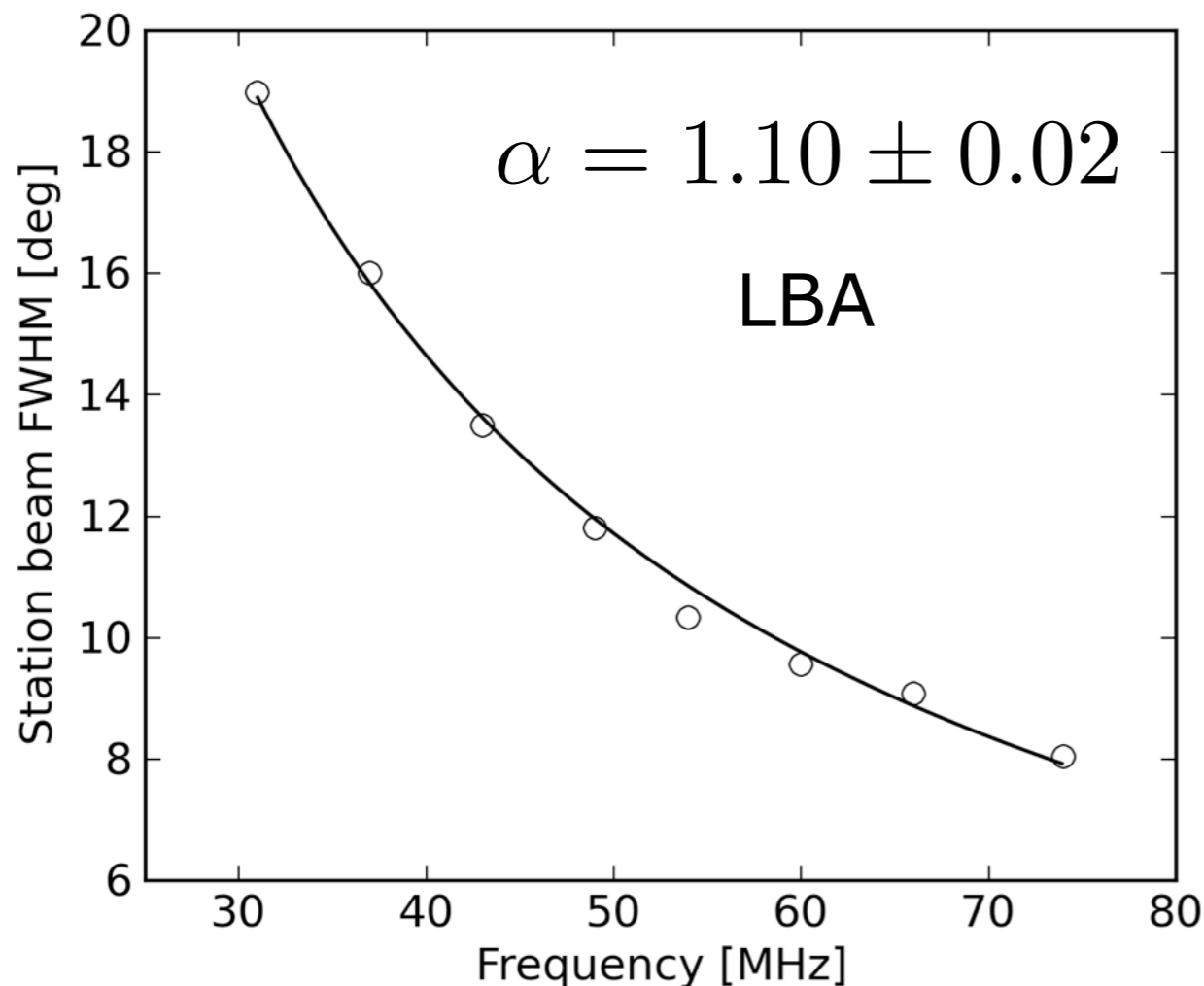
The form of  $f(u, v)$  for an antenna is determined by the way in which the antenna feed illuminates the aperture. In general, the more that  $f(u, v)$  is tapered at the edge of the aperture, the lower will be the aperture efficiency and the sidelobes and the broader the main beam. Tabulations of a wide variety of  $f(u, v)$ , and their  $F(l, m)$ , can be found in antenna textbooks (Hansen 1964, p. 66; Rudge *et al.* 1982, Table 1.2). For example, the VLA antennas are designed to have uniform illumination ( $f(u, v) = \text{constant}$ ) over the whole aperture, except where the aperture is blocked by the subreflector and its support struts. In this case, for a circularly symmetric aperture of diameter  $D$ ,  $F(u) = J_1(\pi D u)/u$ , which has the properties: first sidelobe level =  $-17.6$  dB, half power beamwidth =  $1.02\lambda/D$ , and position of first null =  $1.22\lambda/D$ . These are in good agreement with measured beam parameters for the VLA 25-meter diameter reflector, except for the first sidelobe level, which is modified by aperture blockage as shown in Figure 3-8.

