

In the beginning of the Dark Ages, electrically neutral hydrogen gas filled the universe. As stars formed, they ionized the regions immediately around them, creating bubbles here and there. Eventually these bubbles merged together, and intergalactic gas became entirely ionized.

# The epoch of reionization from 21 cm observations



Jonathan Pritchard

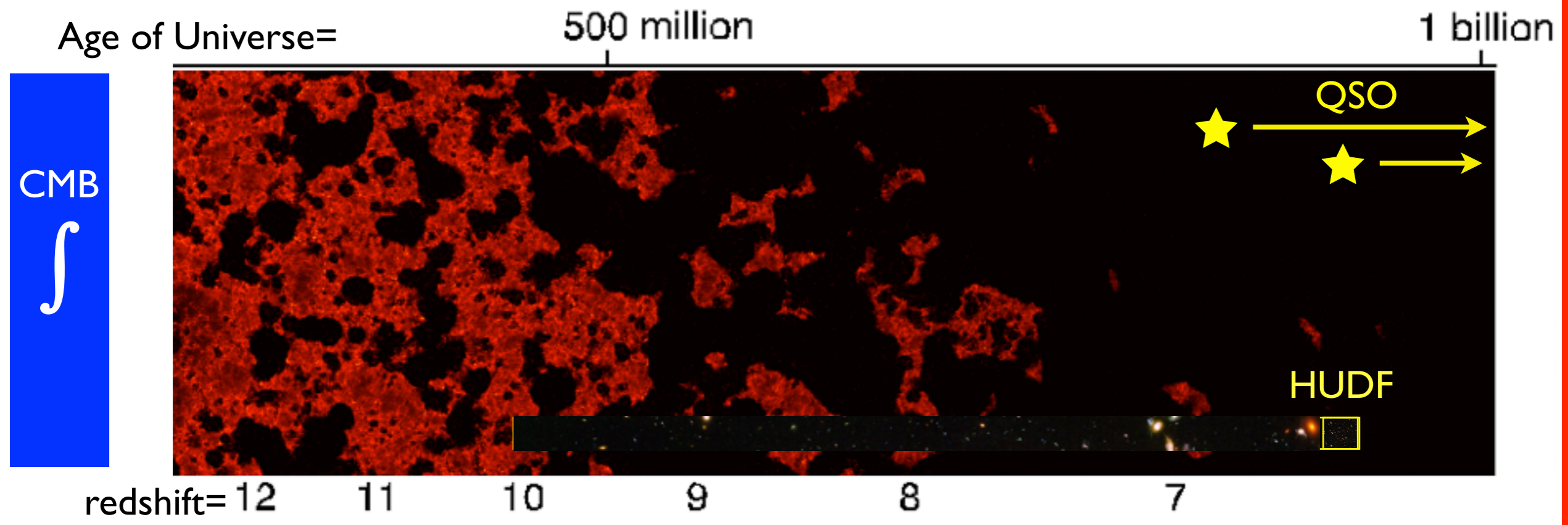
Imperial College  
London







# More needed...



Existing observations leaves much unanswered:

- 1) Lyman-alpha forest: end point  $z > 6.5$
- 2) CMB optical depth: mid point  $z \sim 9 \pm 1.5$
- 3) kSZ amplitude: duration  $z < 3$  ?

HST probes skewer much smaller than scale of ionized regions + only brightest sources

LAE surveys (e.g. HSC) may eventually show enhanced clustering from reionization

LBG/LAE surveys with Euclid possible to  $z \sim 8$  in deep field

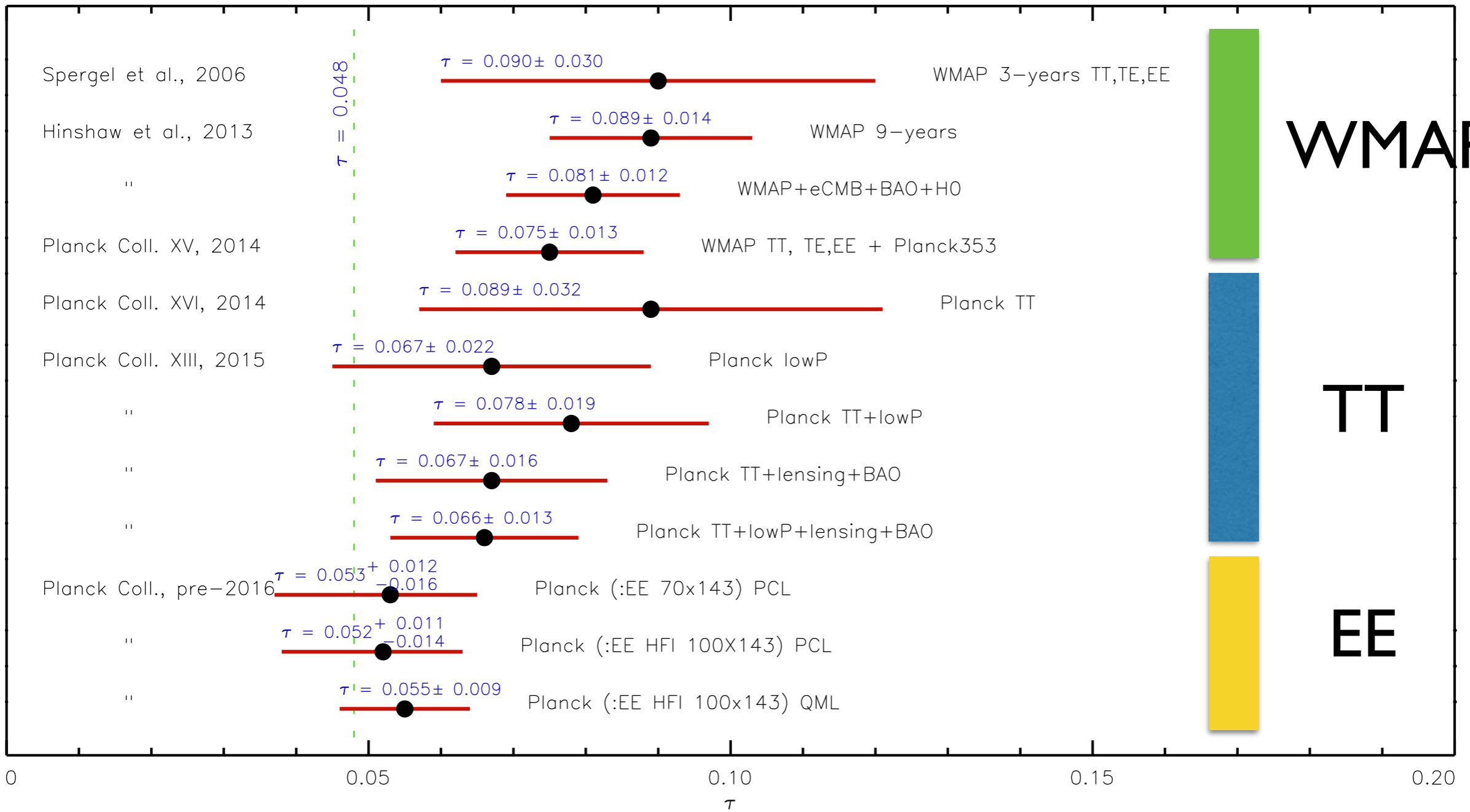
Fundamental need for new types of observation to understand details of reionization



# Evolving optical depth

Planck+ 2016

$$\tau = \sigma_T \int \bar{n}_e(z) \frac{dl}{dz} dz,$$



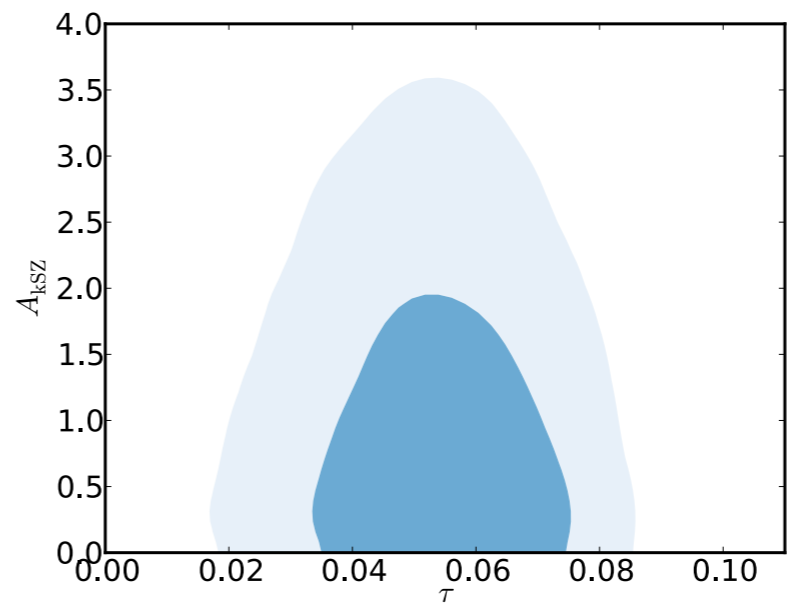
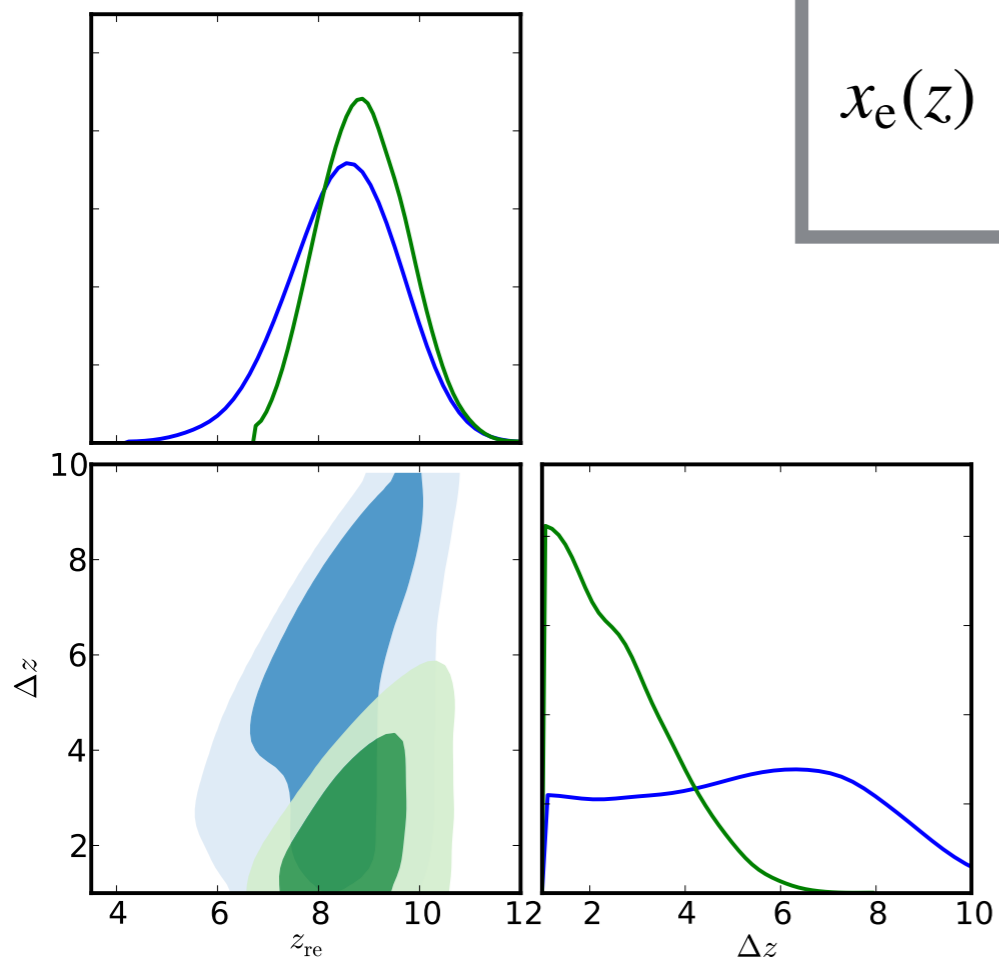
tau has fallen consistently as systematics better accounted for



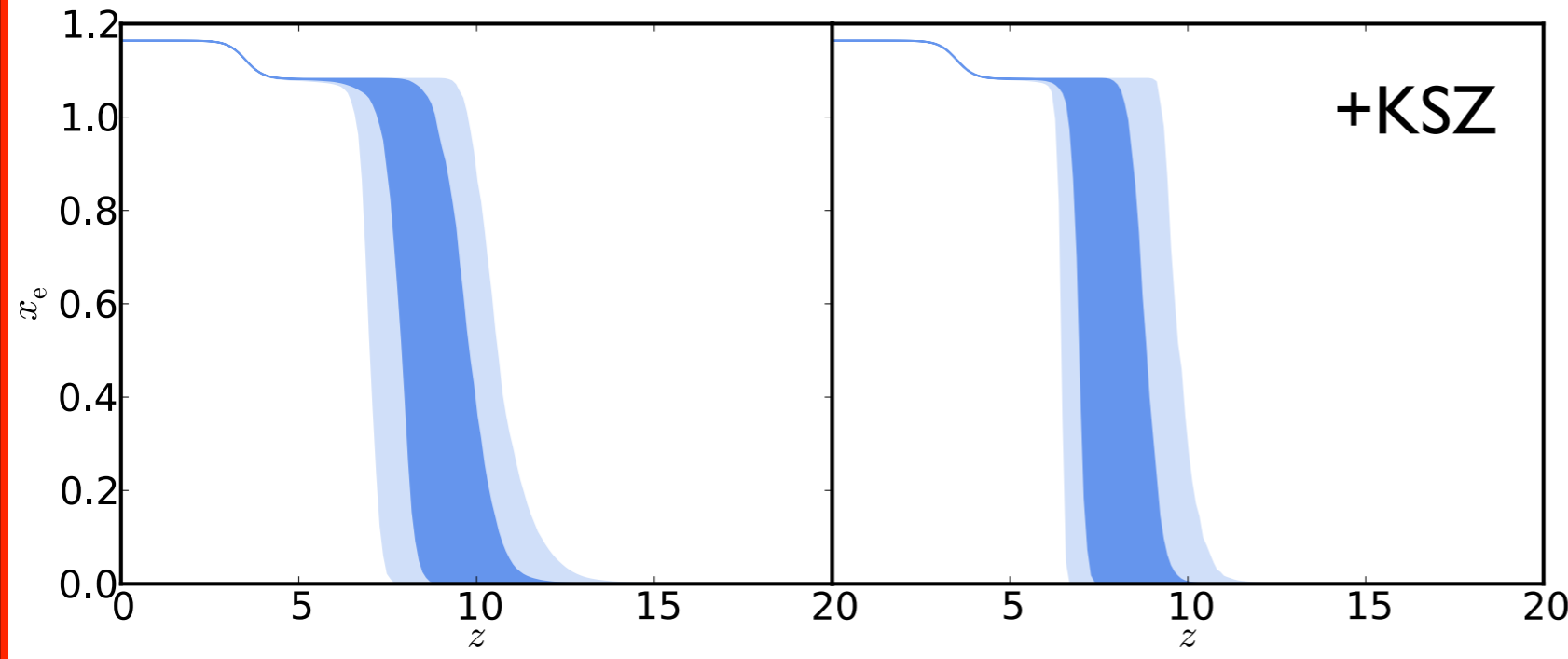
# Planck

Planck+ 2016

$$x_e(z) = \frac{f}{2} \left[ 1 + \tanh \left( \frac{y - y_{re}}{\delta y} \right) \right]$$



KSZ can be included to constrain  $\Delta z$



**tau alone**

$z_{re} = 8.8^{+0.9}_{-0.9}$  (prior  $z_{end} > 6$ ).

$\Delta z < 4.6$  (95 % CL).

**tau + KSZ**

$z_{re} = 7.8^{+1.0}_{-0.8}$  (prior  $z_{end} > 6$ ),

$\Delta z < 2.8$  (95 % CL, prior  $z_{end} > 6$ ).

