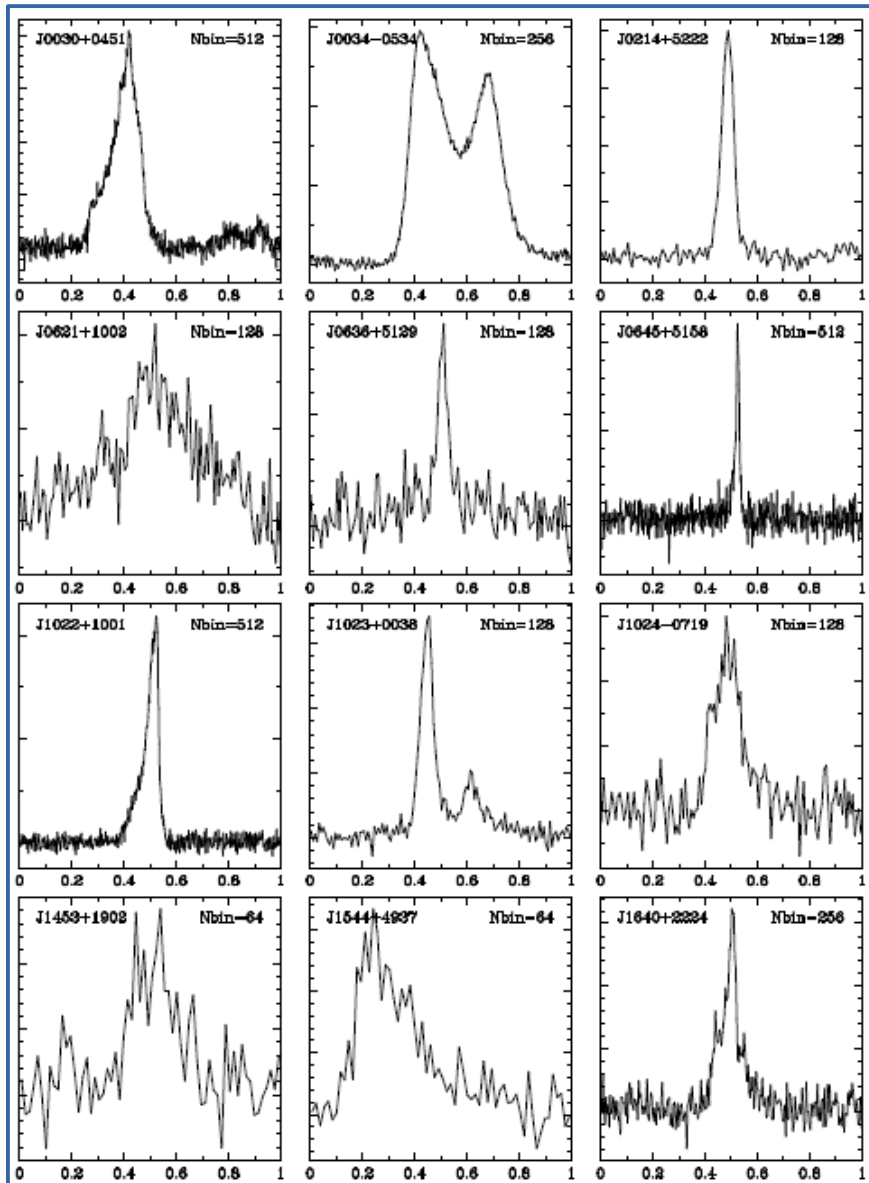


# LOFAR Pulsar Flux Calibration

Vlad Kondratiev (ASTRON),  
Anya Bilous (RU Nijmegen/UvA)

and  
LOFAR Pulsar Working Group



# Flux calibration

In general (see e.g. Lorimer & Kramer 2005):

$$\Delta S_{\text{sys}} = \frac{T_{\text{sys}}}{G \sqrt{n_p t_{\text{obs}} \Delta f}} = C \sigma_p,$$

**C = SEFD**

**LOFAR**

▶  $\Delta f / f \sim 0.5$  (huge)

## Contributing factors

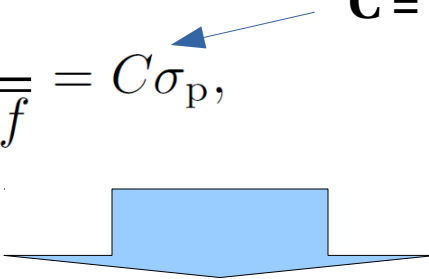
- ▶ Beam shape has strong dependence on AZ, EL, and frequency, and thus the gain,  $G$
- ▶  $\text{Gain}(f) \neq \text{const}$
- ▶  $T_{\text{sys}} = T_{\text{sky}} + T_{\text{inst}}$
- ▶  $T_{\text{sky}}(f) \sim f^{-2.55}$
- ▶  $T_{\text{inst}}(f) \neq \text{const}$
- ▶  $T_{\text{src}}(f) \neq \text{const}$  (ignore for now)
- +
- ▶ Broken tiles ( $\sim 5\%$ )
- ▶ Coherence scaling  $S/N \sim N^{0.85}$ ,  $N$  — number of 48-tile stations
- ▶ Radio frequency interference (RFI), on average 25-30% (MSP data, 1 ch/sub, normally — much less)

# Flux calibration

In general (see e.g. Lorimer & Kramer 2005):

$$\Delta S_{\text{sys}} = \frac{T_{\text{sys}}}{G \sqrt{n_p t_{\text{obs}} \Delta f}} = C \sigma_p,$$

**C = SEFD**



$$\text{SEFD} = \frac{2\beta k [T_{\text{inst}}(f) + T_{\text{sky}}(f, \text{GL}, \text{GB})]}{N_s^\gamma A_{\text{eff}}(f, \text{EL}) [1 - \xi] \sqrt{n_p [1 - \zeta(f)] \left(\frac{T_{\text{obs}}}{\text{nbins}}\right) \Delta f}}$$

$\beta$  — digitization factor = 1  
 GL, GB — Galactic longitude and latitude  
 $\gamma$  — coherence factor  $\approx 0.85$   
 $N_s$  — number of stations used  
 $n_p$  — number of polarizations (2)  
 $A_{\text{eff}}$  — effective area of a 48-tile station

$\xi$  — average fraction of bad/flagged dipoles/tiles  
 $\zeta$  — RFI fraction  
 nbins — number of bins in the profile  
 $T_{\text{obs}}$  — observation length (s)  
 $\Delta f$  — frequency channel width (Hz)

# Beam models

- 1) **“arts”** model (Arts, Kant & Wijnholds 2013), improved Hamaker model
- 2) **“arisN”** model (Noutsos et al. 2015)
- 3) **“hamaker\_carozzi”** model (Hamaker 2006 + Tobia Carozzi's implementation «mscorp»[mscorp](#), on Github)

# Beam models

1) **“arts”**, improved Hamaker model, provides full EM simulations of a 24-tile HBA sub-station, including edge effects and grating lobes (Hamaker's model is based on an infinite array of elements).

In practice →

Table of 91 ELs \* 361 AZs \* 29 frequencies

- AZ, 0 — 360 deg, 1-deg step
- EL, 0 — 90 deg, 1-deg step
- Frequency, 110 — 250 MHz, 5-MHz step

Note! When calibrating, for a given EL  $A_{\text{eff}}$  is averaged over all azimuths, as the stations are randomly rotated.

2) **“arisN”**, maximum theoretical value of  $A_{\text{eff}}$  ( $A_{\text{max}}$ ) is scaled as  $\sim \sin(\text{EL})^{1.39}$  as in Noutsos et al. (2015). For HBA,  $A_{\text{max}} = 48 * 16 * \min\{\lambda^2/3, 1.5625\}$ .

3) **“hamaker\_carozzi”**, maximum theoretical value of  $A_{\text{eff}}$  ( $A_{\text{max}}$ ) is corrected by a corresponding factor calculated from the Carozzi's implementation of the Hamaker model. In practice, we use functions from the “mscorp” package (on Github) written by Tobia Carozzi that calculate Jones matrices for a given HBA station, date/time and frequency (there is also a standalone script `antennaJones.py` to do that). Unlike “arts” model, this model is based on a real station (it uses coordinates, cable delays and time deltas). We used CS001, the difference for other stations is much smaller than the nominal flux error.

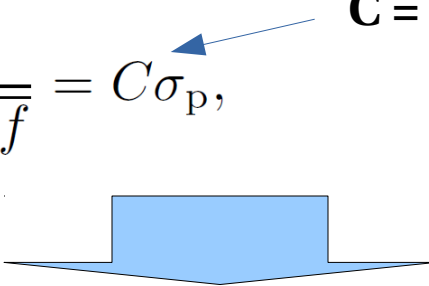
$A_{\text{eff}}$  is scaled by  $B(\text{PSR})/B(\text{CasA})$ , where  $B = 0.5 * |J_{xx} \times J_{xx}^* + J_{xy} \times J_{xy}^* + J_{yx} \times J_{yx}^* + J_{yy} \times J_{yy}^*|$ . The value of  $B(\text{PSR})$  is normalized by reference value of the CasA observation  $B(\text{CasA})$  used in Wijnholds & van Cappelen for A/T measurements. Although, for all freqs the value for CasA is almost 1.0 (changing in 2-3 digits after decimal point).

# Flux calibration

In general (see e.g. Lorimer & Kramer 2005):

$$\Delta S_{\text{sys}} = \frac{T_{\text{sys}}}{G \sqrt{n_p t_{\text{obs}} \Delta f}} = C \sigma_p,$$

**C = SEFD**



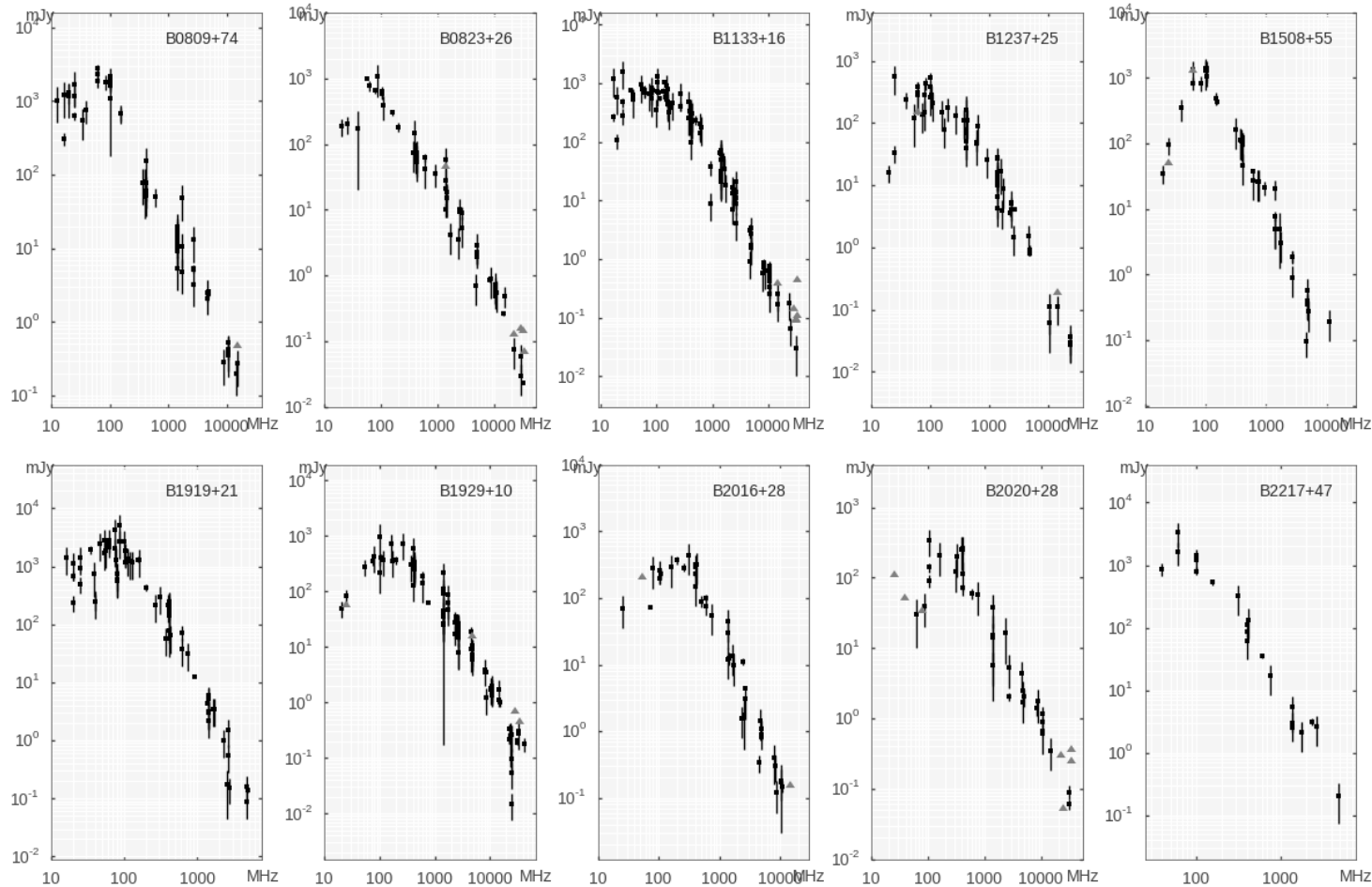
$$\text{SEFD} = \frac{2\beta k [T_{\text{inst}}(f) + T_{\text{sky}}(f, \text{GL}, \text{GB})]}{N_s^\gamma A_{\text{eff}}(f, \text{EL}) [1 - \xi] \sqrt{n_p [1 - \zeta(f)] \left(\frac{T_{\text{obs}}}{\text{nbins}}\right) \Delta f}}$$

For all three beam models all ingredients are the same except for the value of  $A_{\text{eff}}$