*Napier (1999)*

- FWHM determined in LBA & HBA (both for CS004) using Gaussian fit to station beam, using points above 25% of the peak, e.g.:

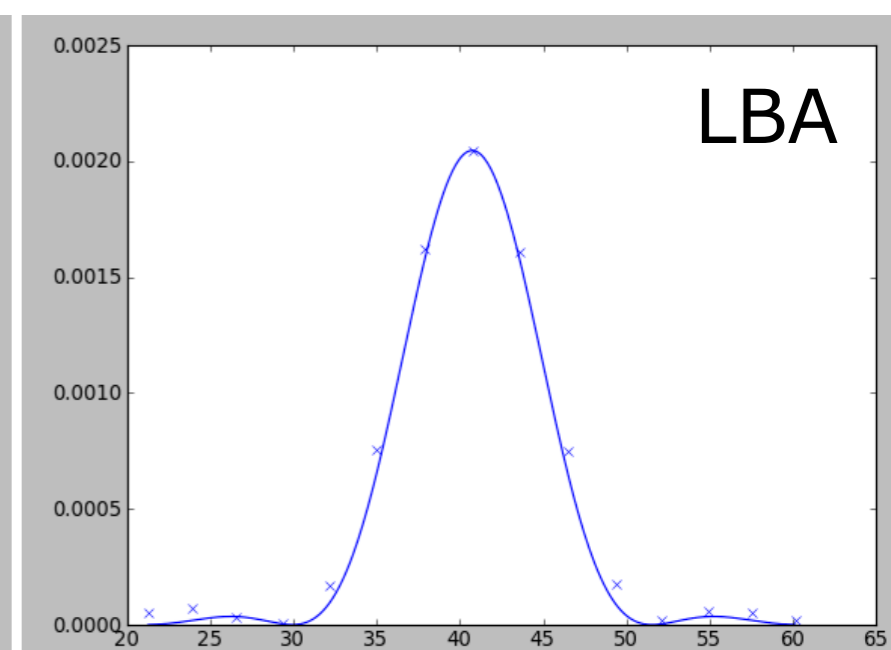
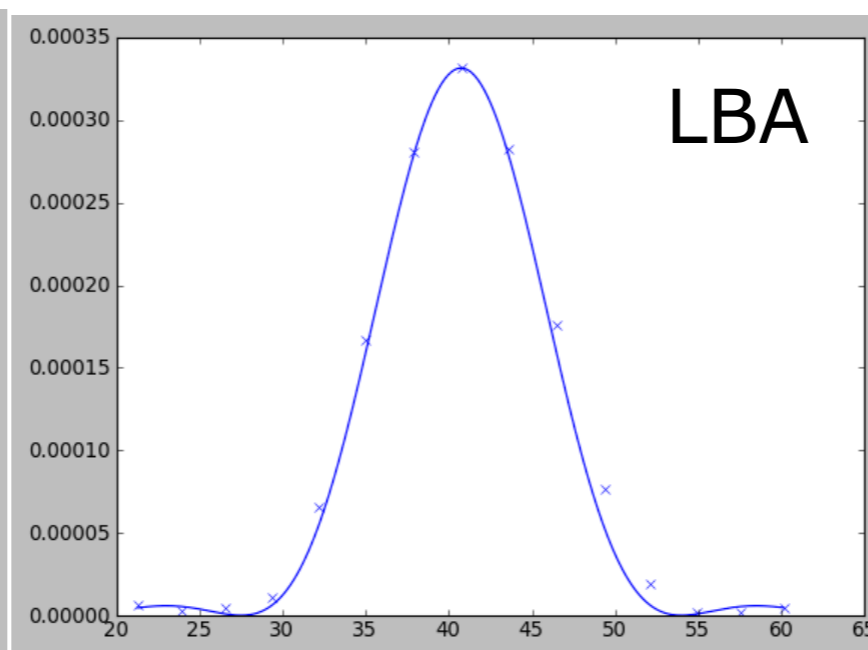
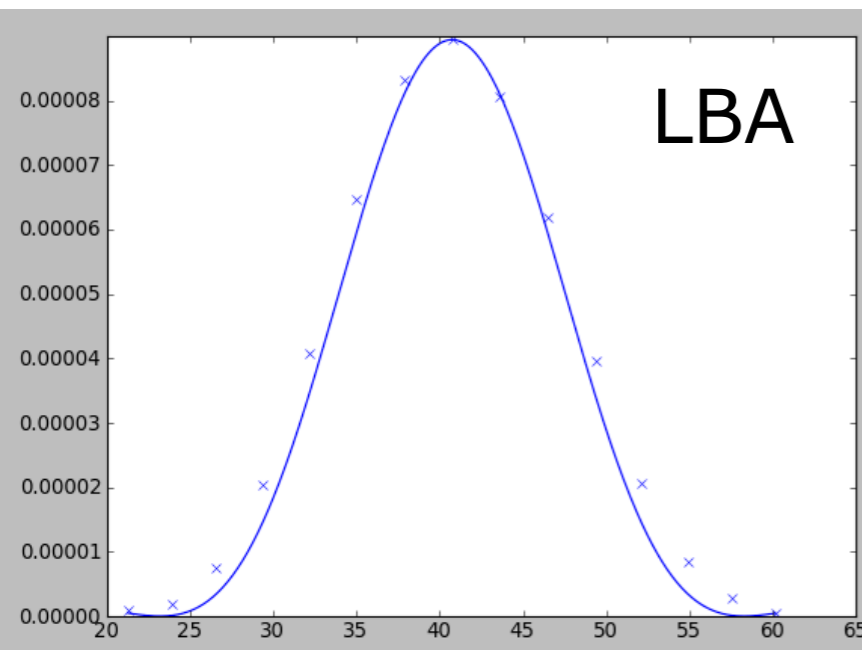
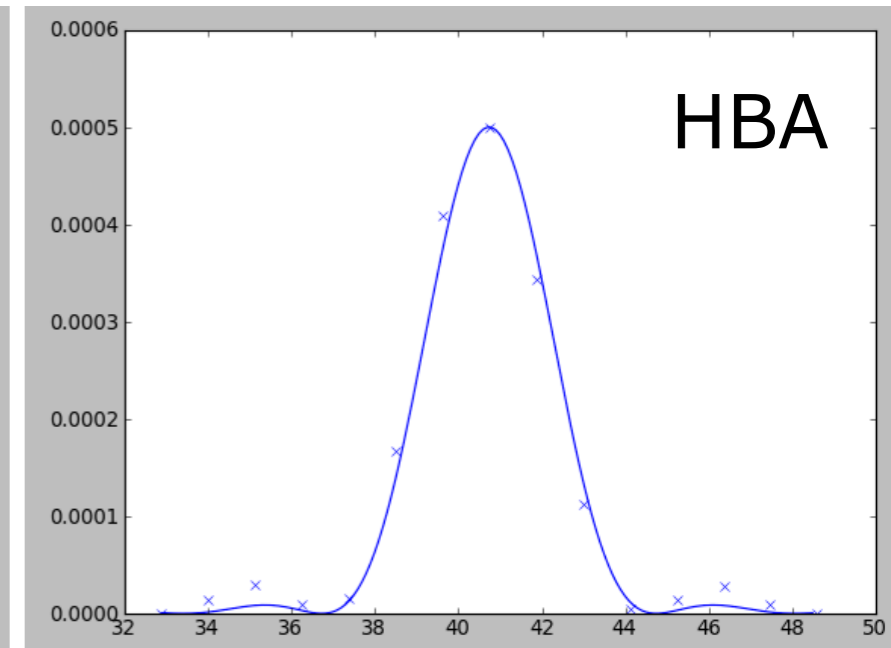
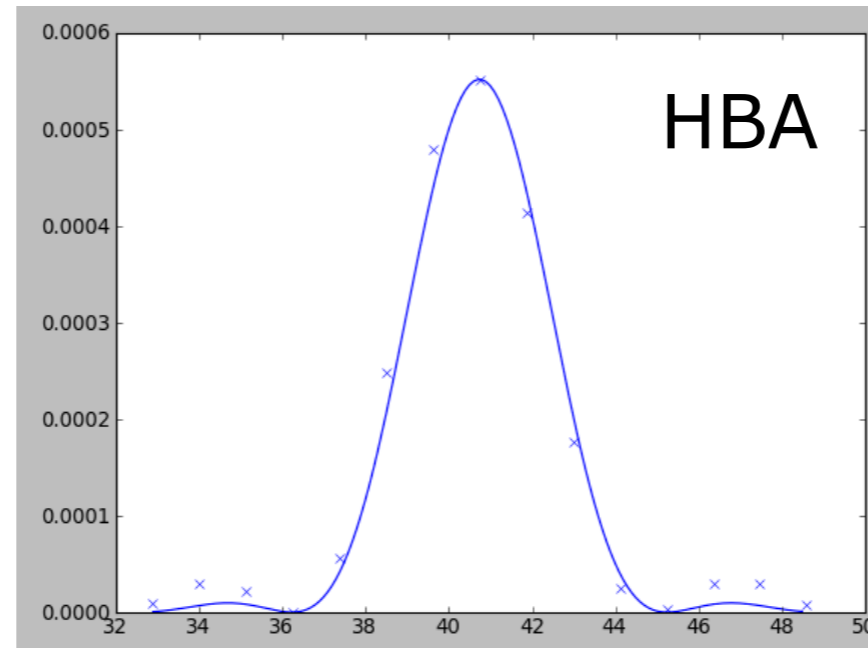
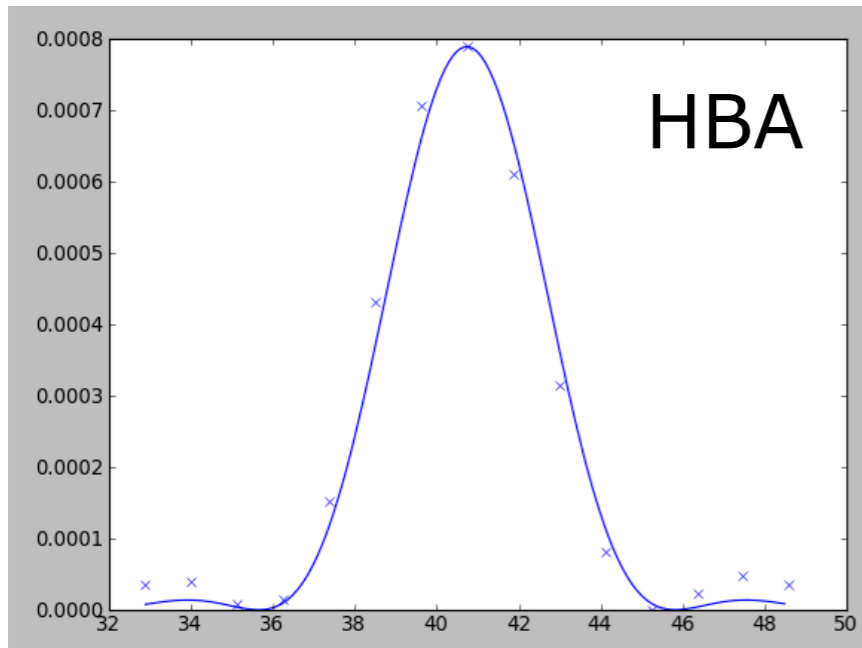


- Variation of beam width expected to follow  $\text{FWHM} = \alpha \frac{\lambda}{D}$
- Value of  $\alpha$  is  $\sim 1.3$  for tapered 25m dish, what is it for LOFAR?
- Fitted run of FWHM vs  $\lambda$  using functional form above
  - error on scale factor estimated using variance of  $(\text{FWHM}/(\lambda/D))$



- Using Bessel-sinc function (prediction only), a good match to the beams is found (though the sidelobe levels are too low for HBA)

**FREQUENCY** 



- Element beam problems? - Further investigation underway.
- Beam mapping not only good for qualitative analysis
- Beam FWHM follows expected trend with wavelength and diameter
  - HBA: scaling factor appropriate for perfectly illuminated "dish"
  - LBA: scaling factor for slightly tapered "dish"
- Beam shapes seem to follow Bessel sinc functions to first order
  - More stations need to be analysed
  - Cannot be completely correct, but what are the limitations?
  - LBA\_OUTER ?????
  - Can analytic beam shapes be used for quick and dirty calibration/imaging?



- Only determined so far for CS004, needs further investigation