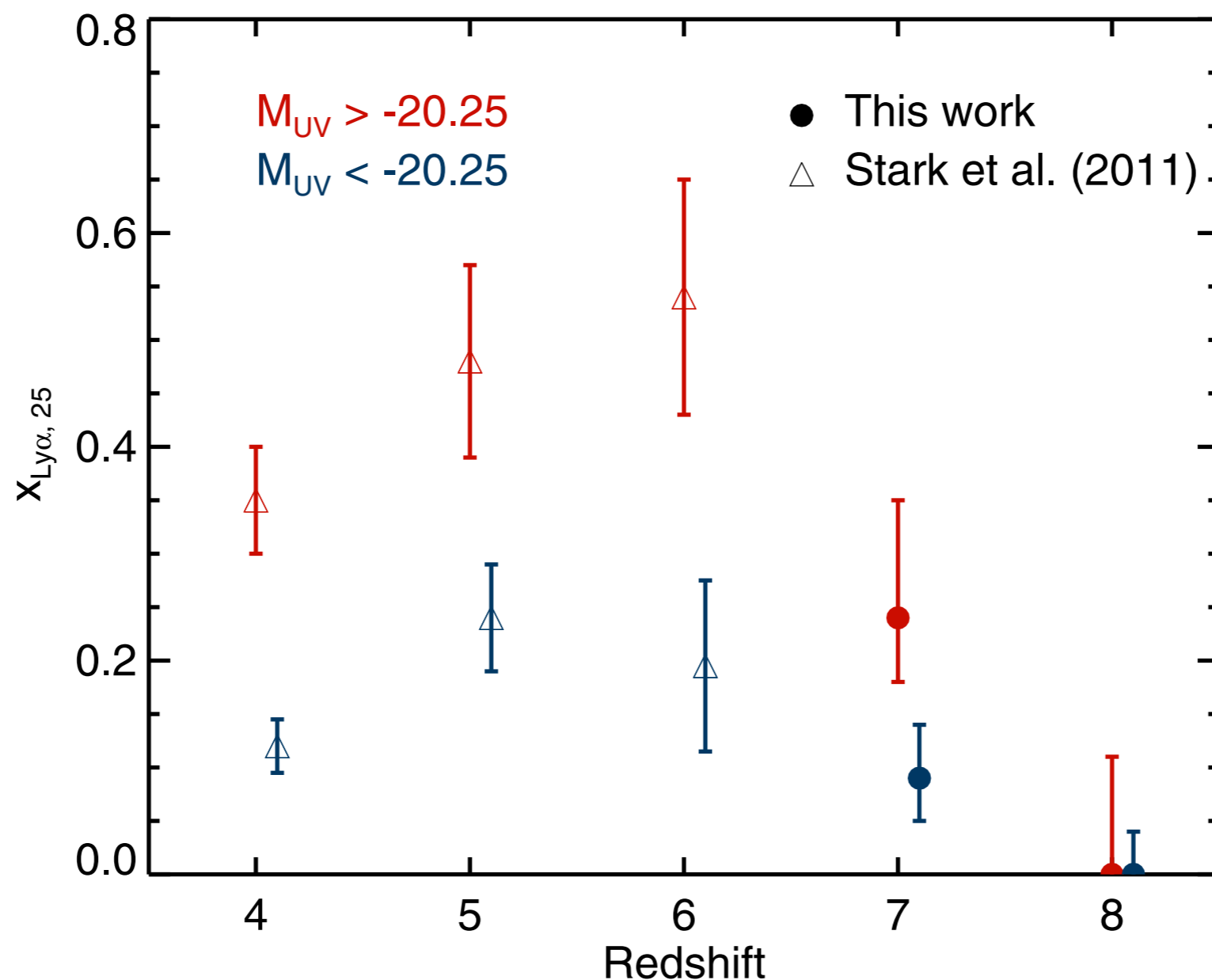




LBG detected up to  $z \sim 10$ . Small numbers at  $z > 7$ . JWST launches 2018

Decline in LAE/LBG fraction at  $z \sim 7$  possible signature of reionization

$$x_{\text{HI}} = 0.39^{+0.08}_{-0.09} \text{ at } z \sim 7 \text{ and } x_{\text{HI}} > 0.64 \text{ at } z \sim 8.$$



Schenker+ 2014



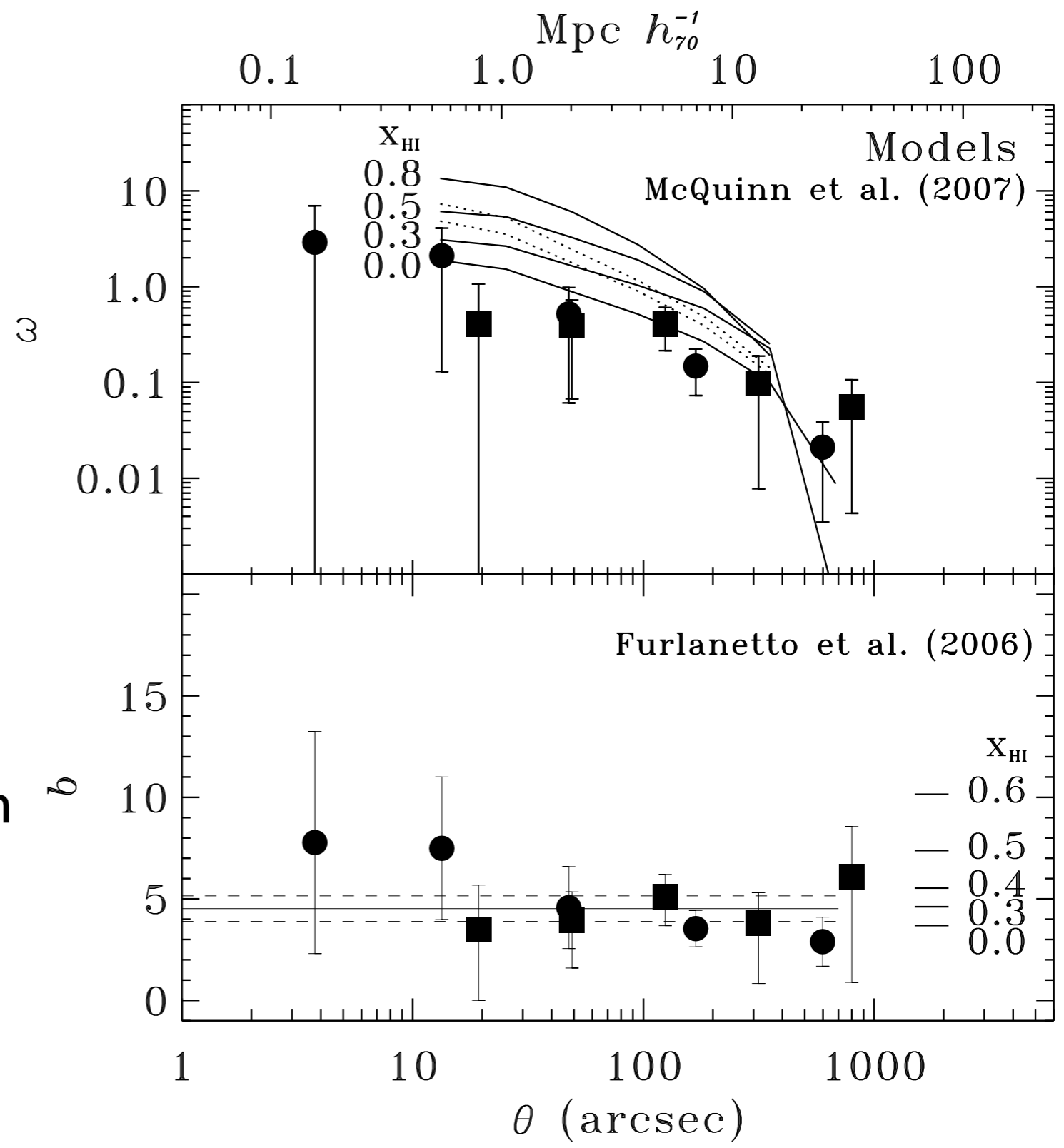
# HSC/LAE

Hypersuprime Cam (HSC)  
 early data on Subaru  
 ~14 deg<sup>2</sup> (21.2 deg<sup>2</sup>)  
 959 (z=5.7), 873 (z=6.6) LAE

No indication of reionization  
 seen in clustering of LAEs

Evolution of number counts  
 also consistent with evolution  
 for 10<sup>11</sup> MSol halos

$x_{\text{HI}} < 0.3$  at  $z=6.6$

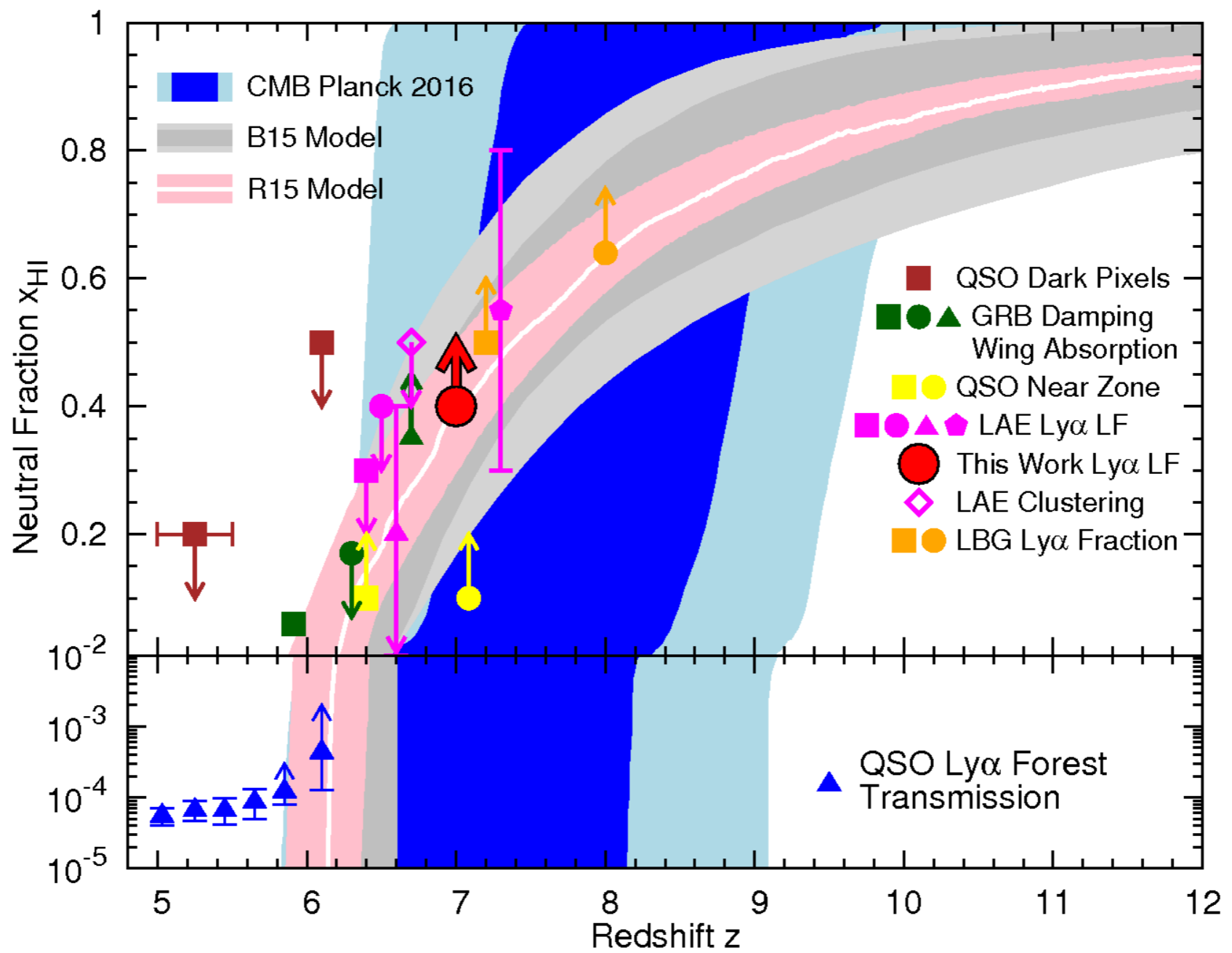




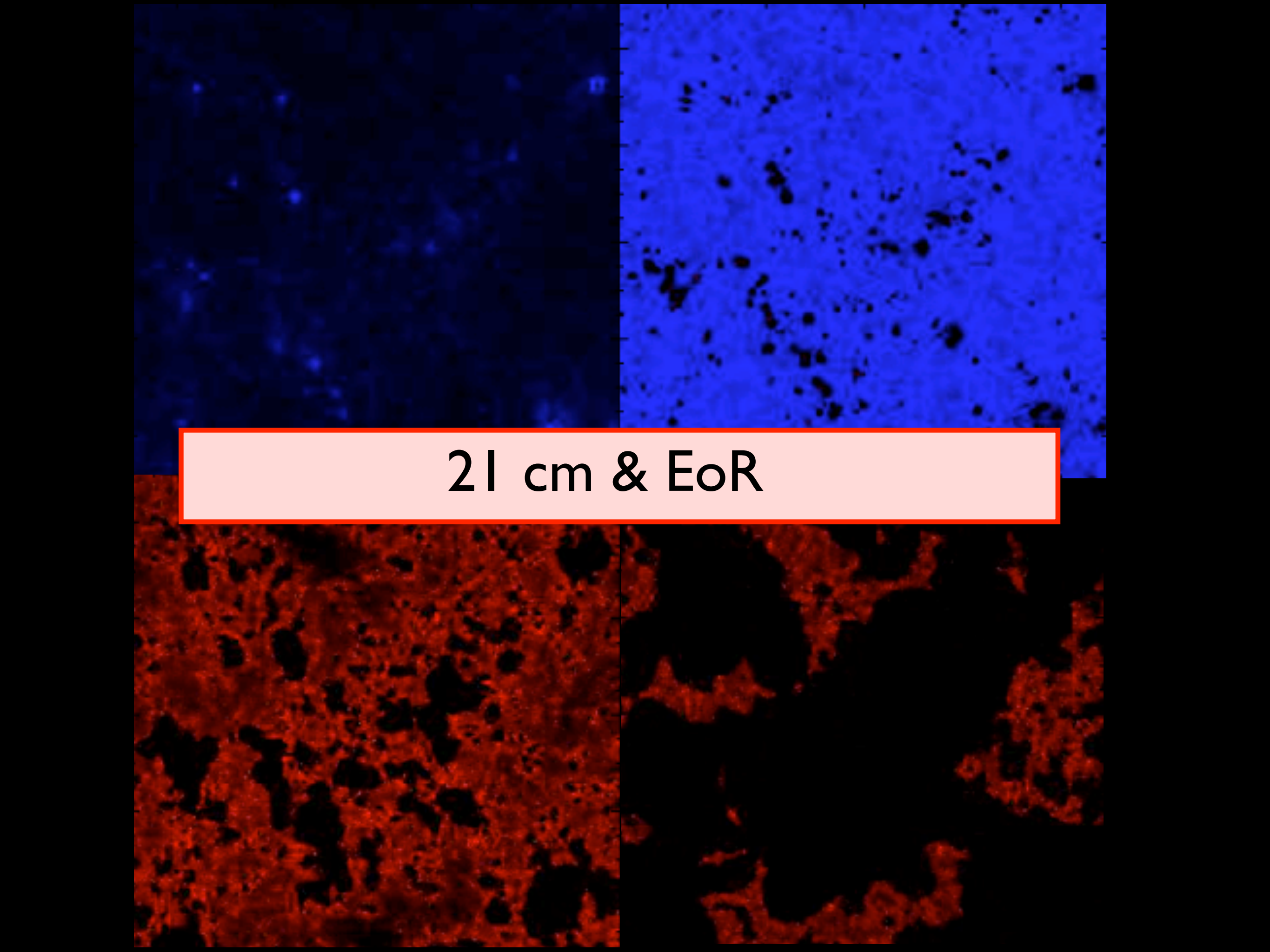
# Reionization summary

Ultimately need to combine all reionization constraints  
e.g. Robertson+ (2015), Greig & Mesinger (2016), ... many more