# Testing flux calibration with timing observations

**Timing observations of 10 slow bright pulsars.  
Covering about a year (2014), ~10 sessions per PSR.**

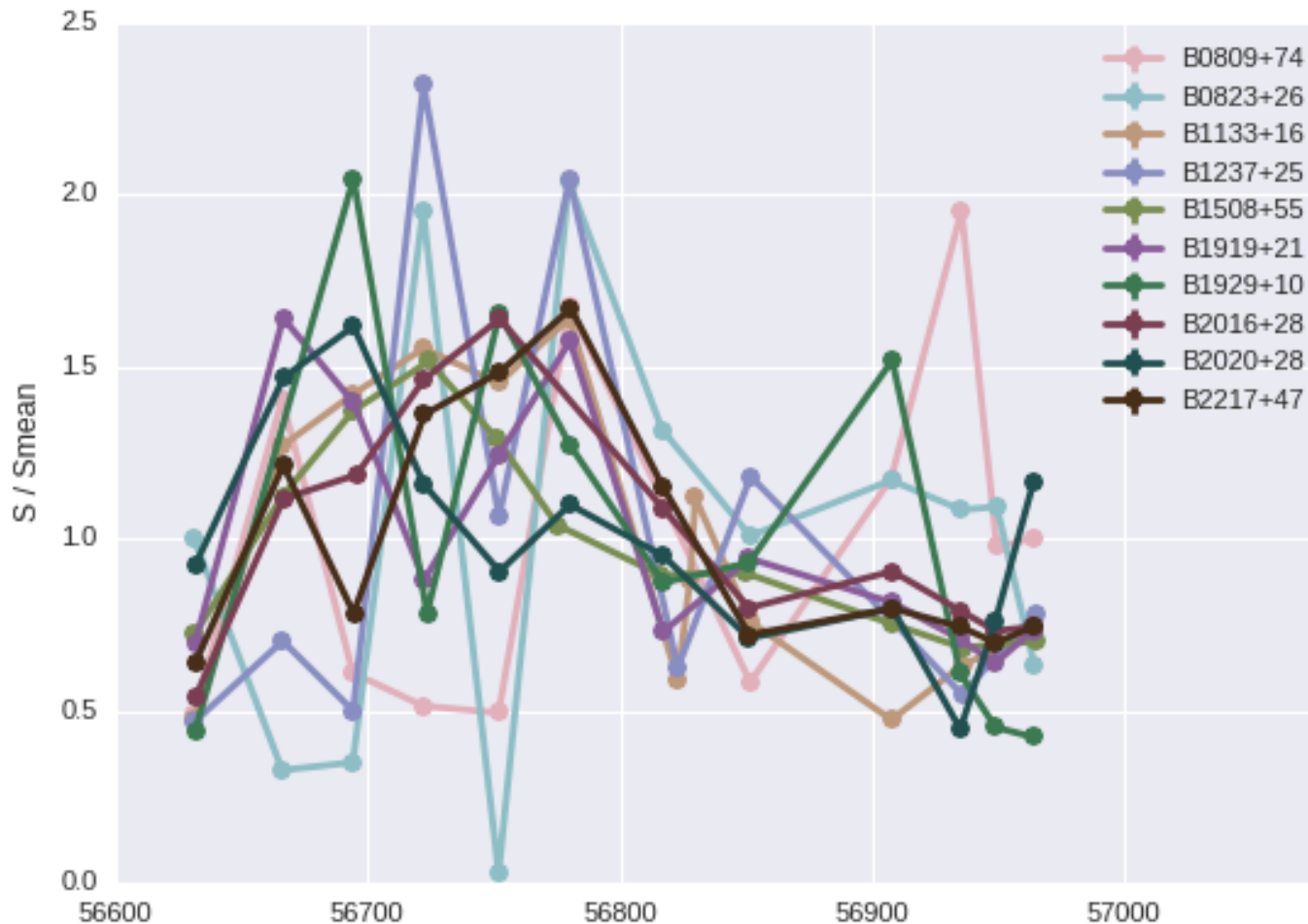
For all 10 pulsars the spectra were already fairly well measured by others:



- RFI excision – paz and psrzap
- DM from census observations

# Flux stability

Beam model: hamaker\_carozzi



For band-integrated fluxes,  
DISS is averaged out within  
band width,  
RISS within 10-20%

- Flux dependence on MJD is very similar for “arts” and “arisN” beam models
- Large variations (within a factor of 2, -50%, +100%). Nominal error (set by rms of noise in off-pulse window) is within markers
- Seemingly correlated variation of fluxes for different pulsars

**Careful! B0823+26 and B1237+25 are moding pulsars.**  
(B1508+55 is also moding, but we did not see any big profile evolution between sessions)

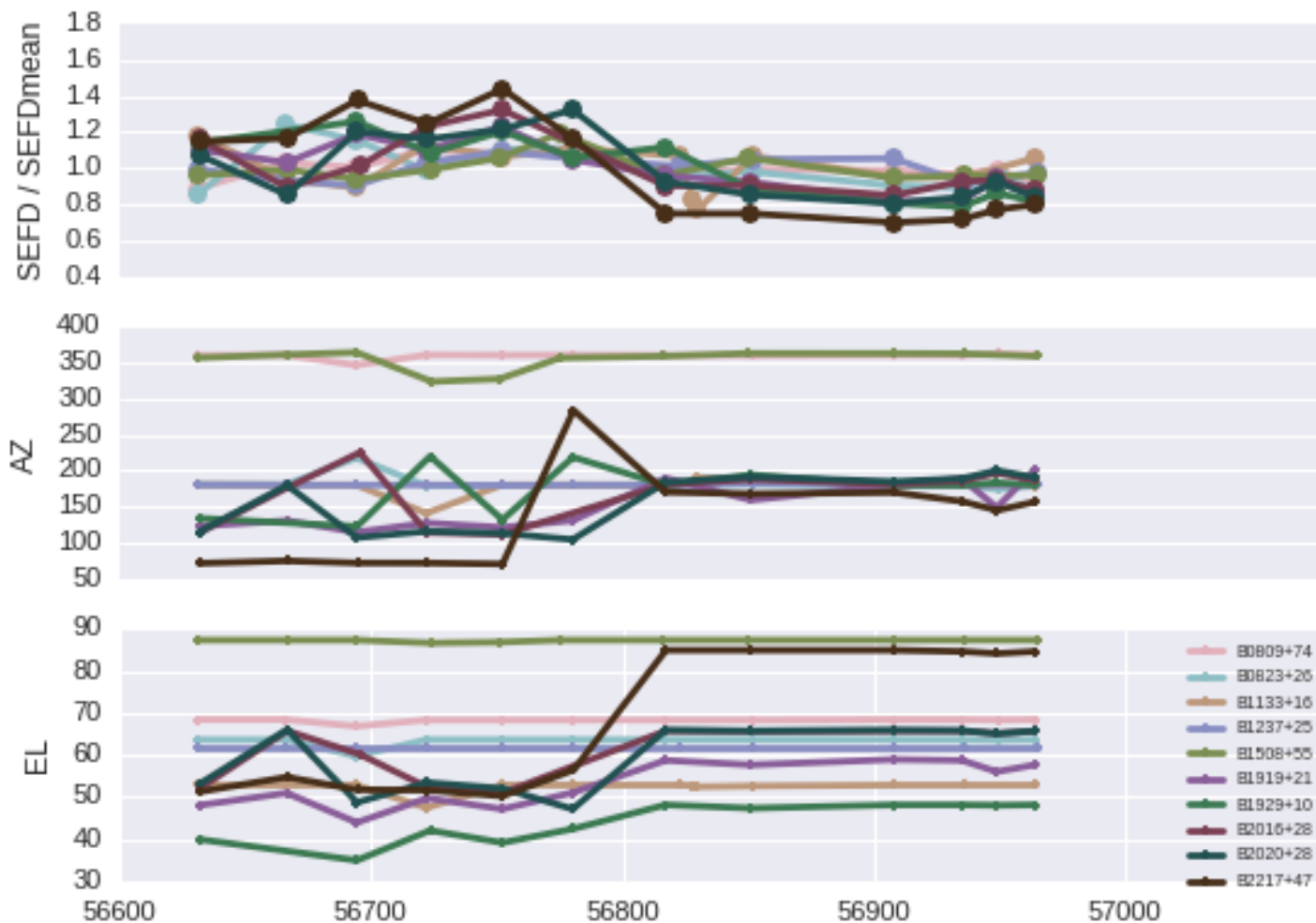


# Summary and further work:

- All beam models are not good (S/N doesn't reflect change in SEFD)
- For the same obs, beam models can predict up to 3 times different fluxes, depending on source elevation
- S/N of pulsars at different parts of the sky may correlate
- **«hamaker\_carozzi» model seems to be the most adequate beam model both for slow pulsars and MSPs**
- A single flux measurement of a strong pulsar integrated within HBA band has error of  $\sim 50\%$
- Flux errors are frequency-dependent
- MSSS fluxes (lower half of HBA band, band-integrated) agree with literature spectra to within 40%
- and to do:
  - Cobalt coherence tests (still have not done yet)
  - Flagged tiles info  $\rightarrow$  HDF5 BF metadata
  - Further calibration development, e.g. take into account contribution of the Galactic plane and background sources in FoV to Tsys
  - Extending/testing on LBA data

# Flux stability: SEFD wrt on-sky location

Beam model: arts

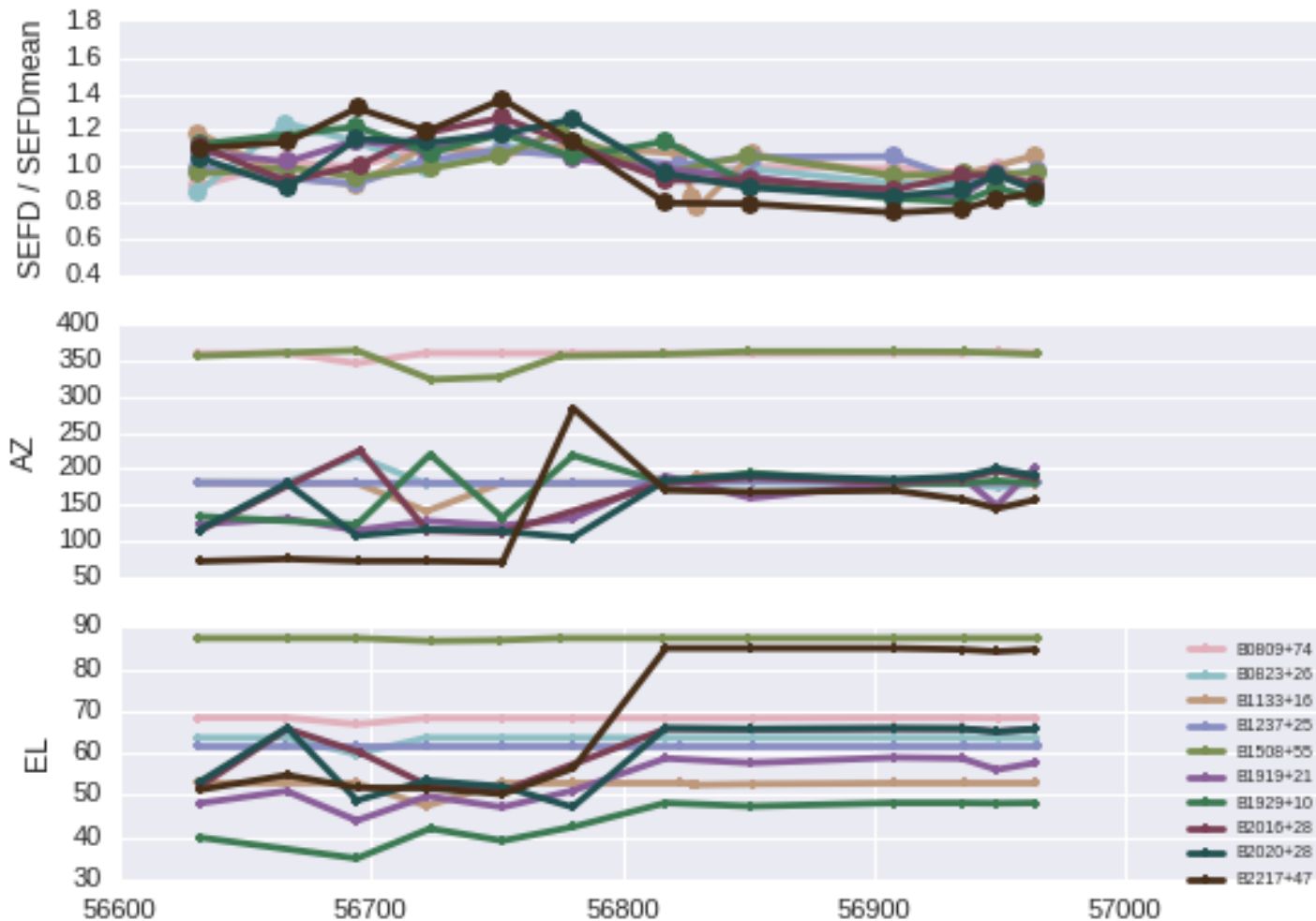


SEFD clearly depends on AZ/EL, as expected.

Are observed flux variations caused by imperfections of a beam model? Then we should see flux depending on pulsar sky position.