Reionization histories typically very model dependent





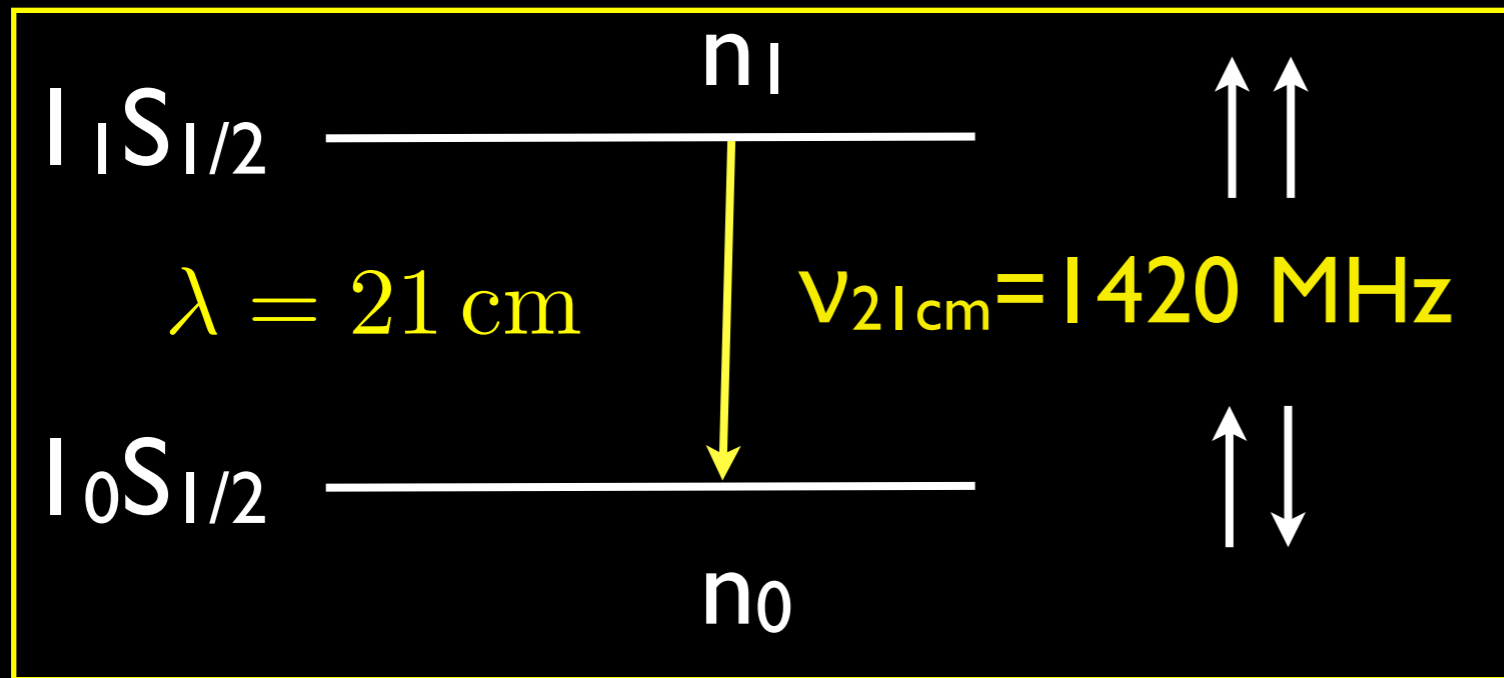


21 cm & EoR



# 21 cm basics

## Hyperfine transition of neutral hydrogen



### Useful numbers:

- 200 MHz  $\rightarrow z = 6$
- 100 MHz  $\rightarrow z = 13$
- 70 MHz  $\rightarrow z \approx 20$
- 50 MHz  $\Rightarrow z \sim 27$

$$t_{\text{Age}}(z = 6) \approx 1 \text{ Gyr}$$

$$t_{\text{Age}}(z = 10) \approx 500 \text{ Myr}$$

$$t_{\text{Age}}(z = 20) \approx 150 \text{ Myr}$$

$$t_{\text{Age}}(z=27) \sim 100 \text{ Myr}$$

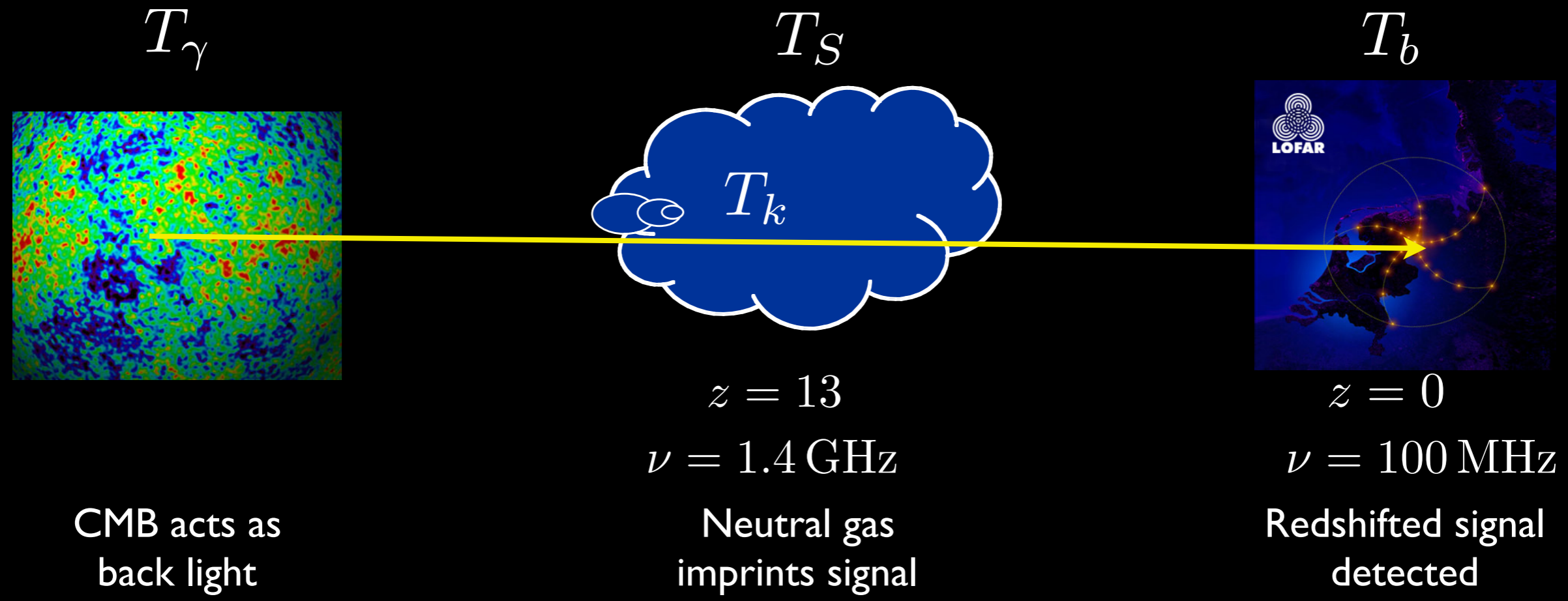
$$t_{\text{Gal}}(z = 8) \approx 100 \text{ Myr}$$

Spin temperature describes relative occupation of levels

$$n_1/n_0 = 3 \exp(-h\nu_{21\text{cm}}/kT_s)$$



# 21 cm line in cosmology



brightness temperature

$$T_b = 27 x_{\text{HI}} (1 + \delta_b) \left( \frac{T_S - T_\gamma}{T_S} \right) \left( \frac{1+z}{10} \right)^{1/2} \left[ \frac{\partial_r v_r}{(1+z)H(z)} \right]^{-1} \text{ mK}$$

neutral fraction      baryon density      spin temperature      peculiar velocities

spin temperature set by different mechanisms:

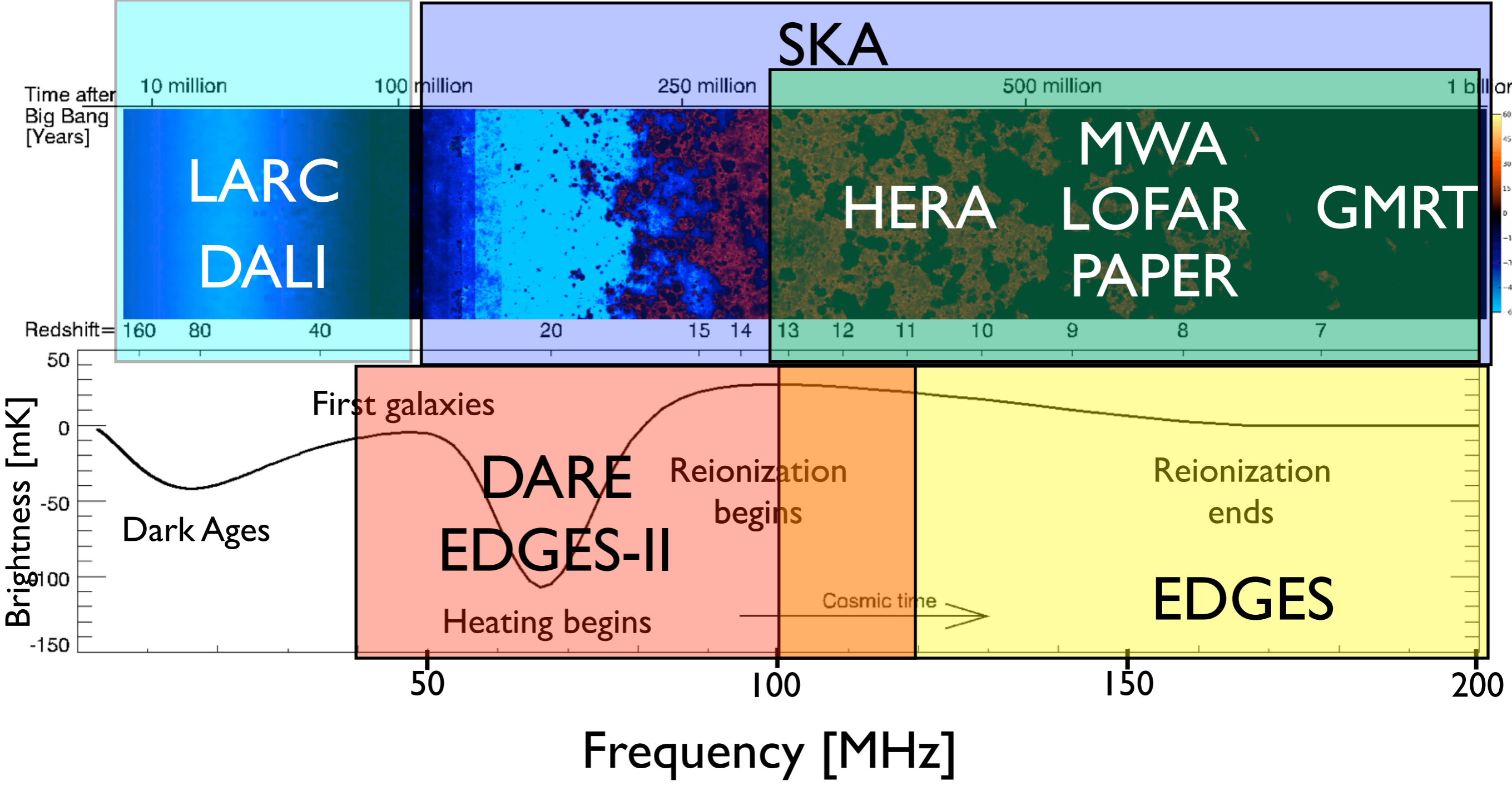
- Radiative transitions (CMB)       $T_{\text{Spin}} \Rightarrow T_{\text{CMB}}$
- Collisions       $T_{\text{Spin}} \Rightarrow T_{\text{gas}}$
- Wouthysen-Field effect (resonant scattering of Ly $\alpha$ )       $T_{\text{Spin}} \Rightarrow T_{\text{gas}}$





# 21 cm astrophysics

Pritchard & Loeb 2010



Systematic path to probing different epochs





**LOFAR**



**MWA**



**PAPER**  
(completed)



**HERA**  
(under construction)



**SKA**  
(roll out 2019-2024)

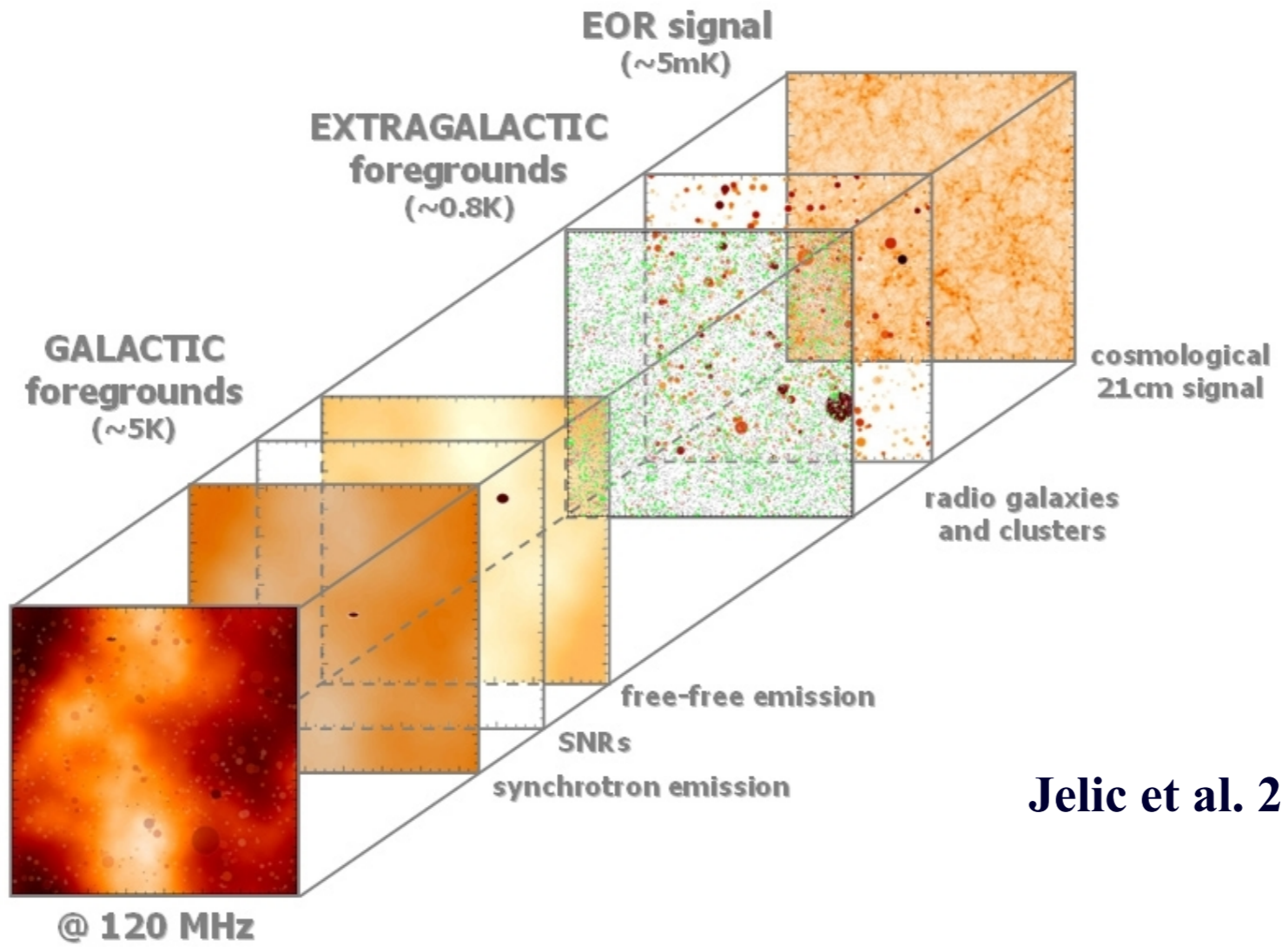




# 21cm challenges

Calibration - sky vs redundant (vs hybrid) calibration

Foregrounds  $\sim 10^3 - 10^5$  signal. Diffuse & pt sources

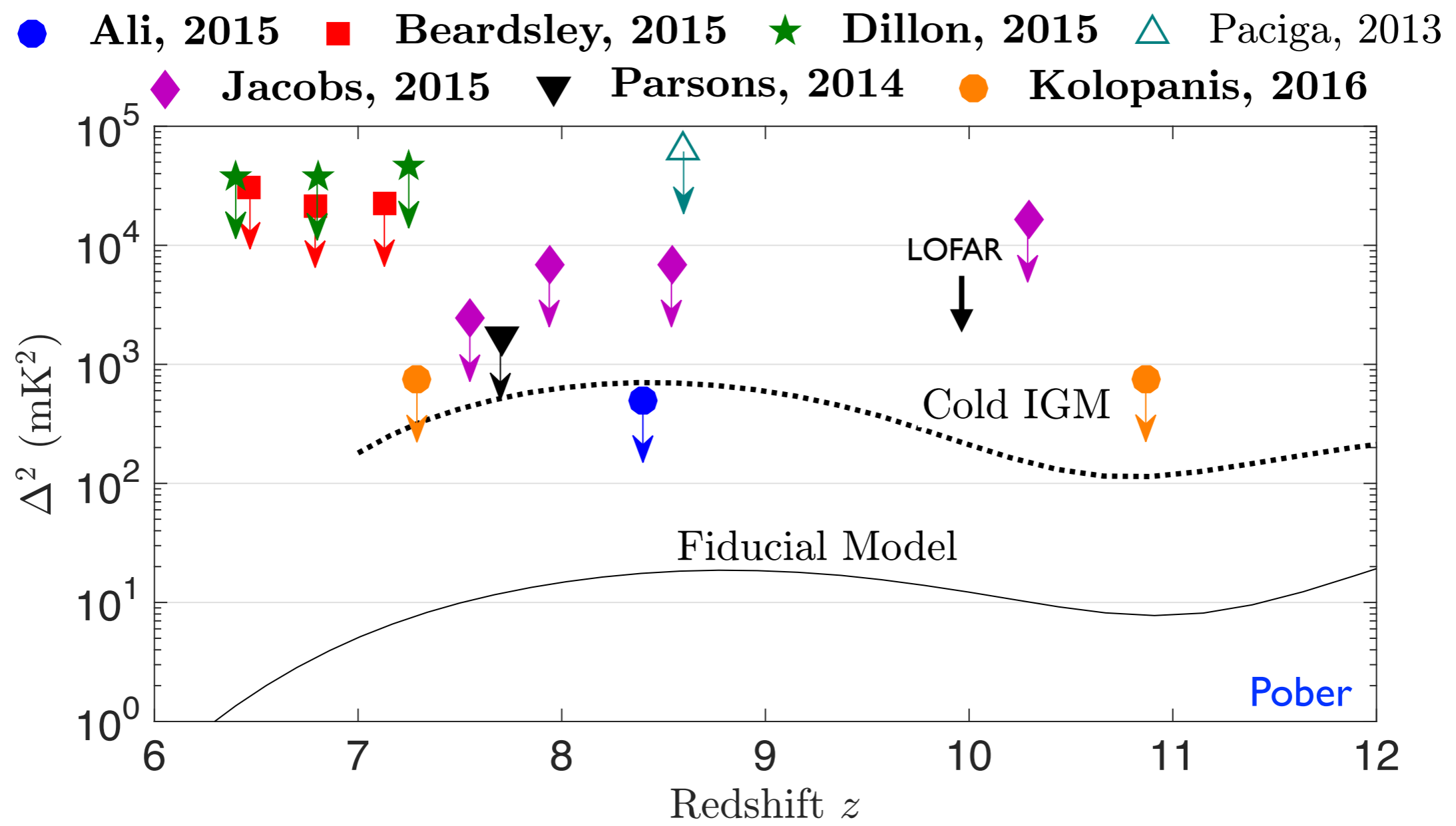


Jelic et al. 2008





# Continuing improvement



Upper limits beginning to make contact with possible models - rule out unheated IGM



# (I) Imaging

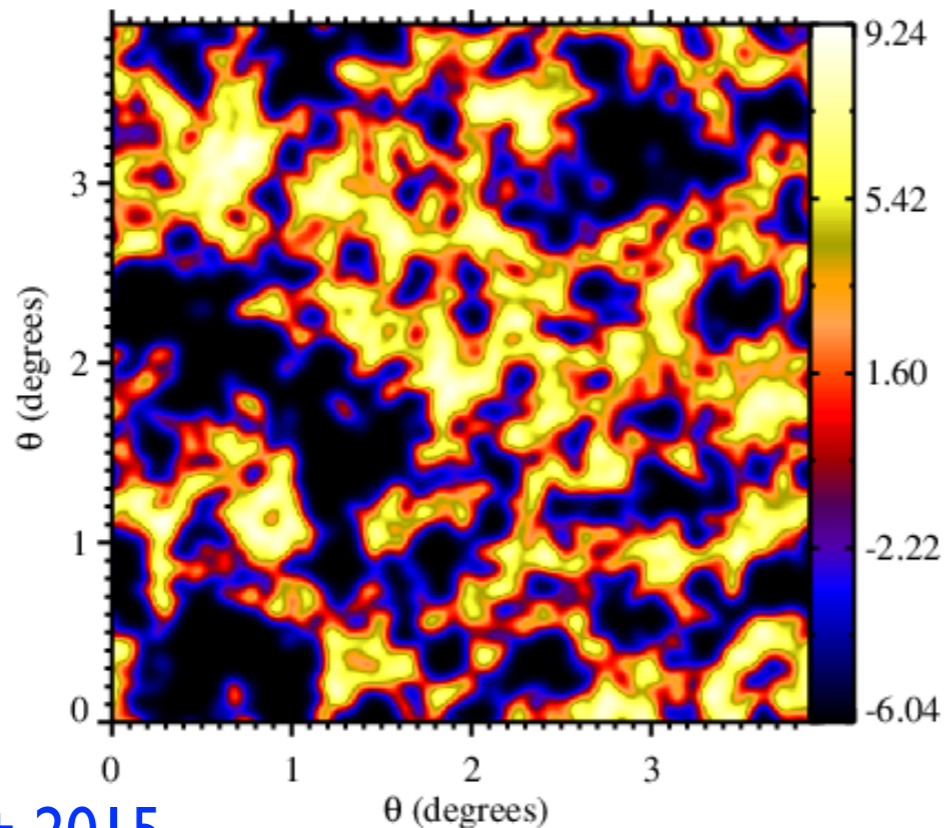
3D maps of topology of reionization -  $\sim 10$  arcmin resolution

Directly image HII region around AGN/bright sources

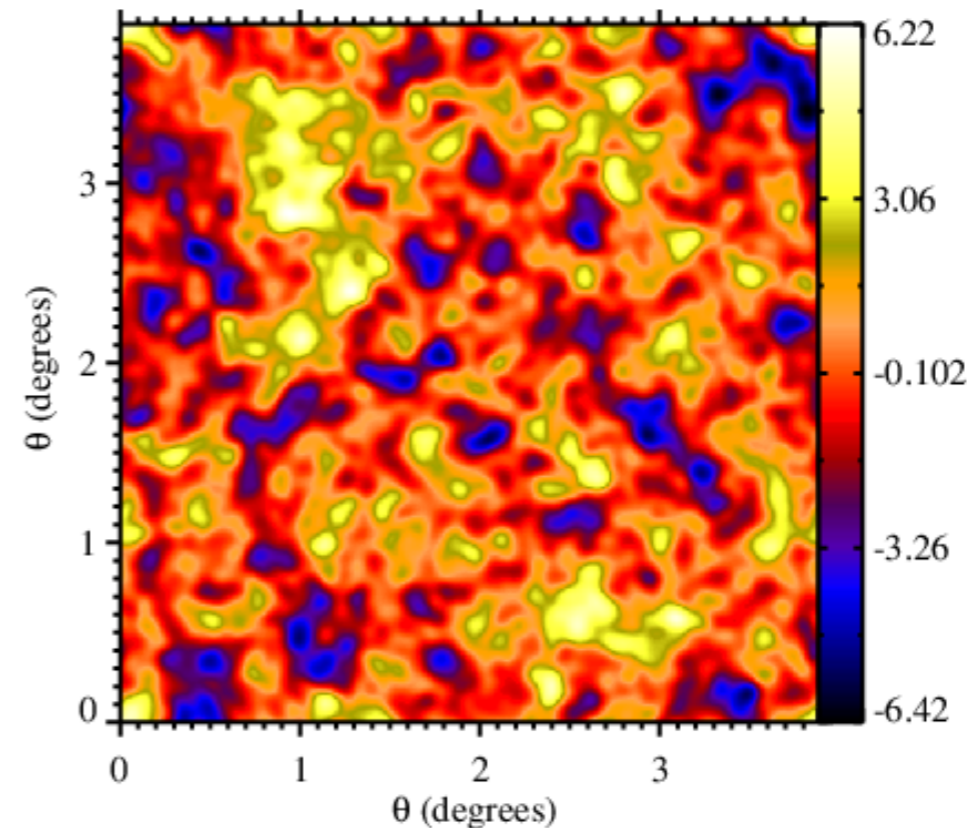
Environmental information for other probes of reionization

HII bubble catalogs and statistics

$\delta T$  (mK) at  $z=7.02$  (117 MHz) with  $[5', 0.8 \text{ MHz}]$



$\delta T$  (mK) at  $z=7.02$  (117 MHz) with  $[5', 0.8 \text{ MHz}]$

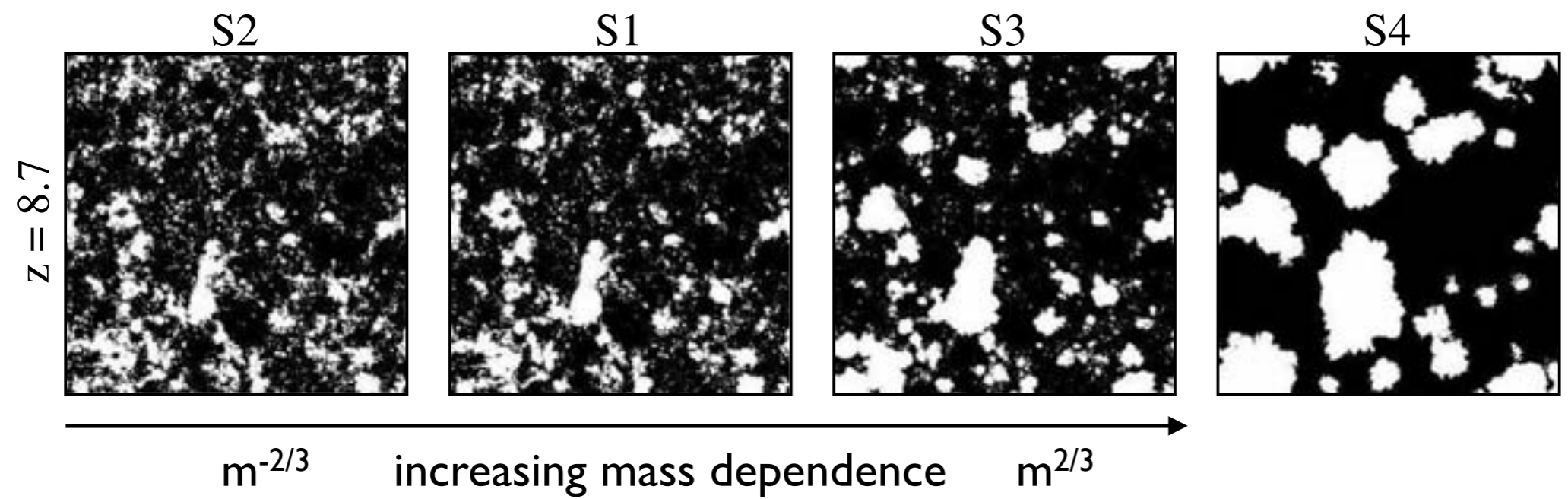


Mellema+ 2015



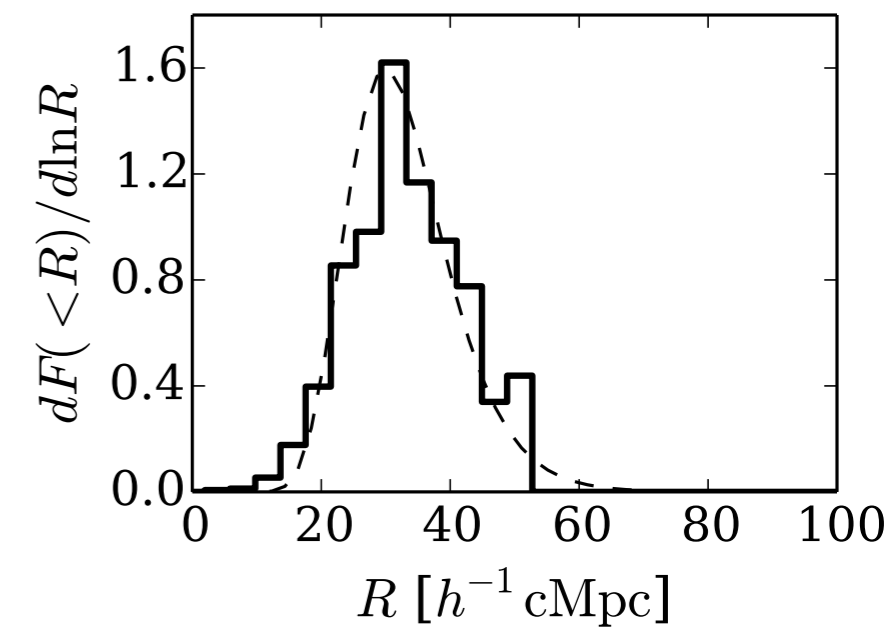
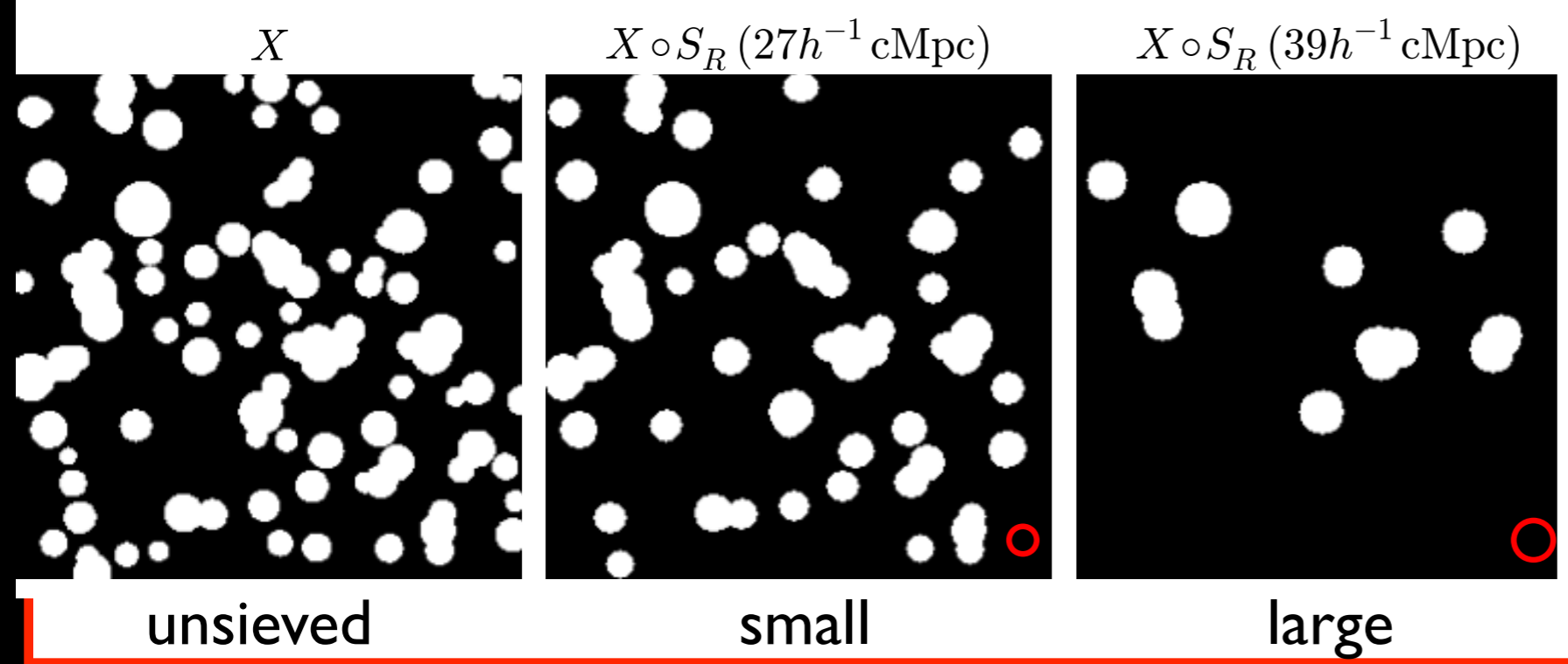
# Granulometry

Size distribution of ionised regions is an interesting probe of reionization



McQuinn+ (2007)

Granulometry: Sieve 21 cm map from small to large scales to reconstruct sizes  
Kakiichi, Majumdar, Mellema+ (2016)