# Flux stability: SEFD wrt on-sky location

Beam model: arisN

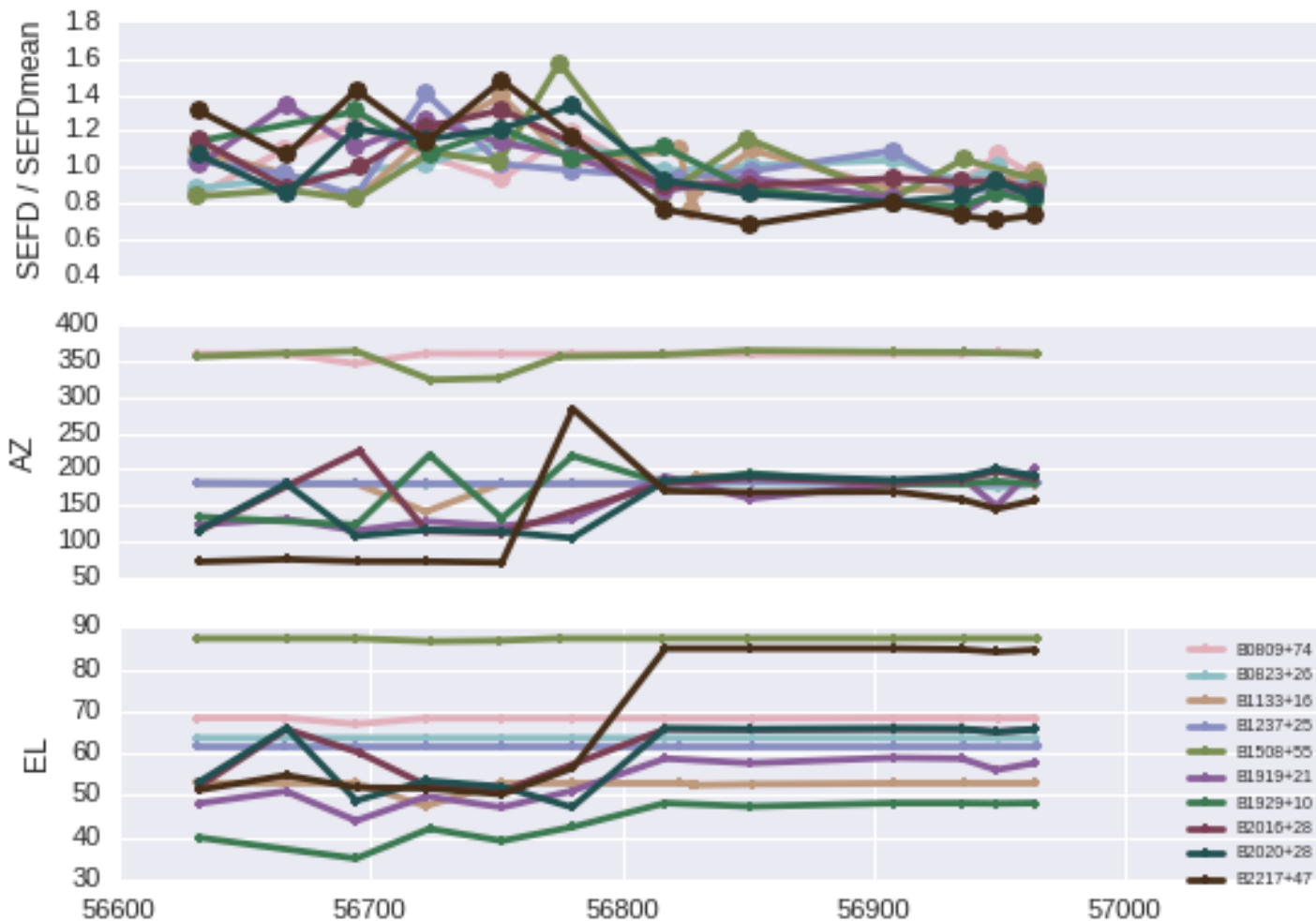


SEFD clearly depends on AZ/EL, as expected.

Are observed flux variations caused by imperfections of a beam model? Then we should see flux depending on pulsar sky position.

# Flux stability: SEFD wrt on-sky location

Beam model: hamaker\_carozzi

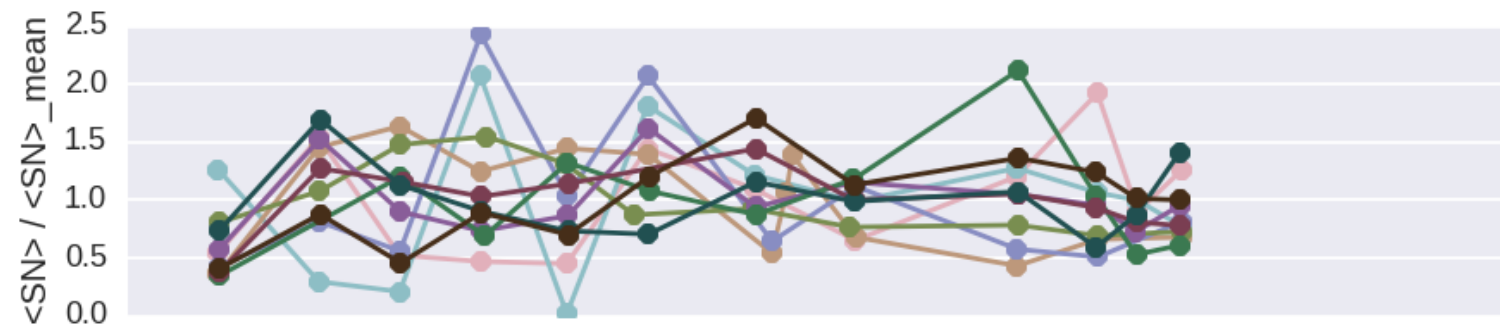


SEFD clearly depends on AZ/EL, as expected.

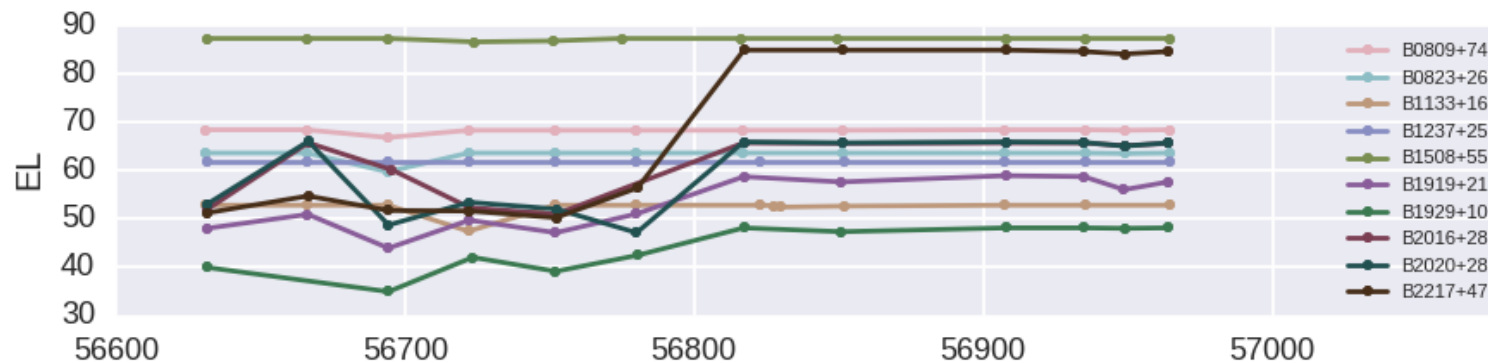
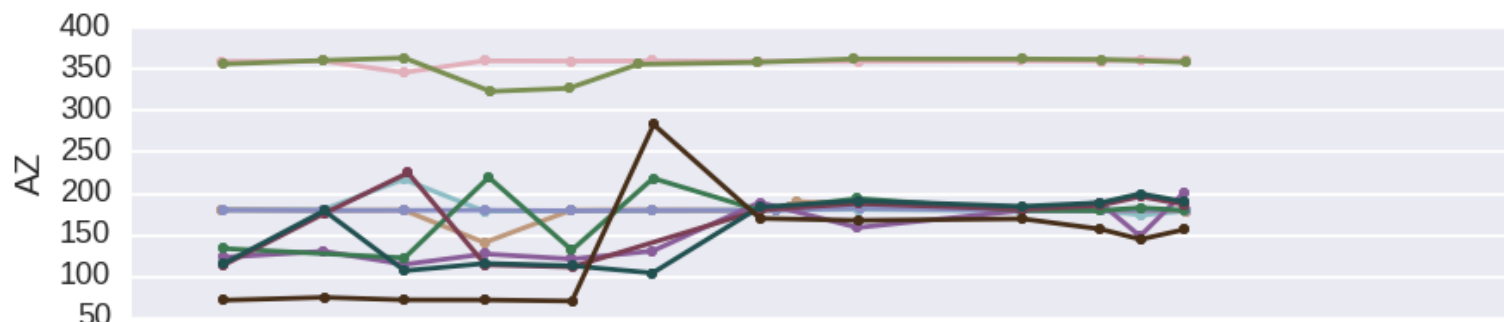
Are observed flux variations caused by imperfections of a beam model? Then we should see flux depending on pulsar sky position.

# Flux stability: phase-averaged S/N of profile

Beam model: arts

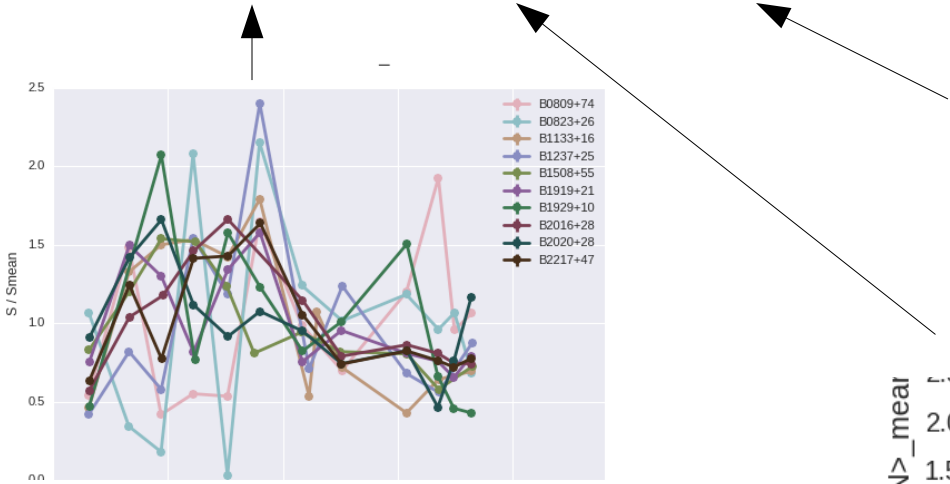


Same for other beam models (as was expected)

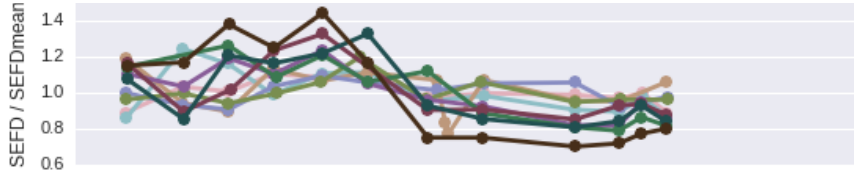


# Correlation of fluxes, S/Ns between different PSRs

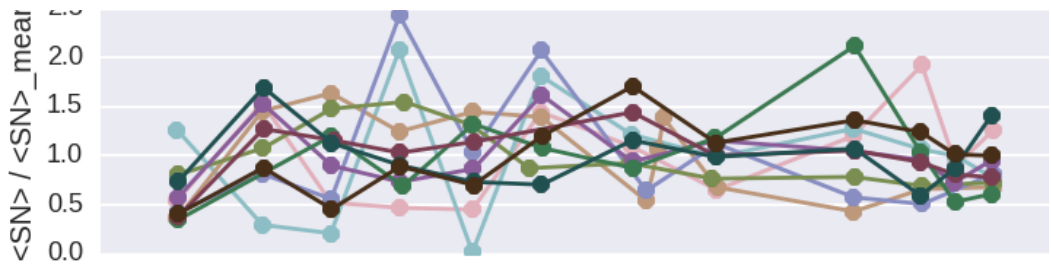
$$\text{Flux} = \text{S/N} * \text{SEFD}$$



Large (factor of 2) apparent variations), correlated between pulsars.



Depends on time, reflecting smoothly varying observing conditions (AZ/EL of a source). Dependence is similar for all three models



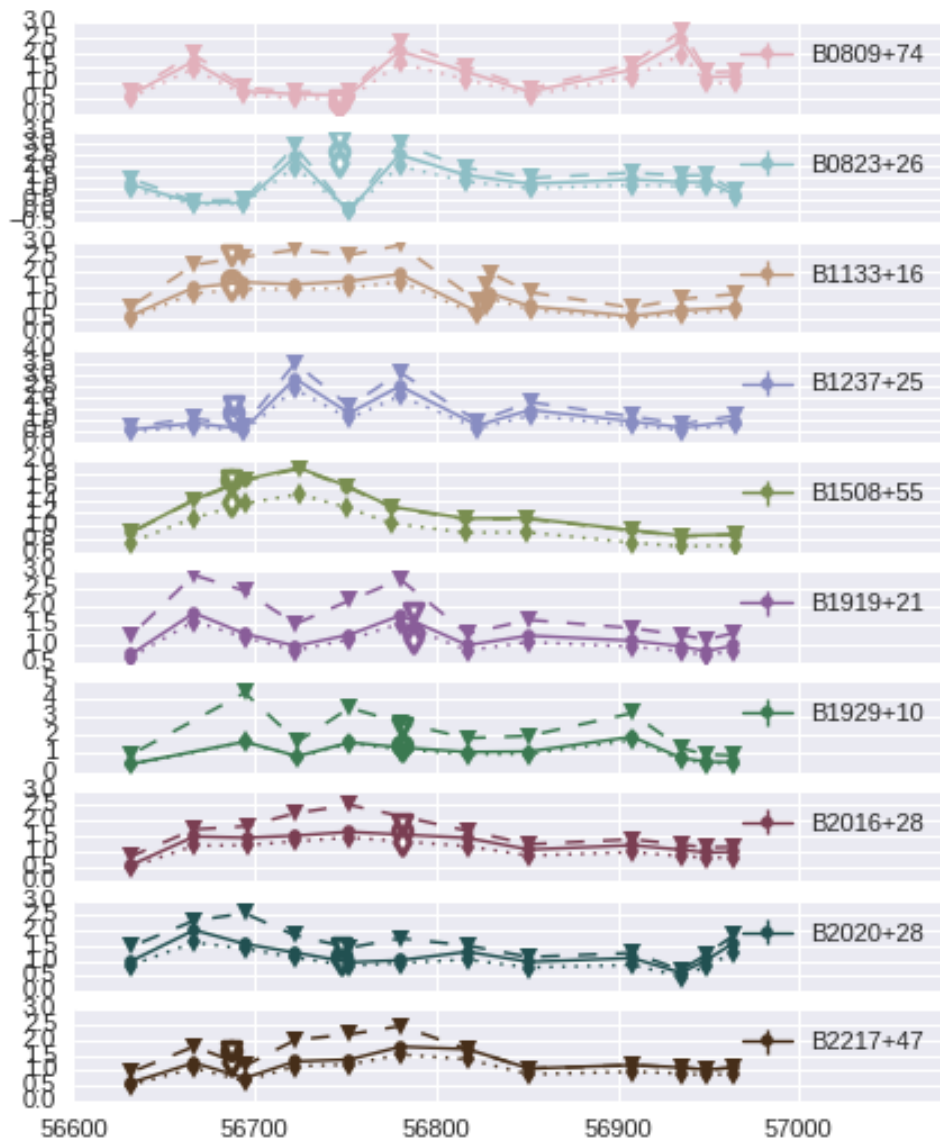
Varies by ~50%, much larger than predicted by RISS. Also is apparently slightly correlated between different pulsars (reflecting some perturbations in telescope setup/condition?..)