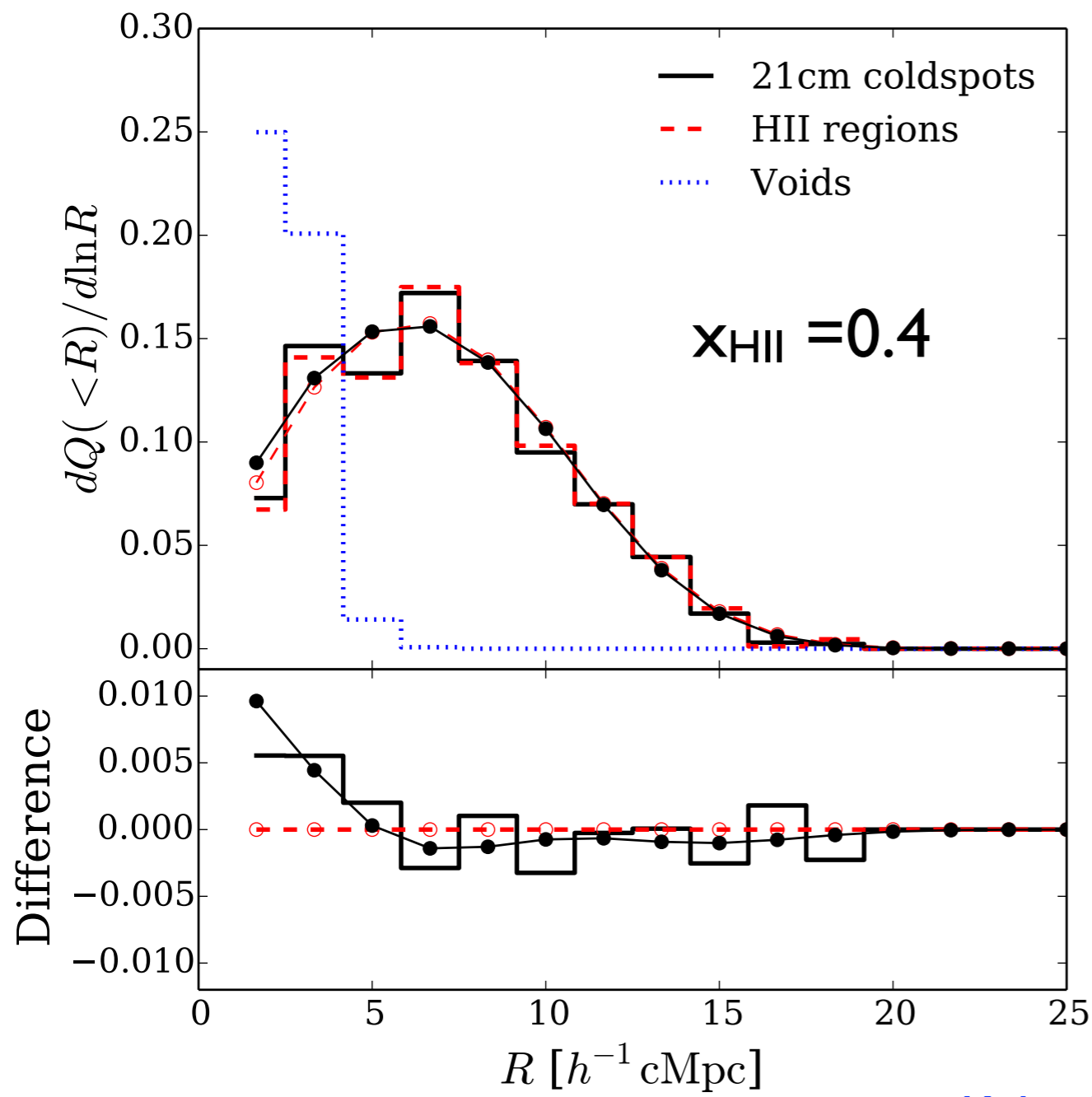




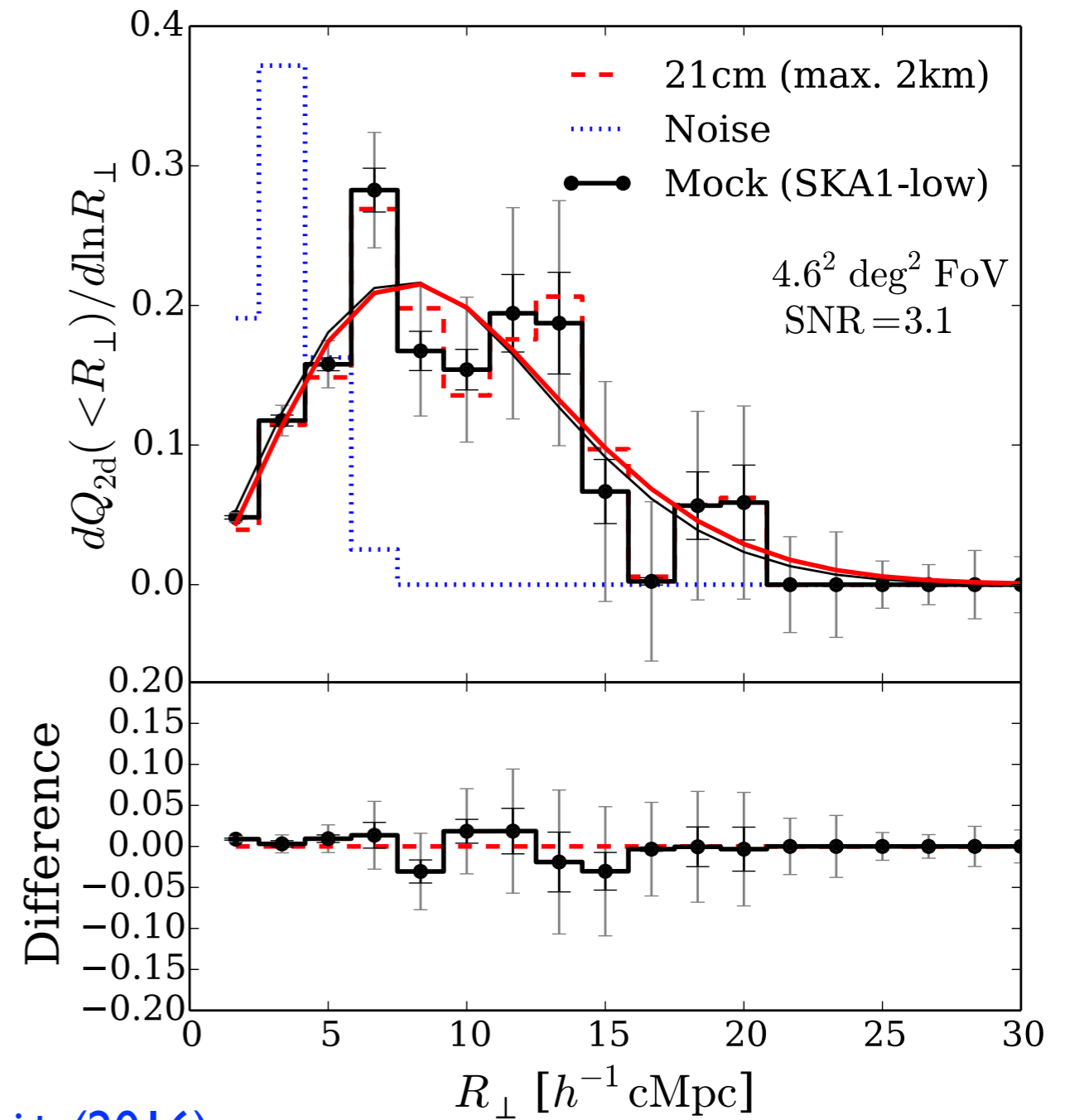
# Granulometry on 21 cm image

21 cm cold spots arise two ways  
- ionised regions or underdense voids

SKA likely needed to study size distributions

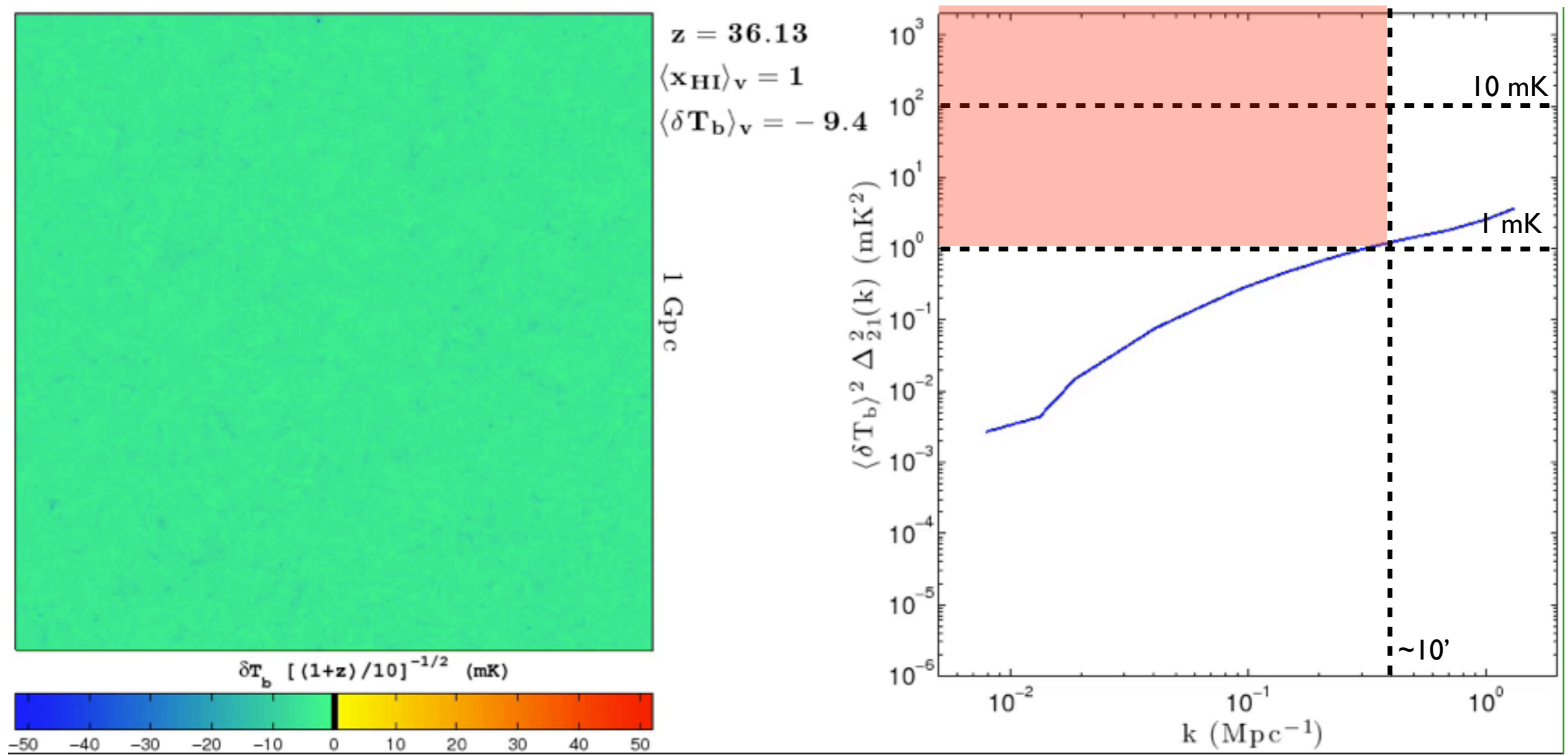


Kakiichi+ (2016)





# (2) Evolution of the power spectrum



Mesinger+ 2010

Rich science contained in spatial and redshift evolution of 21cm power spectrum - observe  $z = 6 - 27$

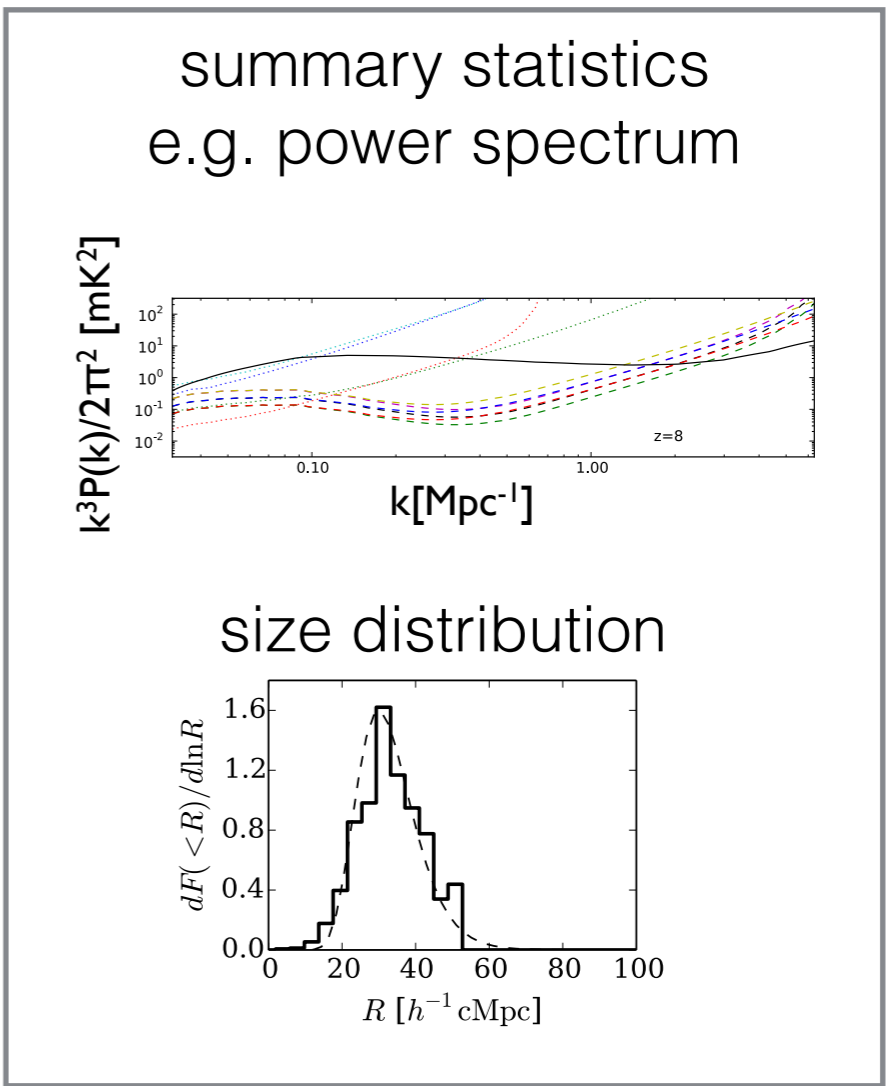
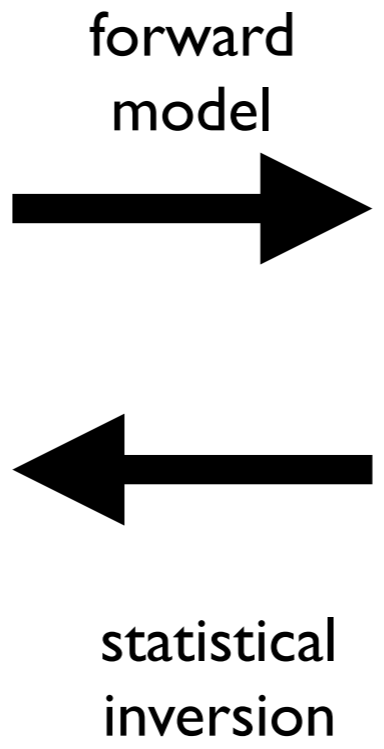


# Parameter estimation

Inputs		Outputs	
$P(\mathbf{d} \theta, M)$	$\times P(\theta M)$	$= P(\theta \mathbf{d}, M)$	$\times P(\mathbf{d} M)$
Likelihood	Prior	Posterior	Evidence

models    parameters

$(f_*, \xi_{\text{ion}}, \xi_X, \xi_\alpha, \lambda_{\text{mfp}})$



- 1) Parameter estimation
- 2) Model selection





# Emulation

Reionization simulations often computationally expensive, but vital for 21 cm analysis - approximate schemes needed

Given a computationally expensive model  $y(x)$ , for parameters  $x$ , build an “emulator”  $\bar{y}(x)$  that is fast to evaluate

- 1) Form training set of well chosen samples  $\{x_{\text{train}}, y_{\text{train}}=y(x_{\text{train}})\}$
- 2) Establish basis for approximation
- 3) Establish means of interpolating from training set to arbitrary points

Used extensively in climate change and also in cosmology

e.g. Coyote universe - emulation of non-linear matter power spectrum  $P(k | \text{parameters})$  [Heitmann+ 2006](#), [Habib+ 2007](#)

- Latin hyper-cube used to build training set
- PCA basis
- Gaussian processes for interpolation

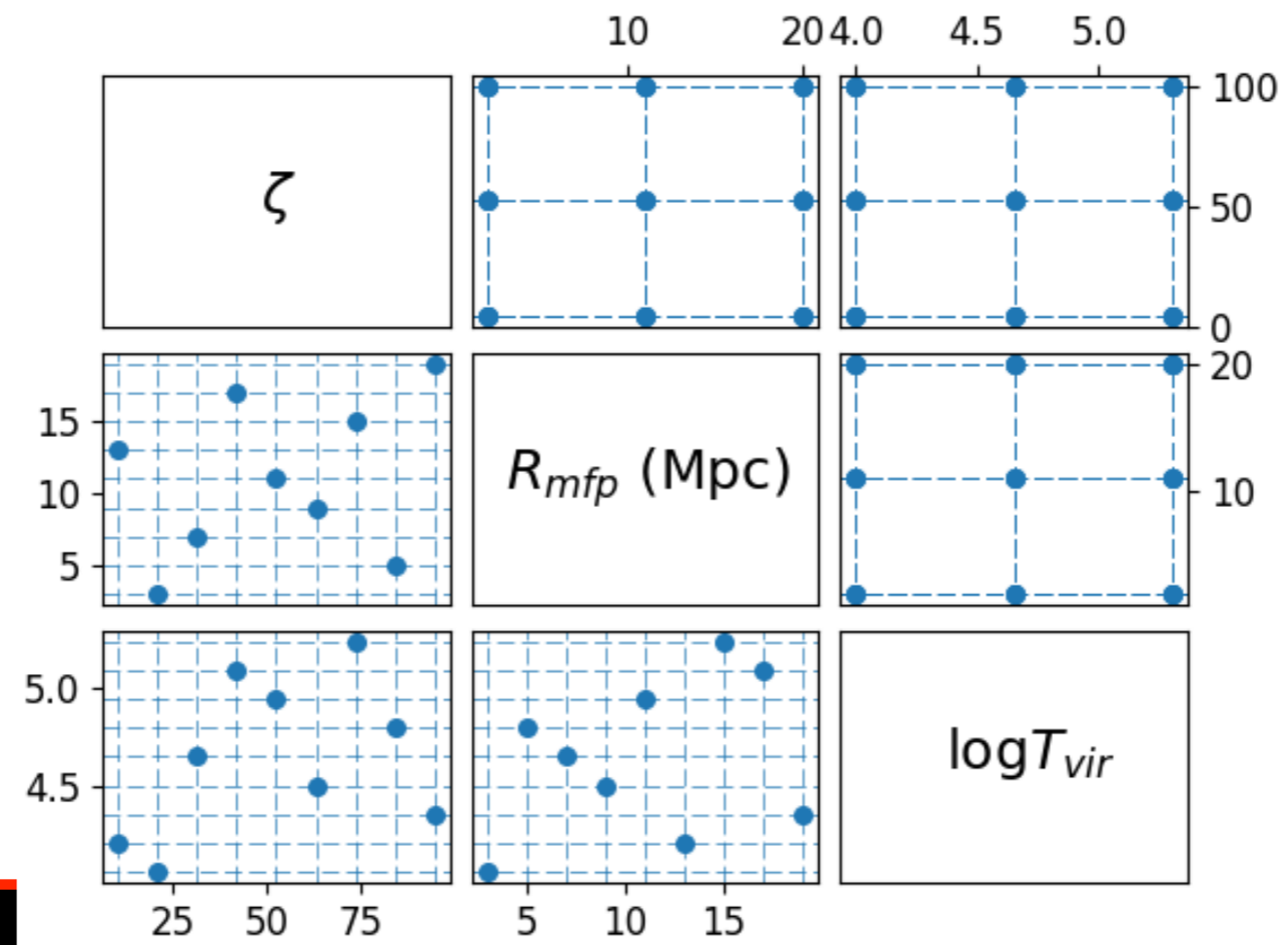


# Latin hypercube sampling

Curse of dimensionality: number of points required to sample in a regular grid scales as  $(L/\Delta)^N$  - prohibitive for even modest N

Latin hypercube sampling - distribute M points such that each parameter is divided into M bins with each bin occupied only once.

More efficiently uses samples, especially if tweaked to reduce clustering of points e.g. minimax nearest neighbour distances



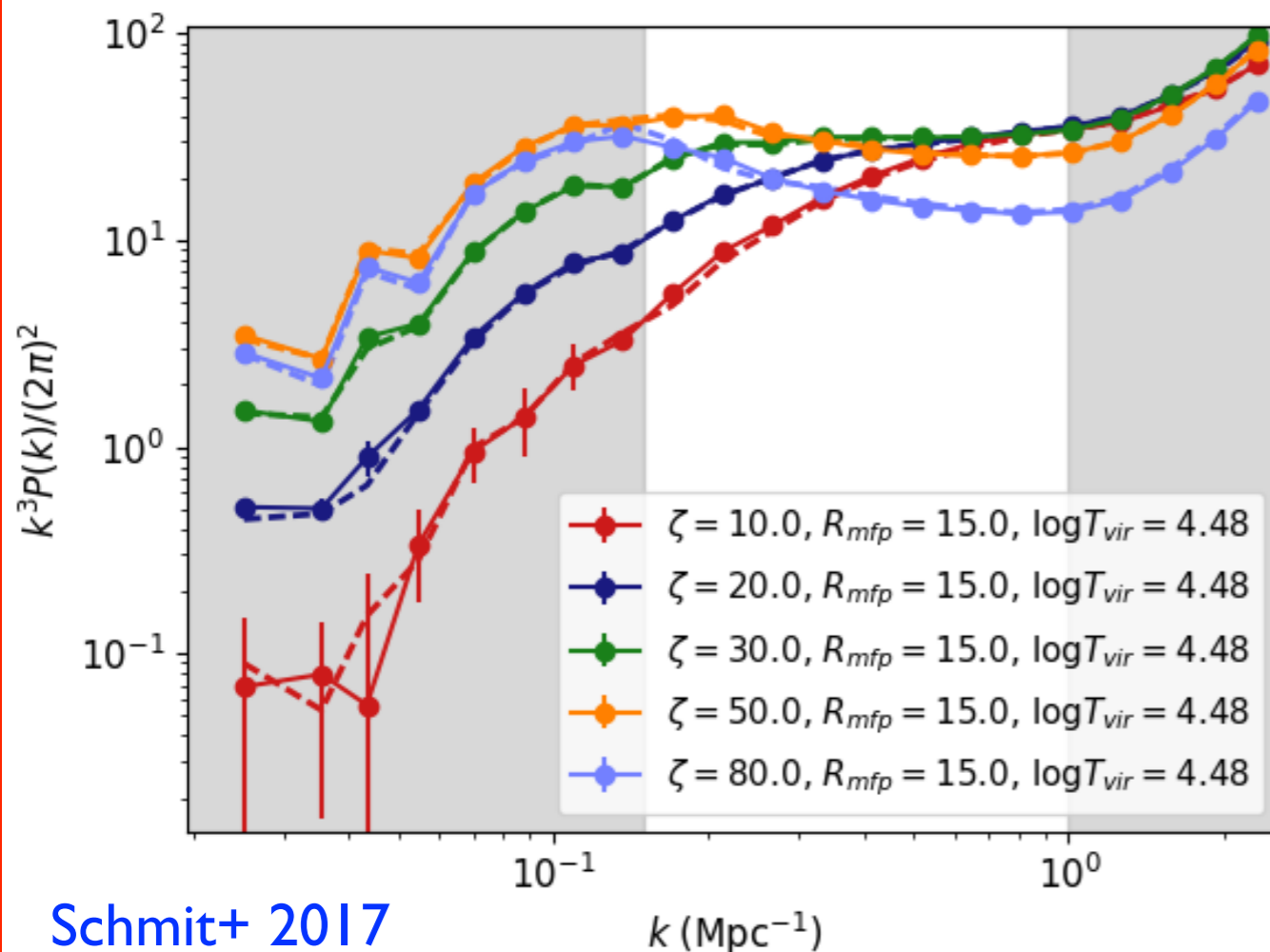
Schmit+ 2017

# Bayesian inference with emulation

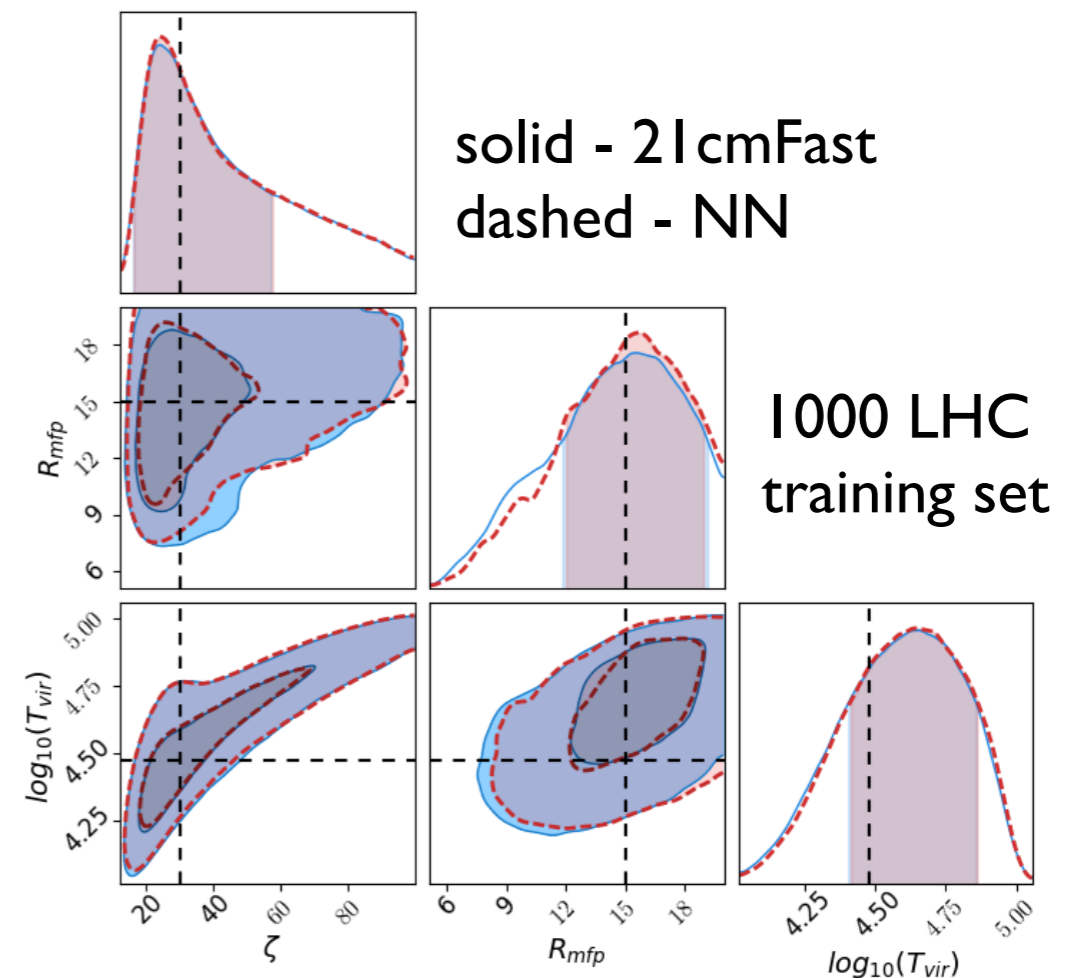
Different interpolation schemes - Gaussian Processes [Kern+ 2017](#)  
- Neural networks [Schmit+ 2017](#)

Sampling density in MCMC proportional to target density  
=> implies many samples are closely spaced in parameter space

Significant increase in speed without loss of accuracy  
e.g. training set  $\sim 10^3$  samples c.f.  $10^5 - 10^6$  in MCMC