**Telescope gain has more complex dependence on sky coordinates than we can currently model. There may be also some long-scale temporal dependence of telescope parameters (resulting in correlated SNR changes), which are not reflected by current models.**

**These uncertainty causes observed flux to fluctuate within ~50%, thus a single observation cannot measure the flux better than that.**

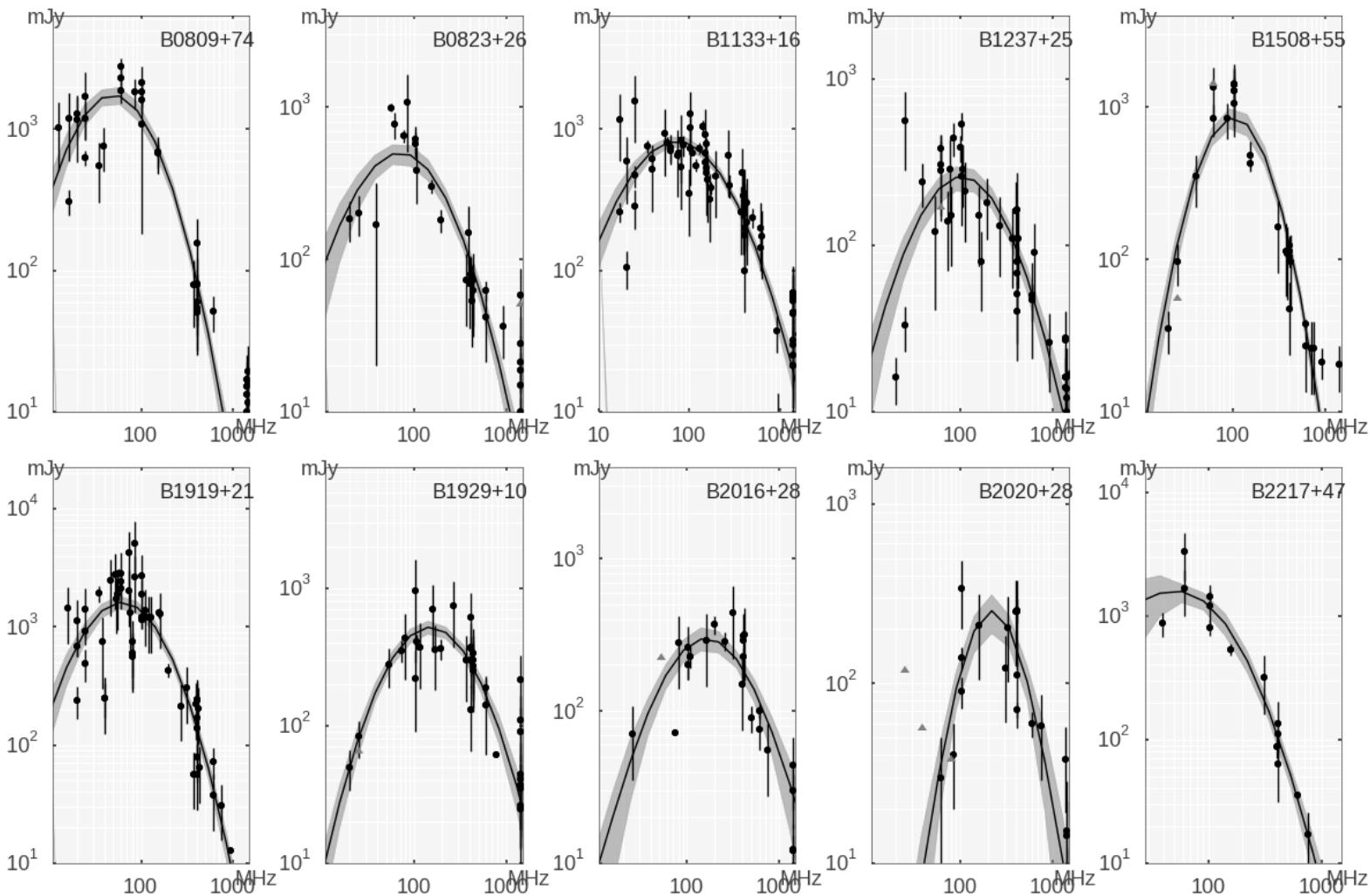
Flux/mean; o - arisN, d - arts,  
v - hamaker, white markers - census

# Comparing timing fluxes to Census fluxes



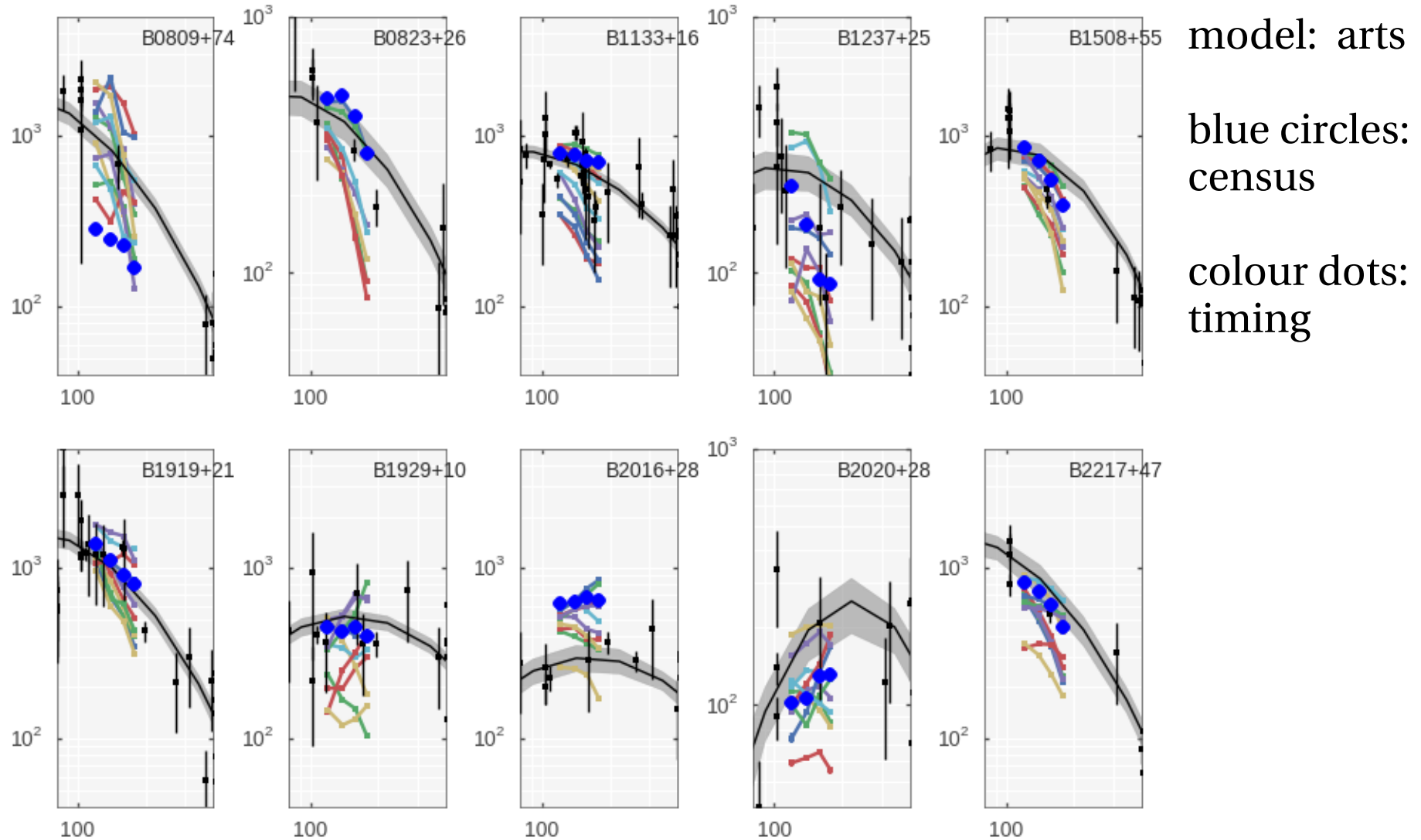
# Comparison to literature fluxes

MCMC parabola fit to the lit fluxes in 10 - 1000 MHz. MCMC gives **distributions** of fitted parameters. Parabolas with mean values of parameters (black line) and  $\pm 1$  sigma are shown (grey shade).