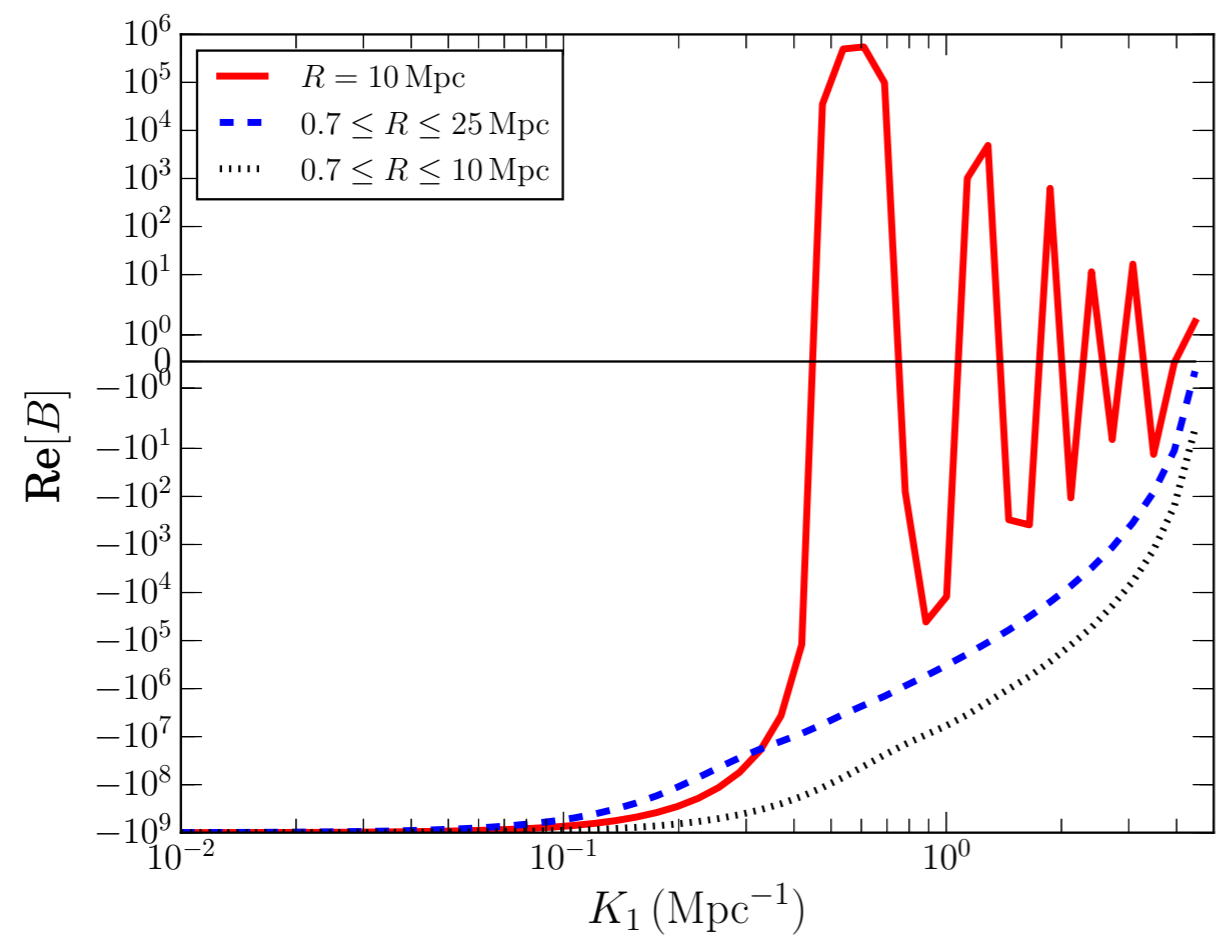
Schmit+ 2017





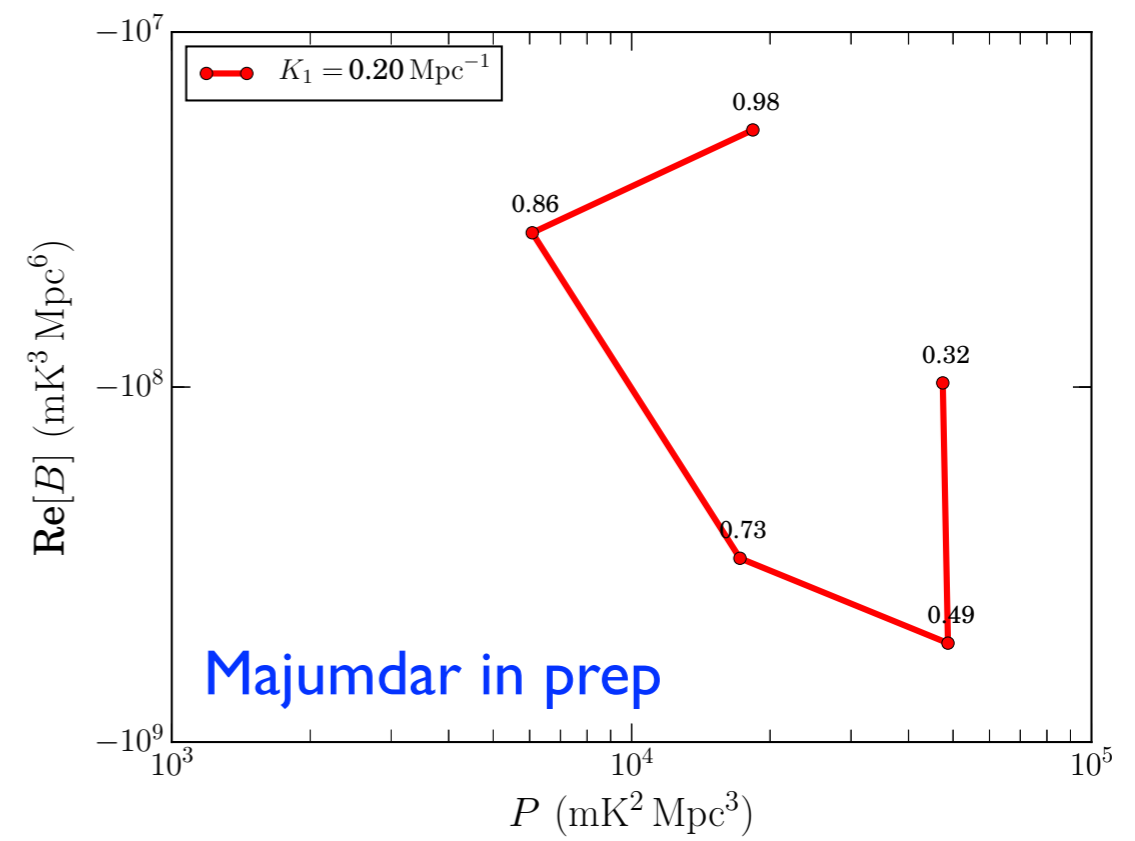


# 21 cm bispectrum



Bispectrum a probe of non-Gaussianity so complementary to power spectrum

Bispectrum a probe of non-Gaussianity so complementary to power spectrum => break degeneracies



Ultimately range of statistics needed to exploit information in 21 cm observations

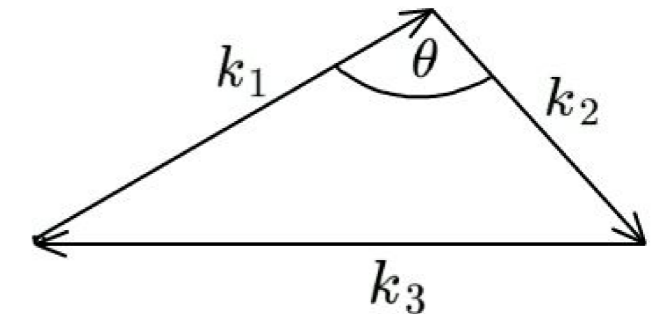


# Modal bispectrum estimator

Need fast estimator for bispectrum, since large range of possible configurations

Expanding Dirac delta function in terms of exponentials allows factorisation

$$\begin{aligned} \delta^K(\mathbf{m}_1 + \mathbf{m}_2 \dots + \mathbf{m}_p) &= \frac{1}{N_{\text{pix}}} \sum_{\mathbf{n}}^{N_{\text{pix}}} e^{i2\pi \mathbf{n} \cdot (\mathbf{m}_1 + \mathbf{m}_2 \dots + \mathbf{m}_p) / N_{\text{side}}} \\ &= \frac{1}{N_{\text{pix}}} \sum_{\mathbf{n}}^{N_{\text{pix}}} \prod_i^p e^{i2\pi \mathbf{n} \cdot \mathbf{m}_i / N_{\text{side}}} . \end{aligned}$$



Can then express poly-spectra in terms of sampled FT of 2D cm field

$$\mathcal{P}(\mathbf{k}_1, \mathbf{k}_2, \dots, \mathbf{k}_p) \approx H^p \frac{1}{V} \frac{\sum_{\mathbf{n}}^{N_{\text{pix}}} \prod_{i=1}^p \delta(\mathbf{n}, \mathbf{k}_i)}{\sum_{\mathbf{n}}^{N_{\text{pix}}} \prod_{i=1}^p I(\mathbf{n}, \mathbf{k}_i)} , \quad \begin{aligned} \delta(\mathbf{n}, \mathbf{k}_i) &= \sum_{\mathbf{k}_i / k_F \simeq \mathbf{m}_i} \Delta_{\text{FFT}}(\mathbf{m}_i) e^{i2\pi \mathbf{n} \cdot \mathbf{m}_i / N_{\text{side}}} , \\ I(\mathbf{n}, \mathbf{k}_i) &= \sum_{\mathbf{k}_i / k_F \simeq \mathbf{m}_i} e^{i2\pi \mathbf{n} \cdot \mathbf{m}_i / N_{\text{side}}} , \end{aligned}$$

For example, estimator of the bispectrum

$$B(k_F \mathbf{m}_1, k_F \mathbf{m}_2, k_F \mathbf{m}_3) \approx \frac{V^2}{N_{\text{pix}}^3} \frac{\sum_{\mathbf{n}}^{N_{\text{pix}}} \delta(\mathbf{n}, \mathbf{k}_1) \delta(\mathbf{n}, \mathbf{k}_2) \delta(\mathbf{n}, \mathbf{k}_3)}{\sum_{\mathbf{n}}^{N_{\text{pix}}} I(\mathbf{n}, \mathbf{k}_1) I(\mathbf{n}, \mathbf{k}_2) I(\mathbf{n}, \mathbf{k}_3)} ,$$

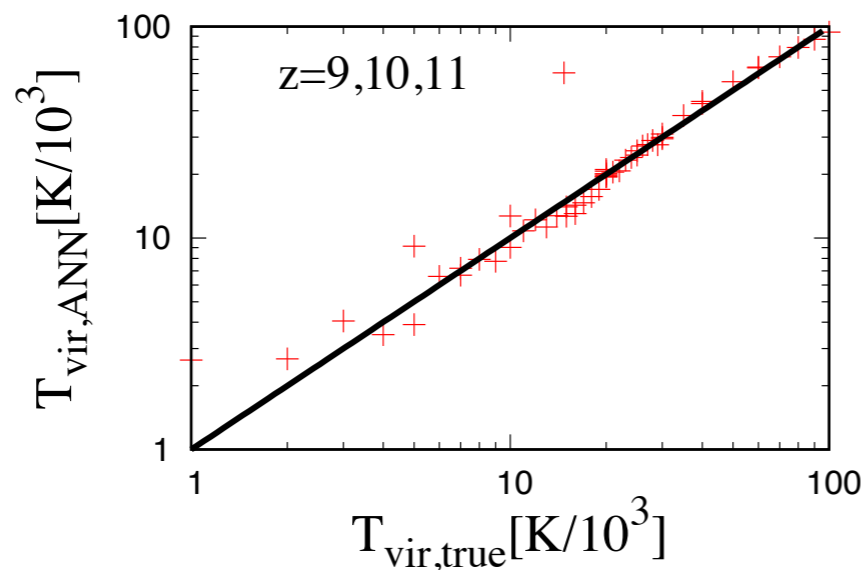
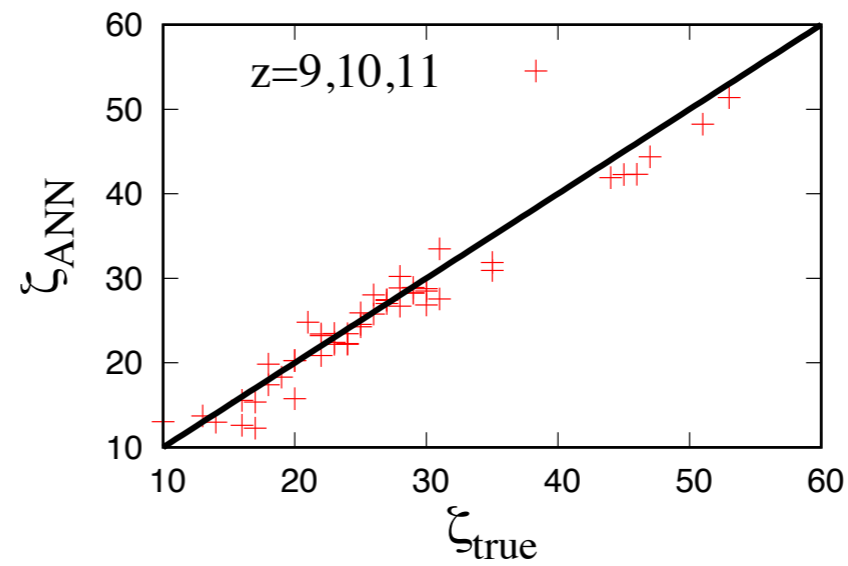
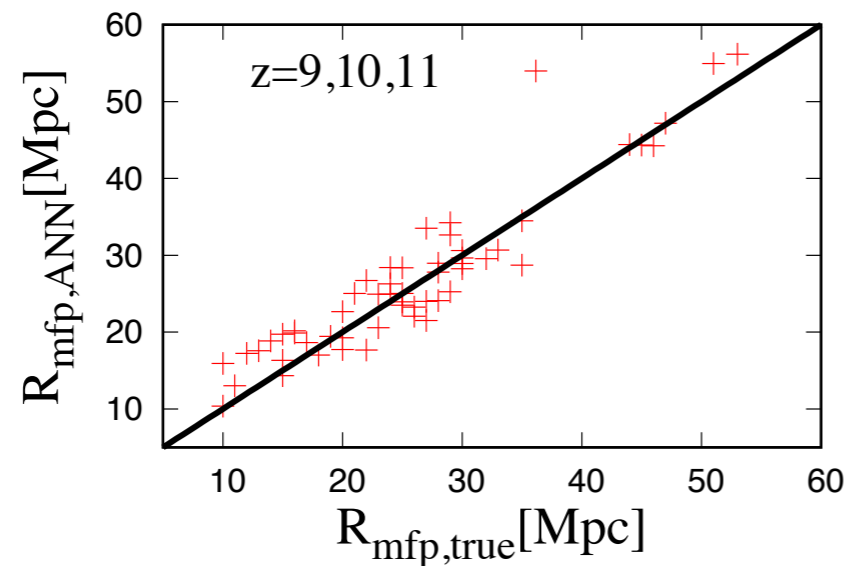
Watkinson+ 2017



# Machine learning?

Can also use ML for inversion (rather than Bayesian inference)

e.g. Neural Networks to identify astrophysics parameters from shape of power spectrum [Shimabukuro & Semelin 2017](#)





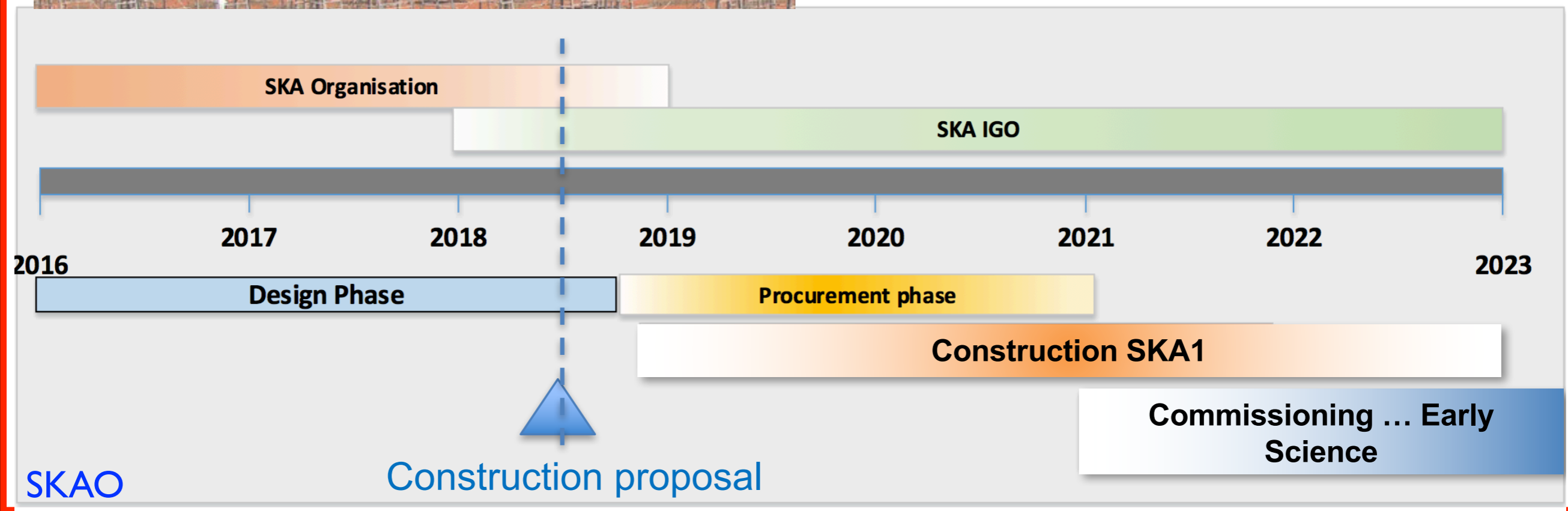


# Beyond LOFAR... SKA

- MID - dishes (SA) - 250MHz - 20 GHz;
- LOW - antennae (AU) - 50-350MHz



- International headquarters at Jodrell Bank
- SKA will be the premier radio telescope facility with science case ranging from cradle of life, through cosmology, to epoch of reionization
- Cost control exercise currently underway
- Form IGO 2019  
Commissioning/Early science 2021-2024  
Key science projects 2024-29



SKAO

Construction proposal



# Conclusions

- Reionization is still interesting! CMB, HST, and LAE surveys seem to indicate interesting behaviour at  $z \sim 7$
- LOFAR, MWA, PAPER are all confronting data with increasingly mature analysis pipelines. Still much to be done.
- 21 cm upper limits are beginning to make contact with plausible (if extreme) models
- Imaging will become interesting with SKA e.g. granulometry and for measuring bubble size distributions
- Power spectrum easiest statistic to work with currently
- Application of emulation may prove a useful conduit between full numerical simulations and Bayesian analysis
- Other non-Gaussian statistics also useful e.g. bispectrum. Need to be fast to evaluate to include in analysis pipelines
- Fruitful to apply machine learning techniques
- SKA finalising design with construction expected to begin  $\sim 2019$

**Fin**





# Science from 21 cm

Analysis more complicated than for, say, CMB because

- 1) No complete and agreed upon model of reionization
  - each simulation uses different parametrization & methods
  - different prescriptions for sources and sinks of photons
  - no guarantee that any are “correct”
  - unclear any one simulation covers all possibilities
- 2) Not clear simple statistics e.g. power spectrum capture all information
- 3) Evaluation of models is computationally expensive
  - full hydro + RT requires hundreds of hours of super-computer time

Strategies:

- 1) Analytic models
- 2) Semi-numerical codes - e.g. 21cmFAST, Simfast21, ...
- 3) Emulation