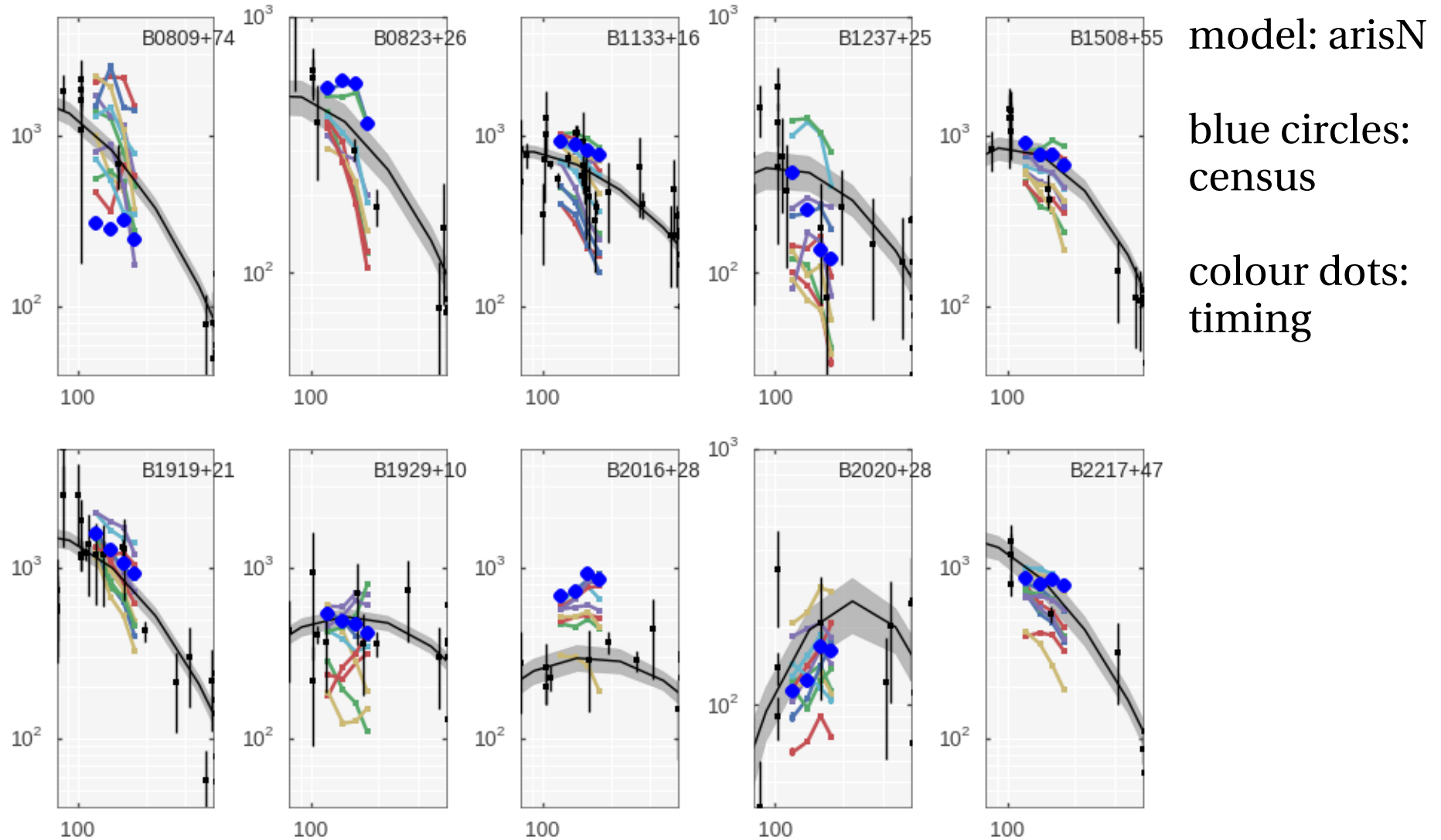




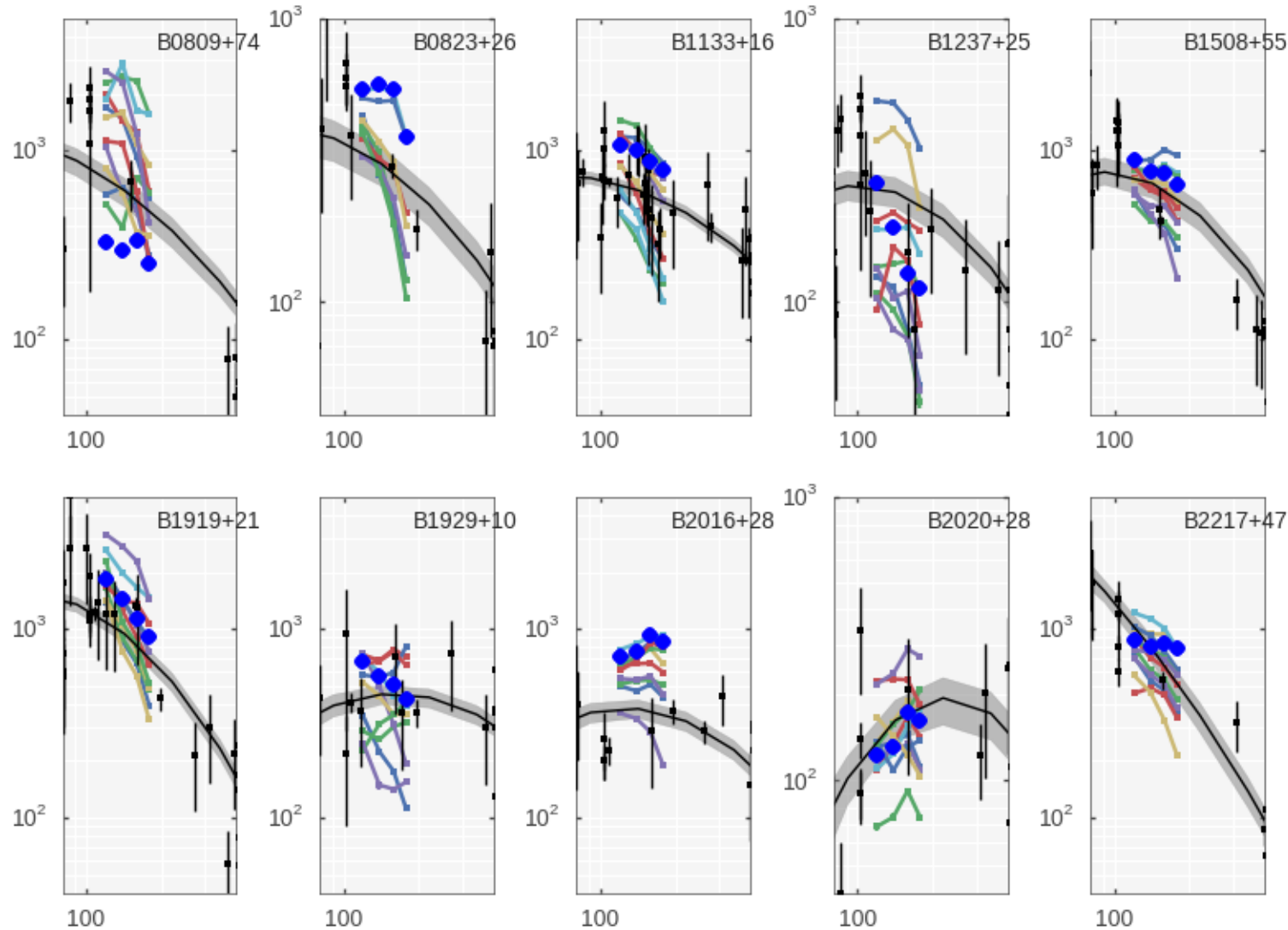
# Comparison to lit fluxes: three beam models



# Comparison to lit fluxes: three beam models



# Comparison to lit fluxes: three beam models



model:  
hamaker\_carozzi

blue circles:  
census

colour dots:  
timing

Fitted lines  
shifted because  
of new published  
flux points.

# Error distribution

For timing pulsars we can measure the distribution of  $K = S_r/S_o$ , the ratio of the real pulsar flux  $S_r$  to observed flux  $S_o$ .

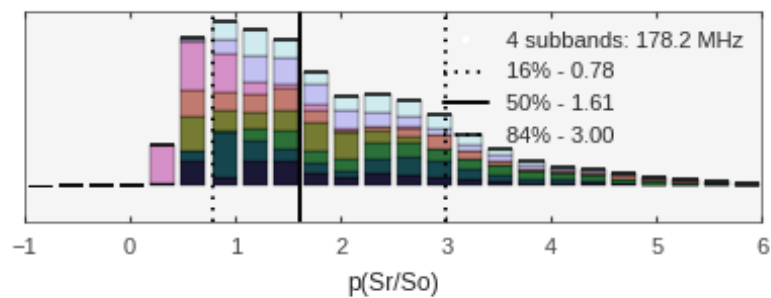
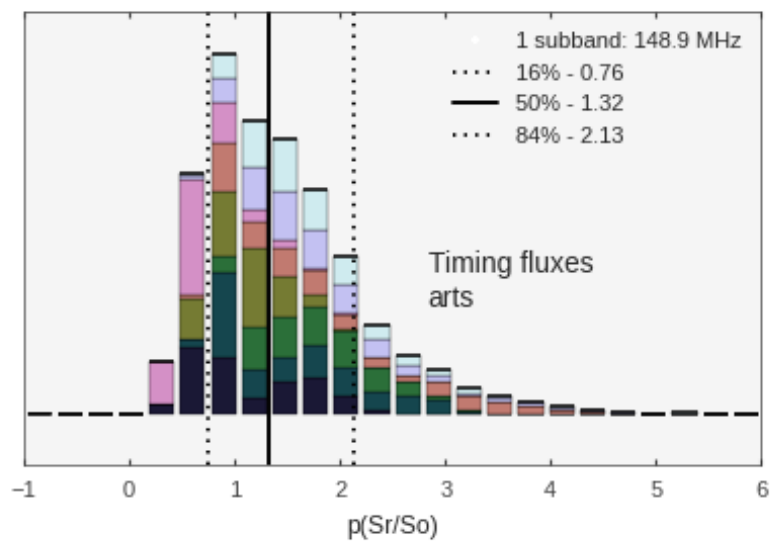
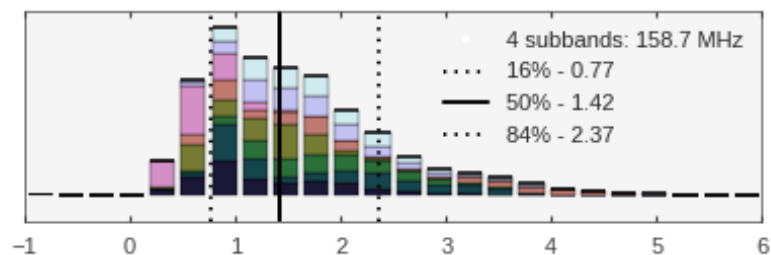
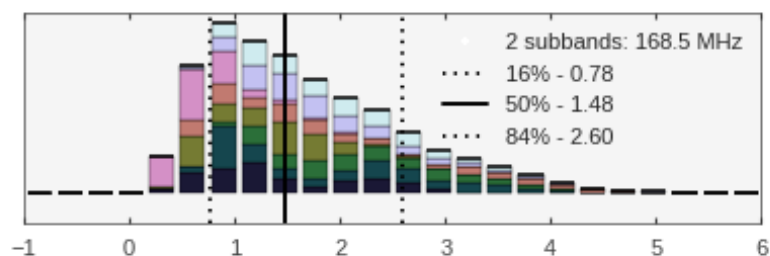
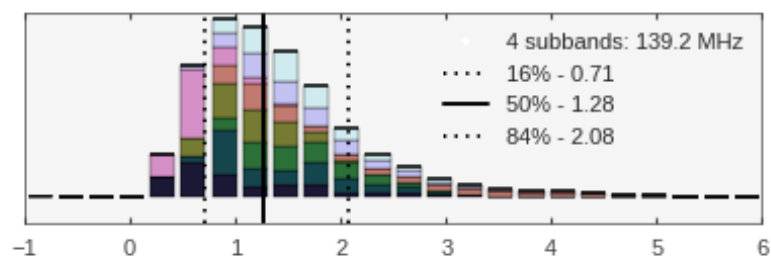
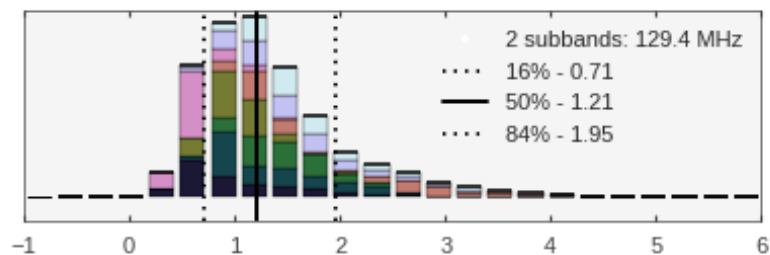
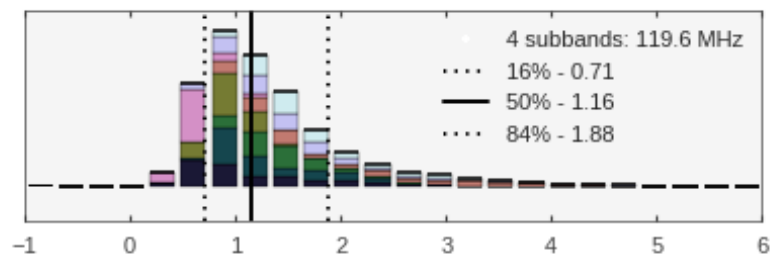
This distribution reflects our uncertainty about telescope parameters as well as ISM influence.

We assume that  $p(K)$  is the same for all pulsars regardless of their brightness.

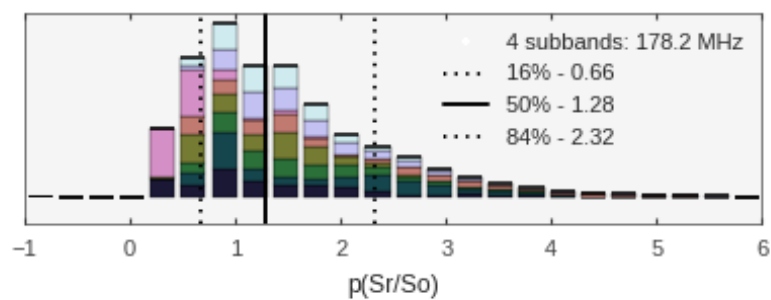
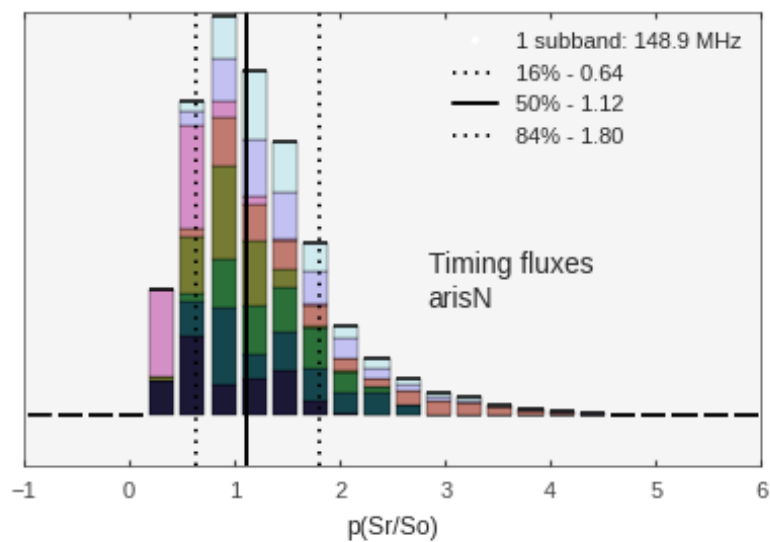
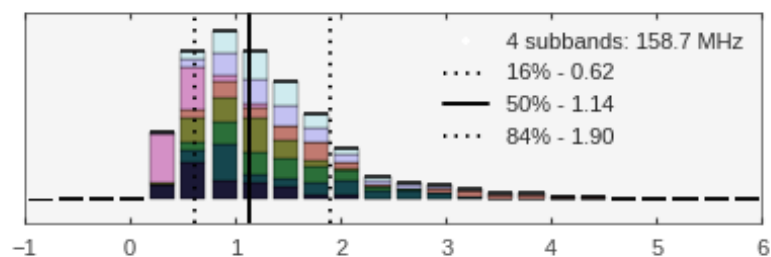
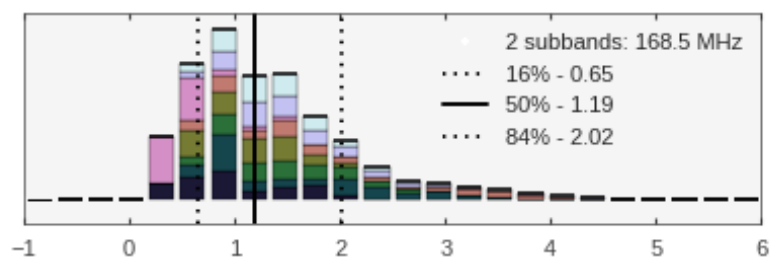
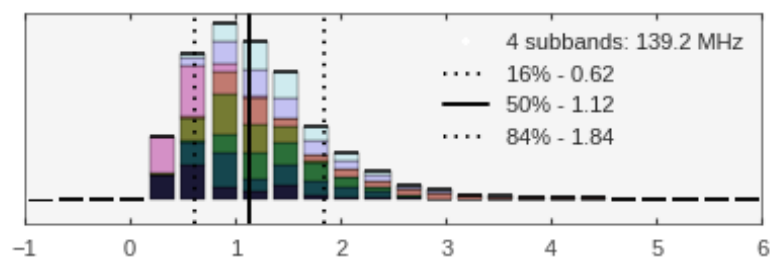
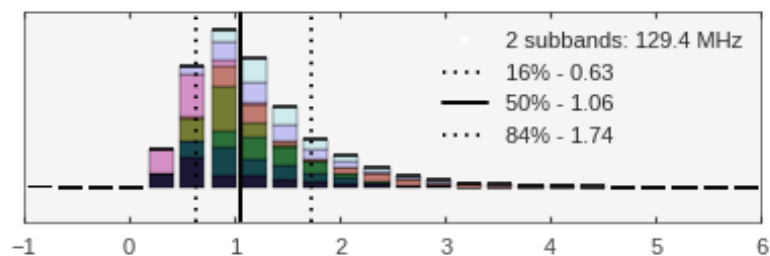
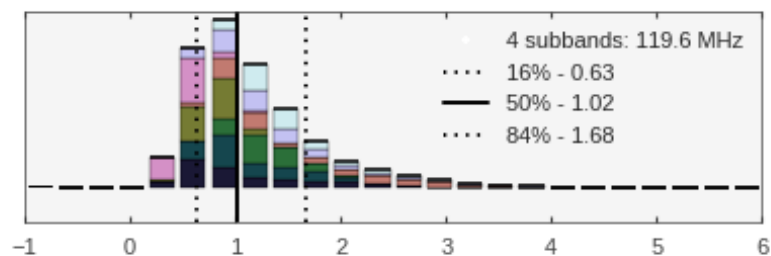
Then, for a single  $S_o$  measurement the probability of getting  $S_r=S_r$  (some fixed value) is  $p(S_r=S_r | S_o=S_o) = p(S_r=K*S_o | S_o) = p(K)$ .

For the histogram of  $K = S_r/S_o$ , we did not use a single value for  $S_r$ , but  $\sim 200$  values weighted with probabilities from MCMC fit.

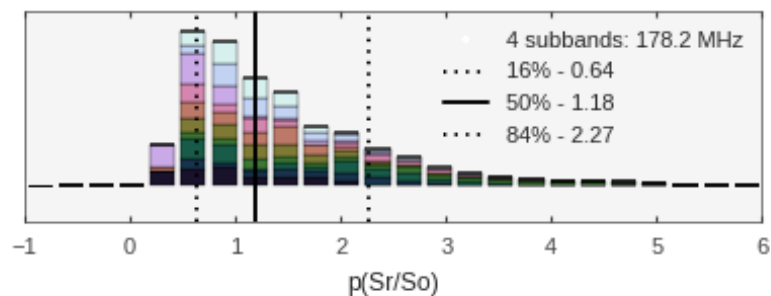
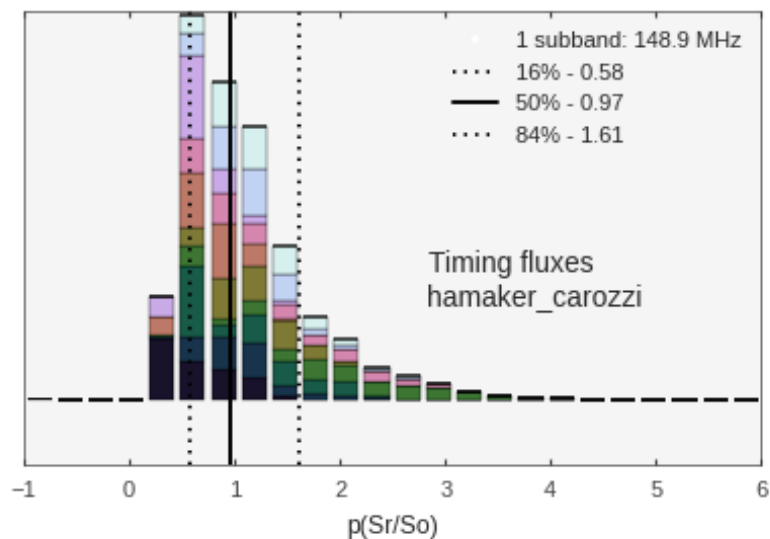
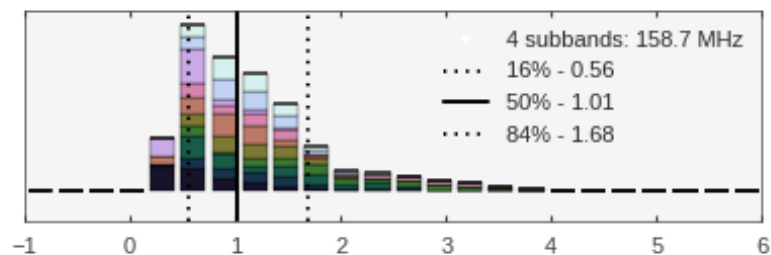
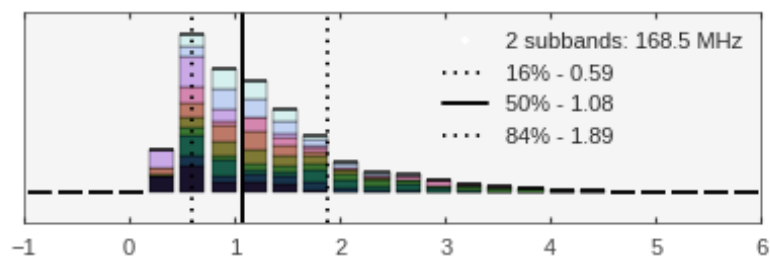
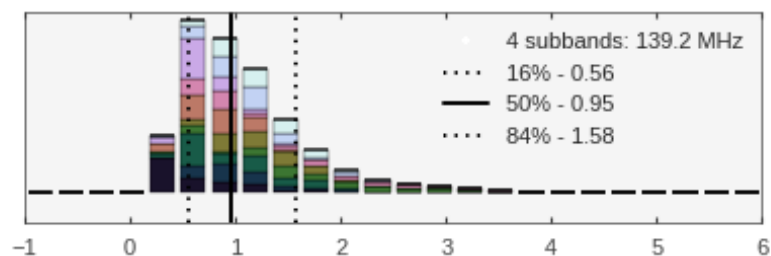
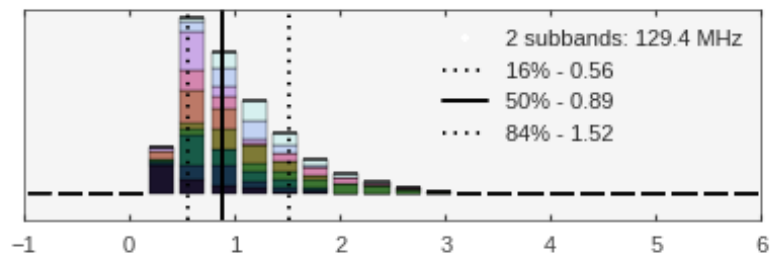
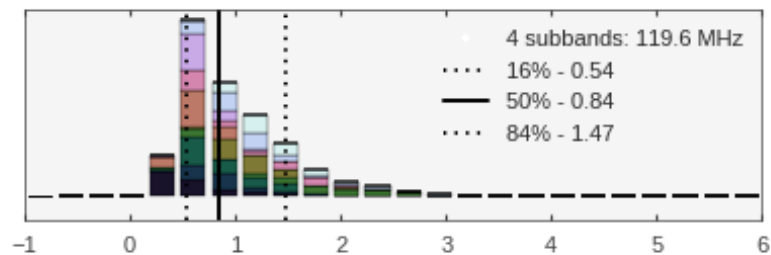
# Error distribution: arts



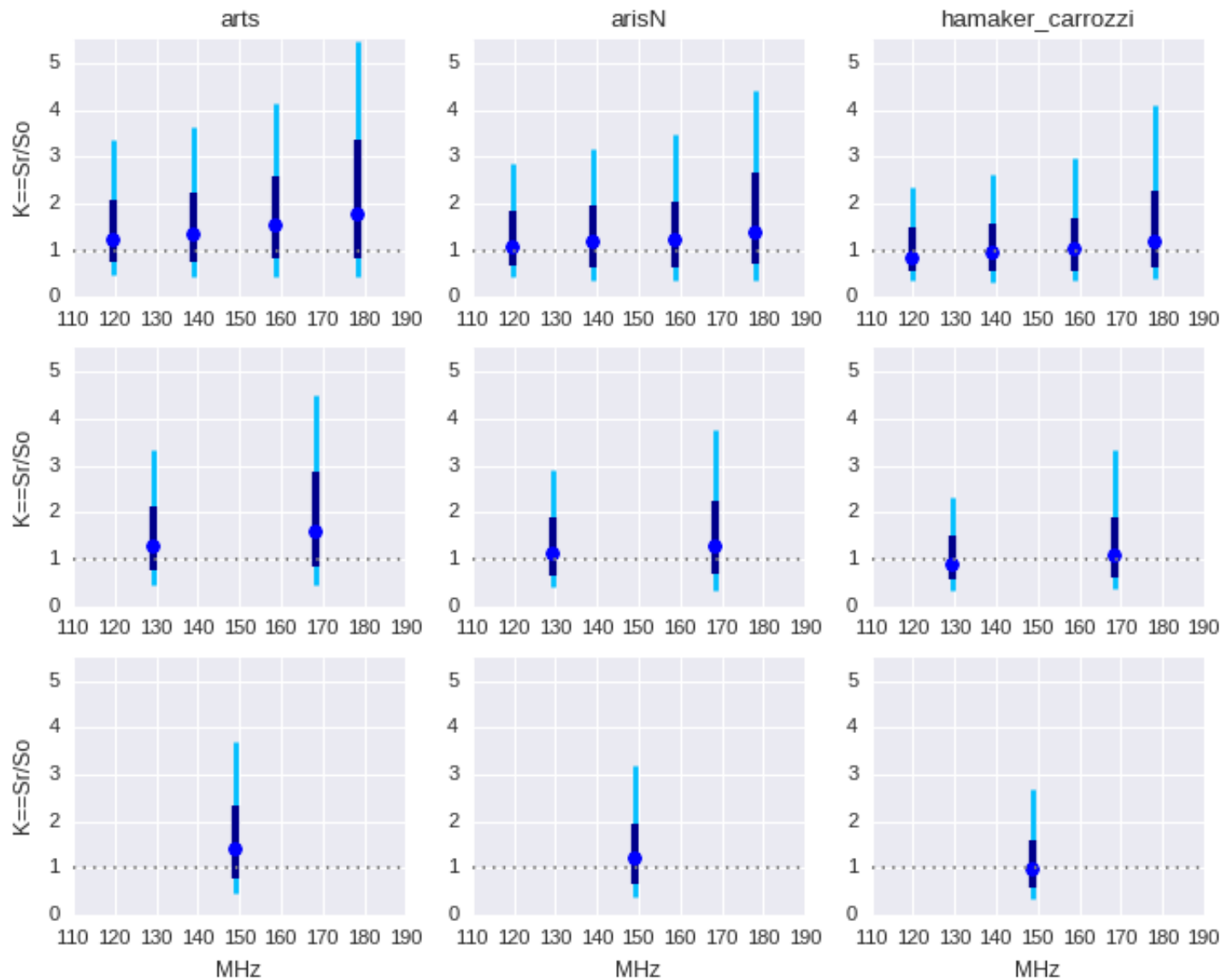
# Error distribution: arisN



# Error distribution: hamaker\_carozzi



# Error distribution: all three models

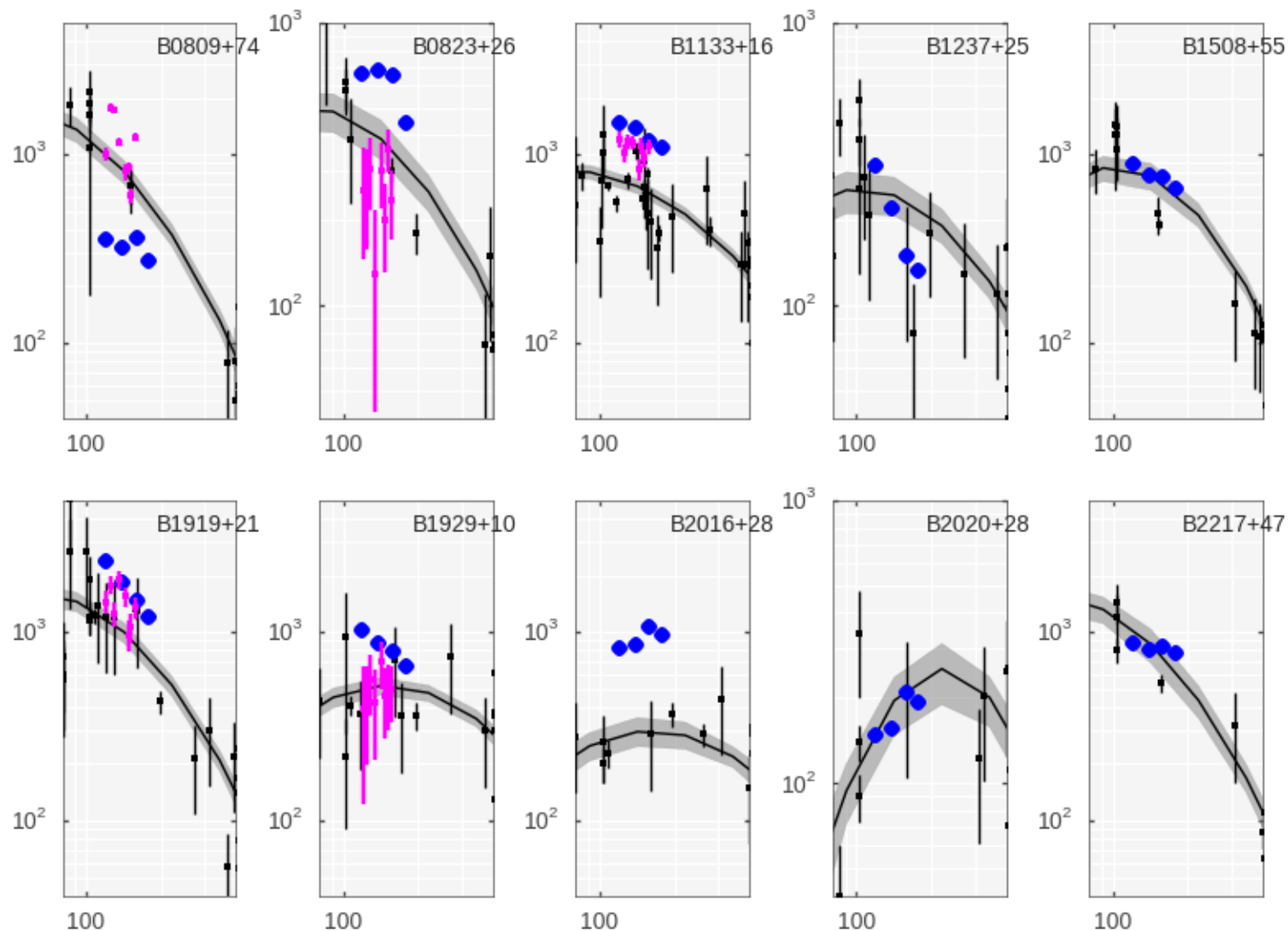


blue dot: median  
dark blue - 68%  
light blue - 95%

Best beam model,  
band-integrated  
flux: with 68%  
confidence real  
flux lies within  
~50% of measured



# MSSS fluxes

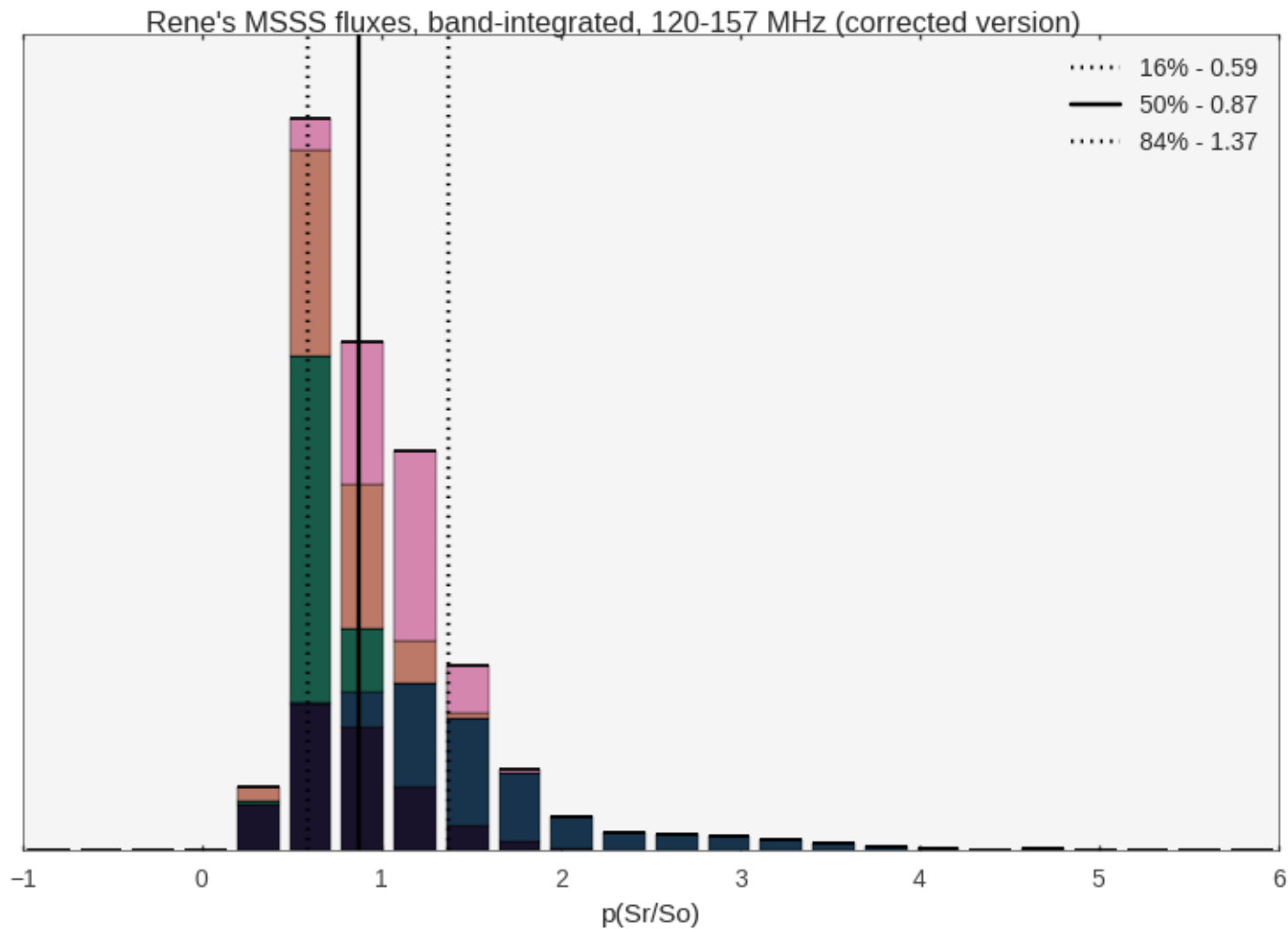


magenta - MSSS  
(from Rene Breton)

blue - census,  
hamaker\_carrozzi

# MSSS fluxes, band-integrated

Band-integrated  
flux: with 68%  
confidence real  
flux lies within  
40% of measured



# Fluxcal software

- `tsky.py` – Tsky (GL, GB, freq) or (RA, DEC, freq)
- `lofar_tinst.py` – T of the instrument (both HBA and LBA)  
    `--plot` – Tinst-vs-Freq diagnostic plot
- `lofar_gain.py` – Aeff (freq, EL) for a 48-tile station (HBA only)  
    `--plot` - diagnostic plots  
    `--model <arts | arisN >`. For hamaker\_carozzi beam model one can use corresponding function(s) after importing it as a module
- `snr.py` – calculate S/N using different methods (Q-Q probability plot, Off-pulse range, Polynomial to the baseline), so one can choose proper method and/or other parameters (fscrunching/bscrunching, off-pulse window) for flux calculation

# Fluxcal software (cont.)

- `lofar_psrflux.py` – to calculate flux density in mJy for a given PSRFITS file (ar-file). First tscrunching all observation (so, good only for not very long ones)
  - `--plot, --plot-saveonly` – diagnostic plots
  - `--spectrum=#NCHAN` – to produce calibrated spectrum for N output channels, and plot
  - `--spectrum-skip-first-channels=#INCHAN`
  - `--spectrum-skip-last-channels=#INCHAN`
  - `--model <arts | arisN | hamaker_carozzi>`
- `lofar_fluxcal.py` – to calibrate the samples in mJy in the PSRFITS file (or writes out new file). Calibrates separately individual sub-integrations. Can also calibrate different Stokes separately (thanks to Maciej).
  - `--model <arts | arisN | hamaker_carozzi>`
  - `--plot*` and `--spectrum*` options are also there

Both programs can read .h5 file to get number of stations. Unfortunately, info about the flagged tiles is not yet available for Beamformed data... Currently, this info can be obtained from Science Support and passed to a program via command-line option `--flagged`

# Other factors affecting flux measurements

- Scattering → hard to get S/N, it is underestimated
- Refractive scintillations.  
Can change pulsar flux by a factor of  $\sim 1.5$ . Need long-term monitoring program  
Diffractive scintillations is not a factor → averaged out,  $\Delta\nu_d < 0.2$  MHz
- Beam jitter by the ionosphere.  
Can be up to  $\sim 2$ -3 arcmins, i.e. half the Full-Core HBA TA beam (at half maximum)
- Variation of Tsys with time due to rise/set of the Galactic plane (up to 30-40% when Galactic plane is in the FoV) and other strong background sources.  
Also with pointing direction due to noise coupling effects.

Despite these factors:

- We've got  $\sim 20\%$  agreement with EOR data for the new LOFAR pulsar J0815+4611
- Flux estimates from the MSSS images (Rene Breton) for several MSPs — on average there is an agreement within  $\sim 40\%$

# Summary and further work:

- All beam models are not good (S/N doesn't reflect change in SEFD)
- For the same obs, beam models can predict up to 3 times different fluxes, depending on source elevation
- S/N of pulsars at different parts of the sky may correlate
- **«hamaker\_carozzi» model seems to be the most adequate beam model both for slow pulsars and MSPs**
- A single flux measurement of a strong pulsar integrated within HBA band has error of  $\sim 50\%$
- Flux errors are frequency-dependent
- MSSS fluxes (lower half of HBA band, band-integrated) agree with literature spectra to within 40%
- and to do:
  - Cobalt coherence tests (still have not done yet)
  - Flagged tiles info  $\rightarrow$  HDF5 BF metadata
  - Further calibration development, e.g. take into account contribution of the Galactic plane and background sources in FoV to Tsys
  - Extending/testing on LBA data



# Arts et al. beam model

«AKW» model by Arts M., Kant G., & Wijnholds S. (2013)

- 1st version of the improved Hamaker model (2006) → BBS
- Provides full EM simulations of a 24-tile HBA sub-station, including edge effects and grating lobes (Hamaker's model is based on an infinite array of elements)
- Flux values with both models agree with a factor of  $\sim 1.5$  for most of the MSPs

AKW model →  $A_{\text{eff}}$  for a given frequency range, AZ, and EL

In practice →

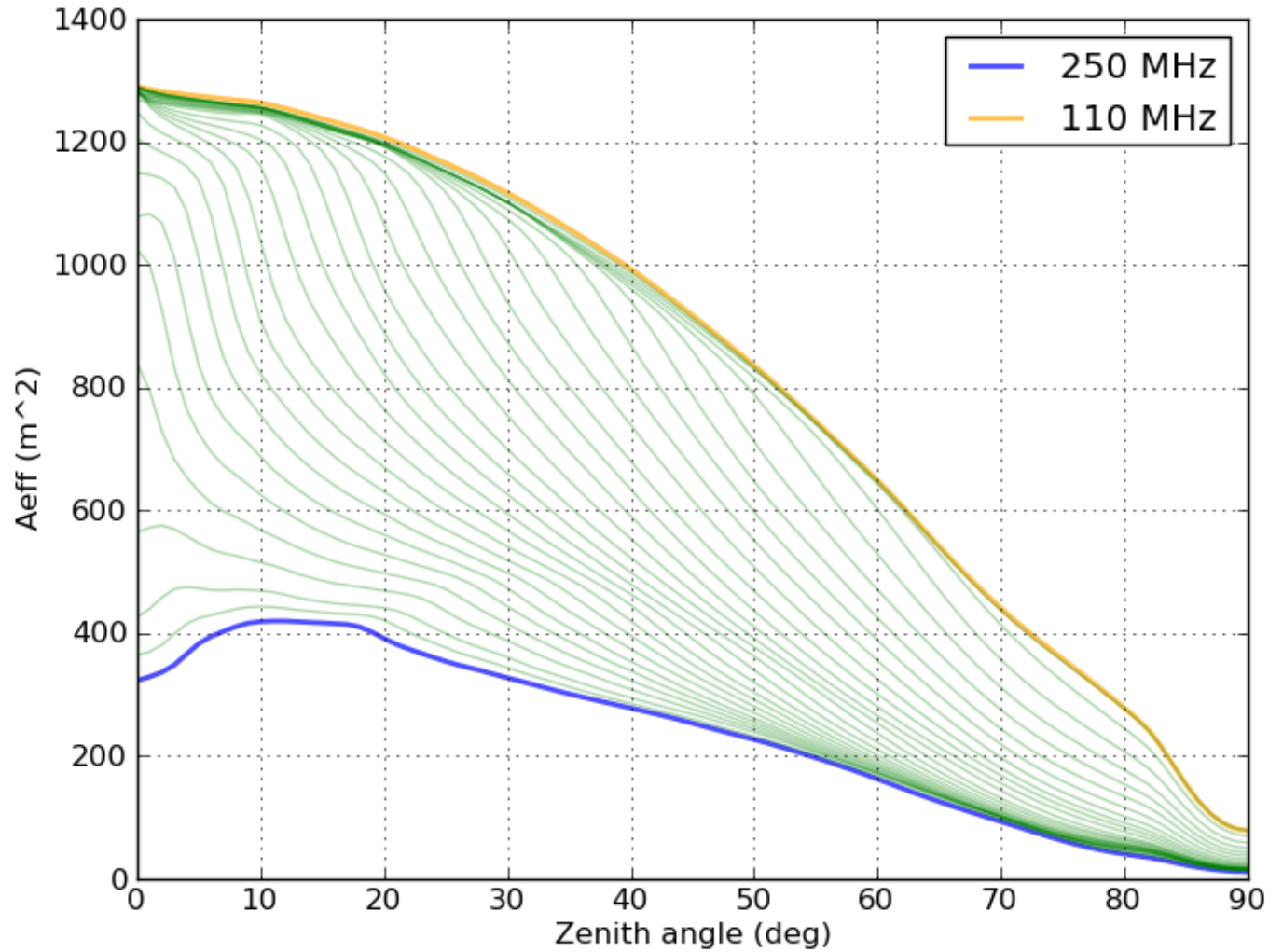
Table of 91 ELs \* 361 AZs \* 29 frequencies

- AZ, 0 — 360 deg, 1-deg step
- EL, 0 — 90 deg, 1-deg step
- Frequency, 110 — 250 MHz, 5-MHz step

Note! When calibrating, for a given EL  $A_{\text{eff}}$  is averaged over all azimuths, as the stations are randomly rotated.



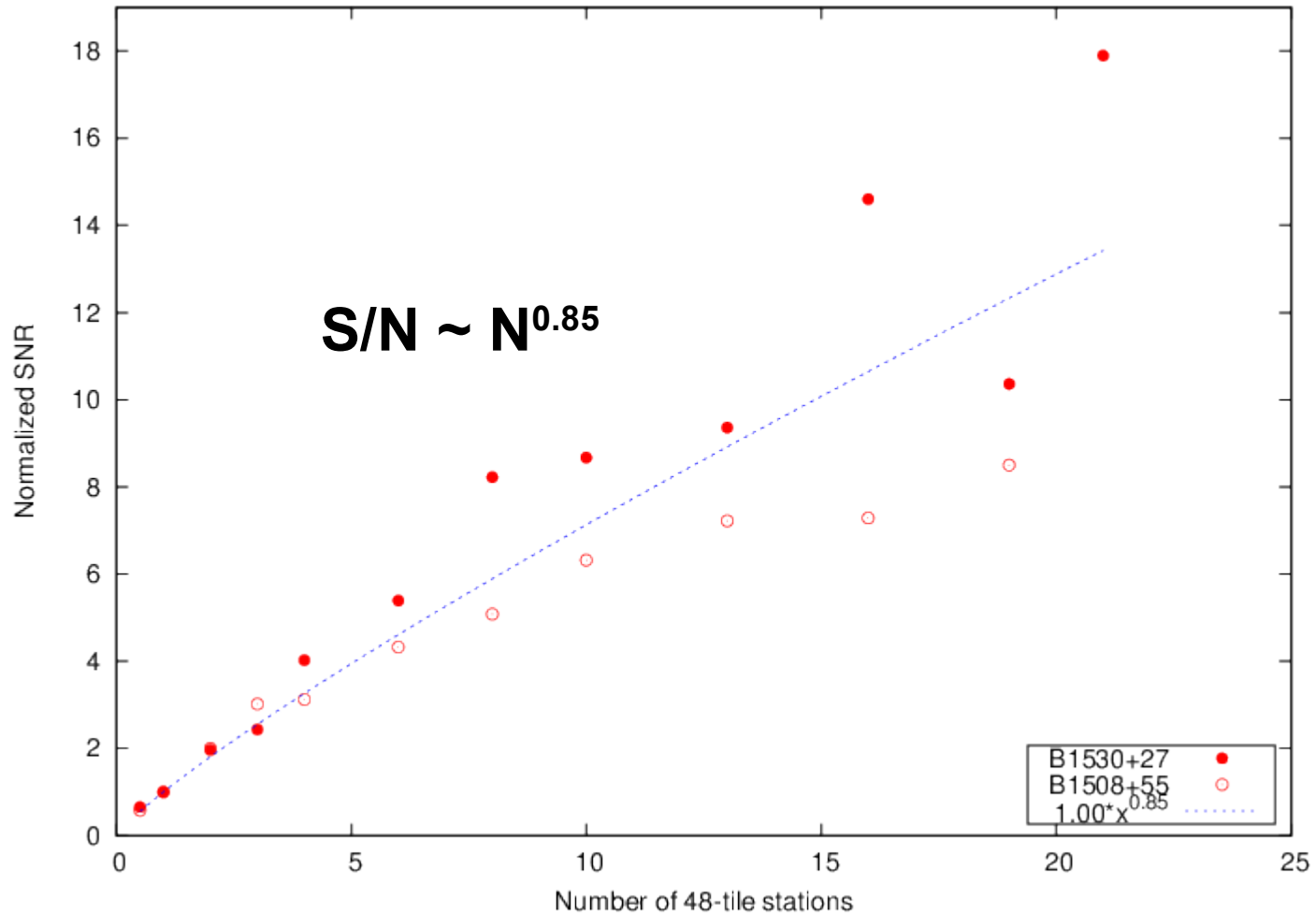
# Aeff vs. ZA



one 48-tile station

# Coherence scaling

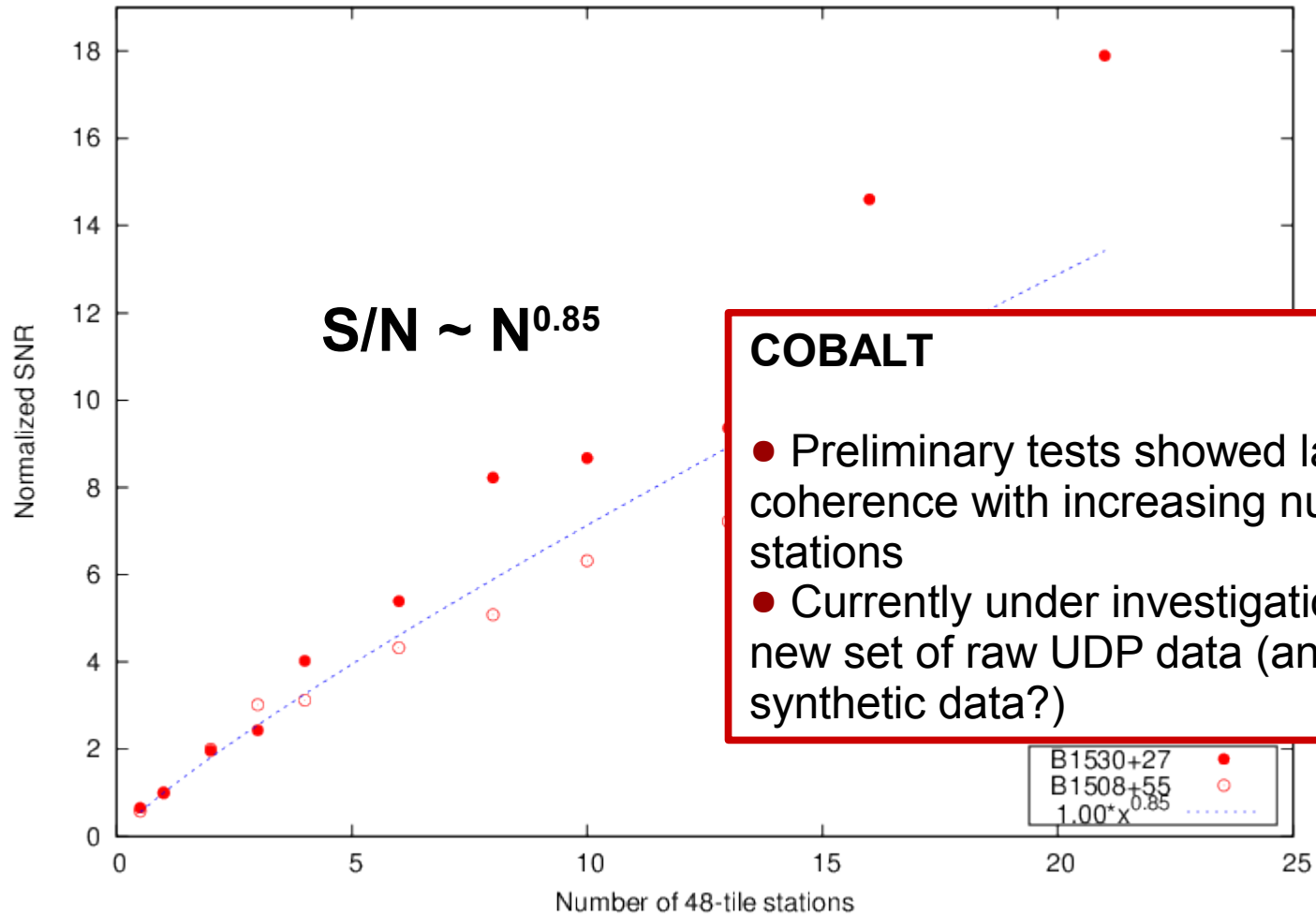
BG/P  
data



N – number of 48-tile stations

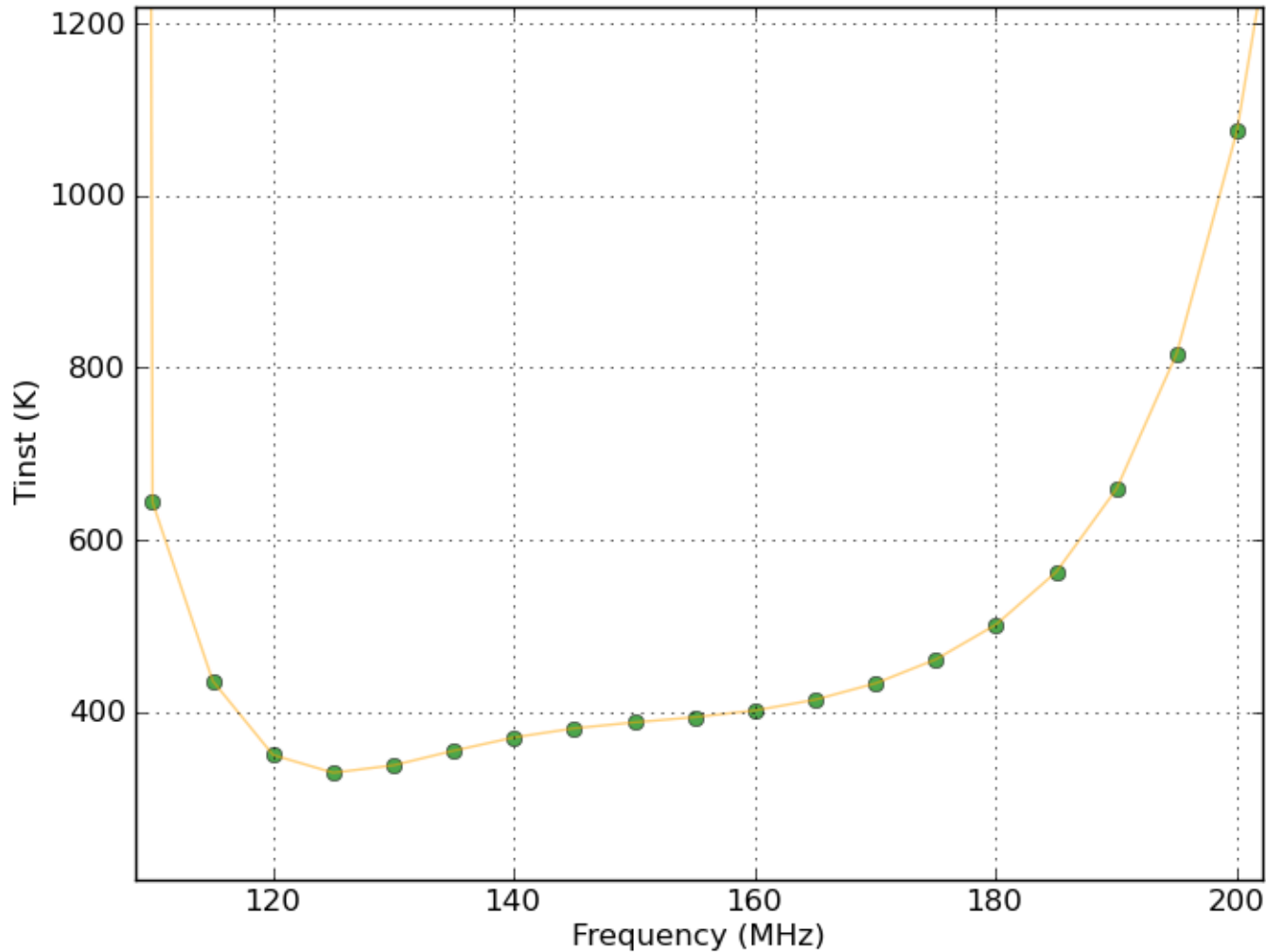
# Coherence scaling

BG/P  
data



N – number of 48-tile stations

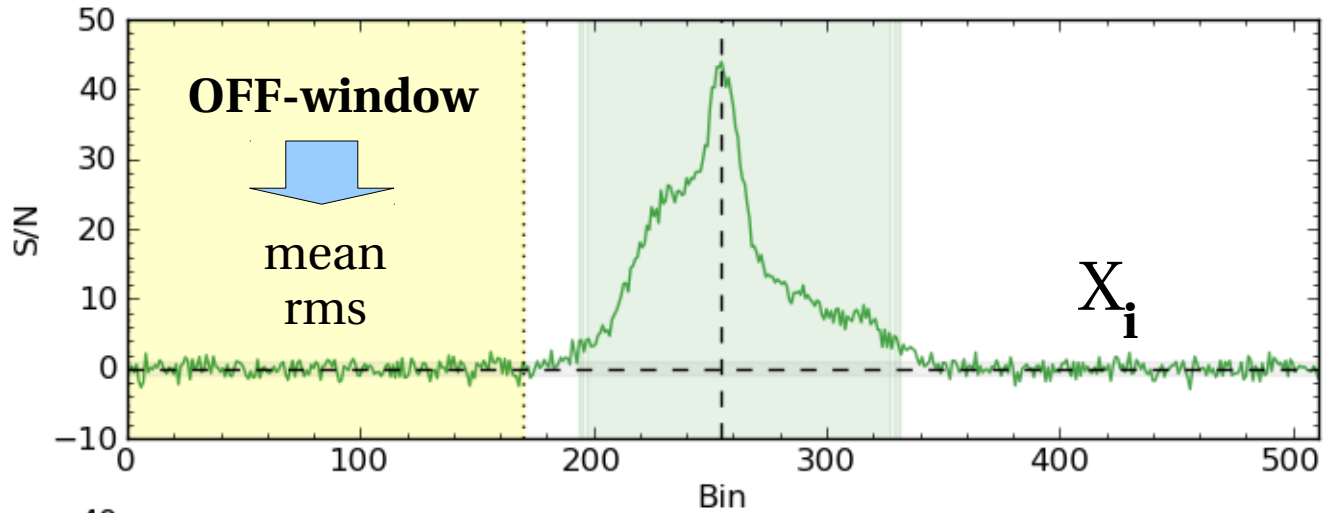
# Instrumental temperature, $T_{\text{inst}}$



6th order polynomial  
function of the frequency  
based on CasA  
measurements

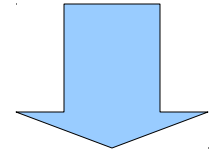
Wijnholds &  
van Cappellen  
(2011)

# Pulsar profile, S/N



$$(S/N)_i = (X_i - \text{mean}) / \text{rms}$$

i — profile bin



$$\text{Flux}_i = (S/N)_i * \text{SEFD}$$