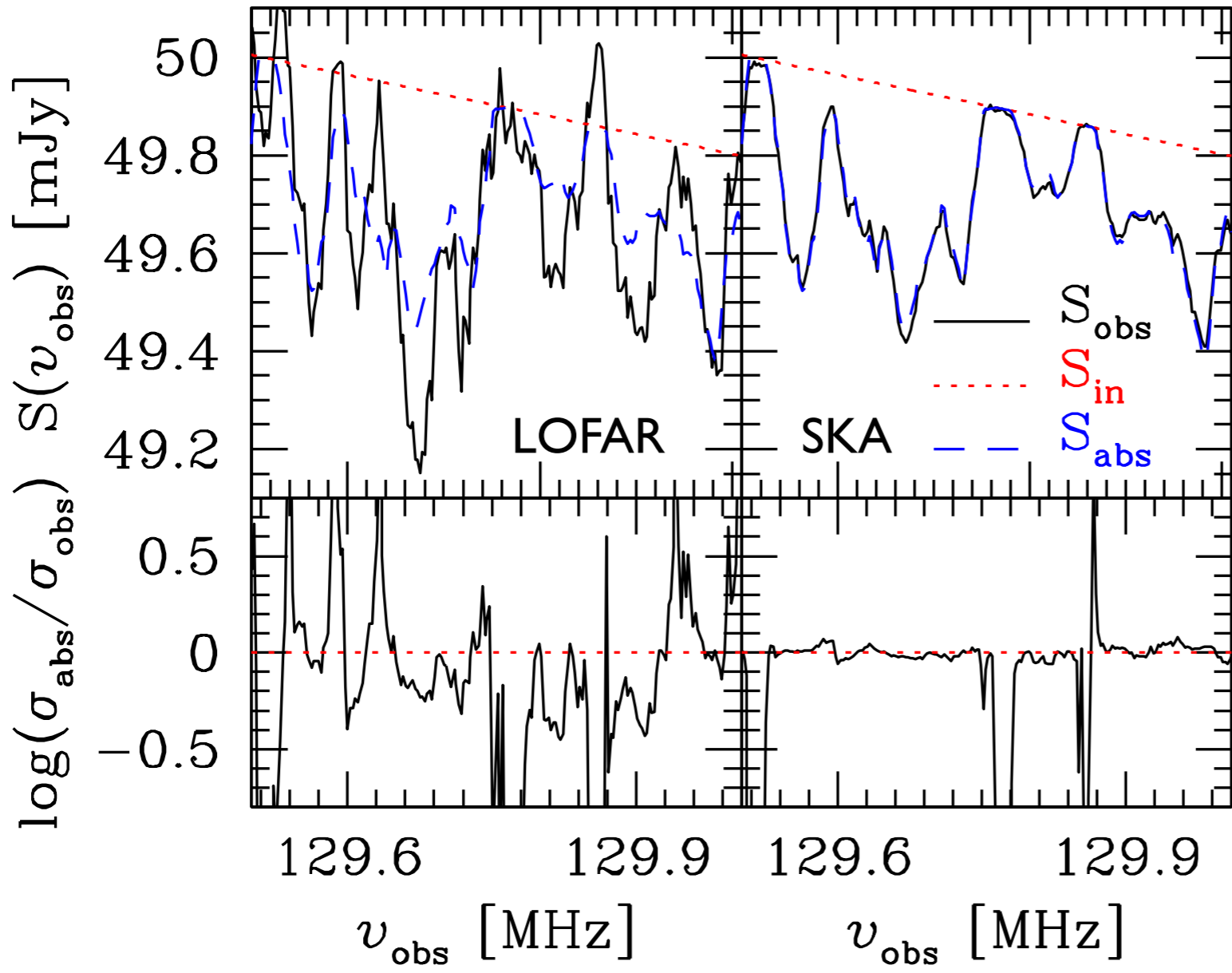


# (3) 21cm Forest

IF find  $z > 6$  radio bright QSOs or other radio bright objects e.g. GRB

10kHz resolved spectra of 21cm forest in bright radio sources at  $z > 6$

Resolve  $\sim$ kpc scale structures in IGM



50mJy source @z=10

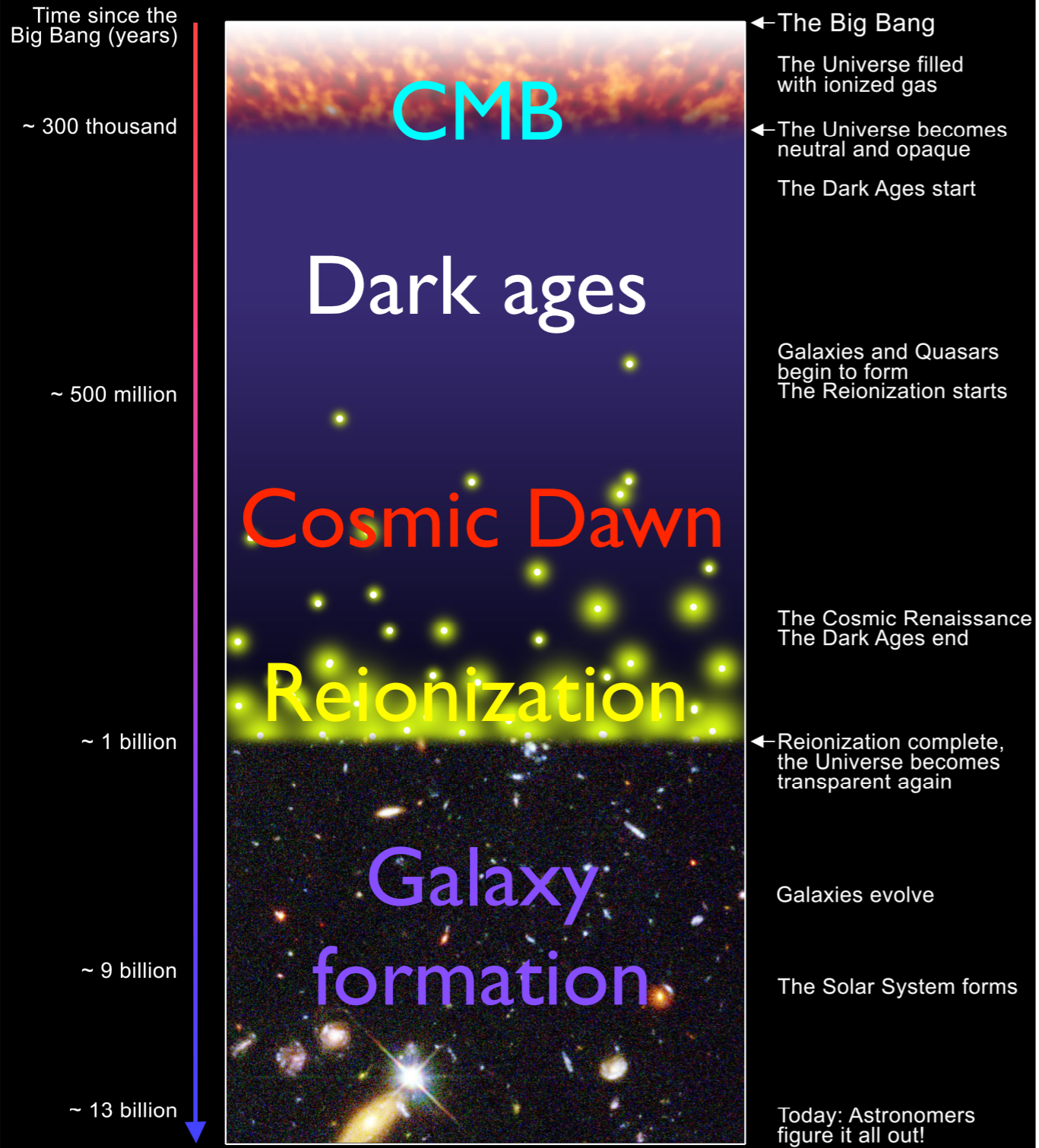
Ciardi+ 2015



# Overview

## What is the Reionization Era?

A Schematic Outline of the Cosmic History



S.G. Djorgovski et al. & Digital Media Center, Caltech

- Reionization
- CMB constraints of reionization
- 21 cm observations
- CMB optical depth from 21cm



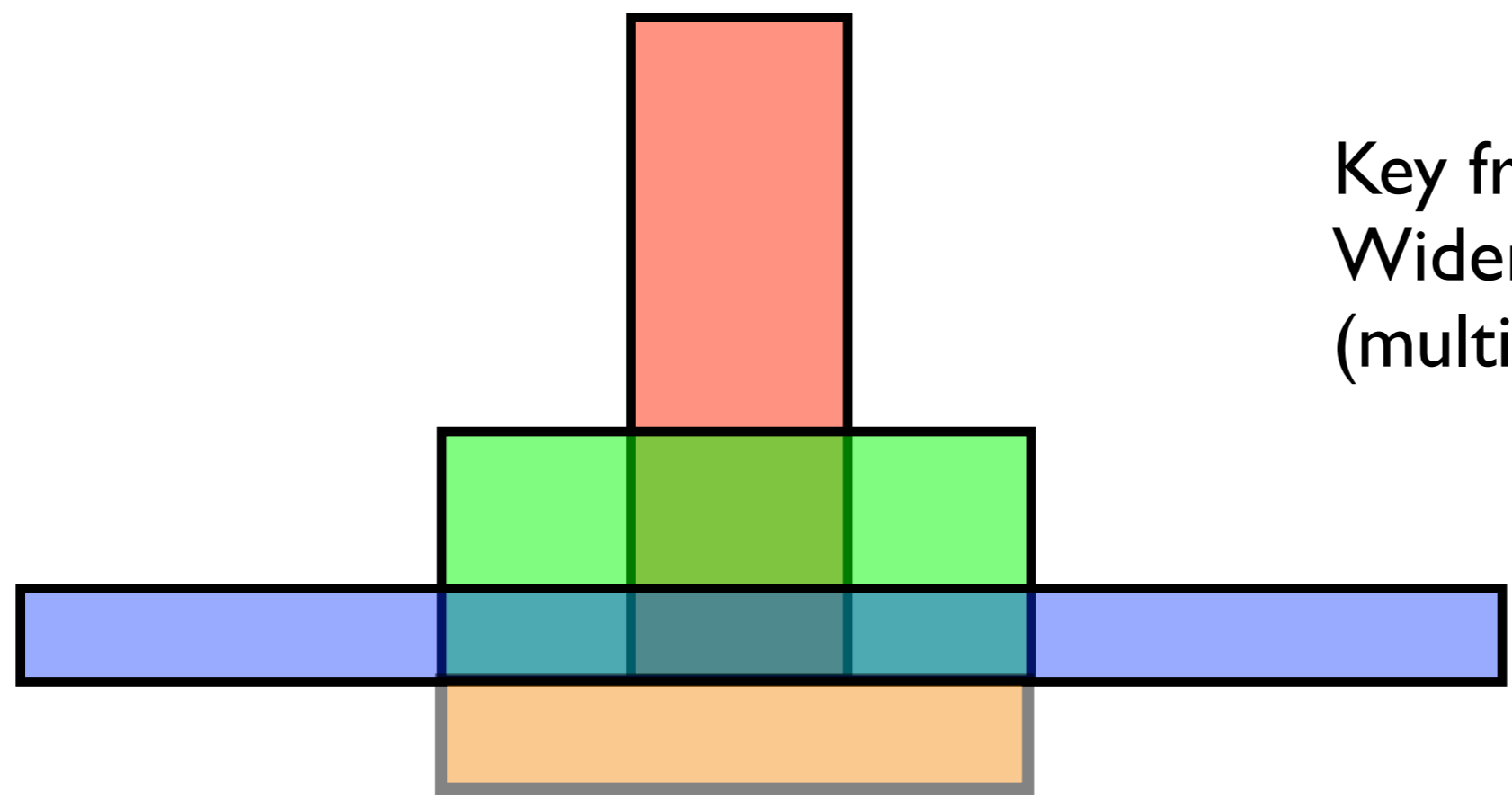


# SKA-LOW observing strategy

Deep: 5 x 1000hr integration => 100 deg<sup>2</sup> field  
 Middle: 50 x 100hr integration => 1,000 deg<sup>2</sup> field  
 Shallow: 500 x 10hr integration => 10,000 deg<sup>2</sup> field  
 IM: 50 x 100hr integration => 1,000 deg<sup>2</sup> field

Koopmans+ 2015  
[\[arXiv 1505.07568\]](https://arxiv.org/abs/1505.07568)

Single pointing  
 ~ 20 deg<sup>2</sup>



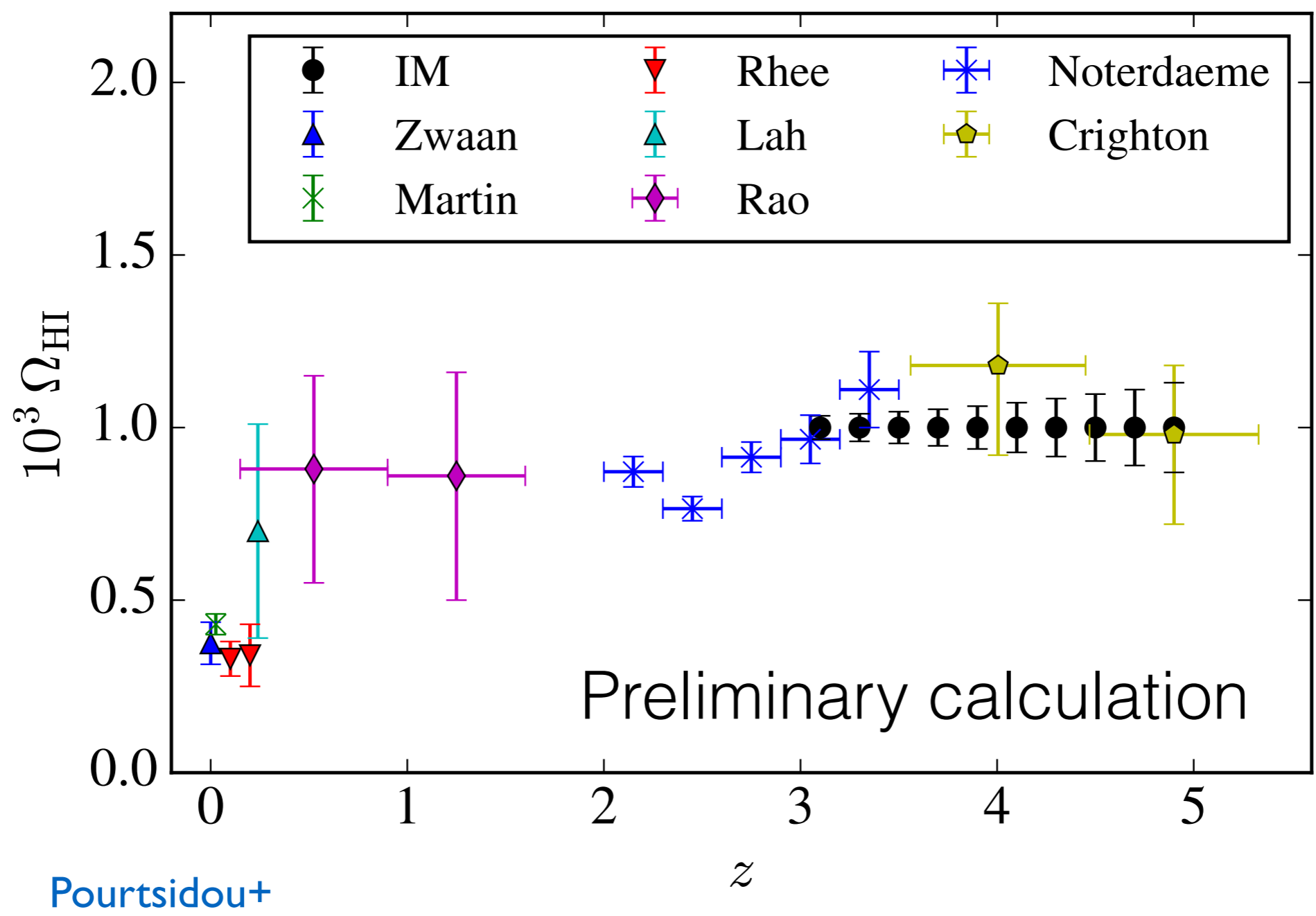
Key frequencies: 200-50MHz  
 Wider band for foregrounds  
 (multibeaming to reduce tint)

Shallow: LOFAR-like power spectrum sensitivity over 10000 deg<sup>2</sup>.  
 Middle: Shallow imaging + power spectrum over 1000 deg<sup>2</sup>  
 Deep: Power spectrum to z<27 & deep imaging over 100 deg<sup>2</sup>  
 IM: OmegaHI & cosmology at 3<z<6 over 1000 deg<sup>2</sup>



# (4) Intensity mapping at $3 < z < 6$

Intensity mapping with LOW for  $\Omega_{\text{HI}}$  & cosmology

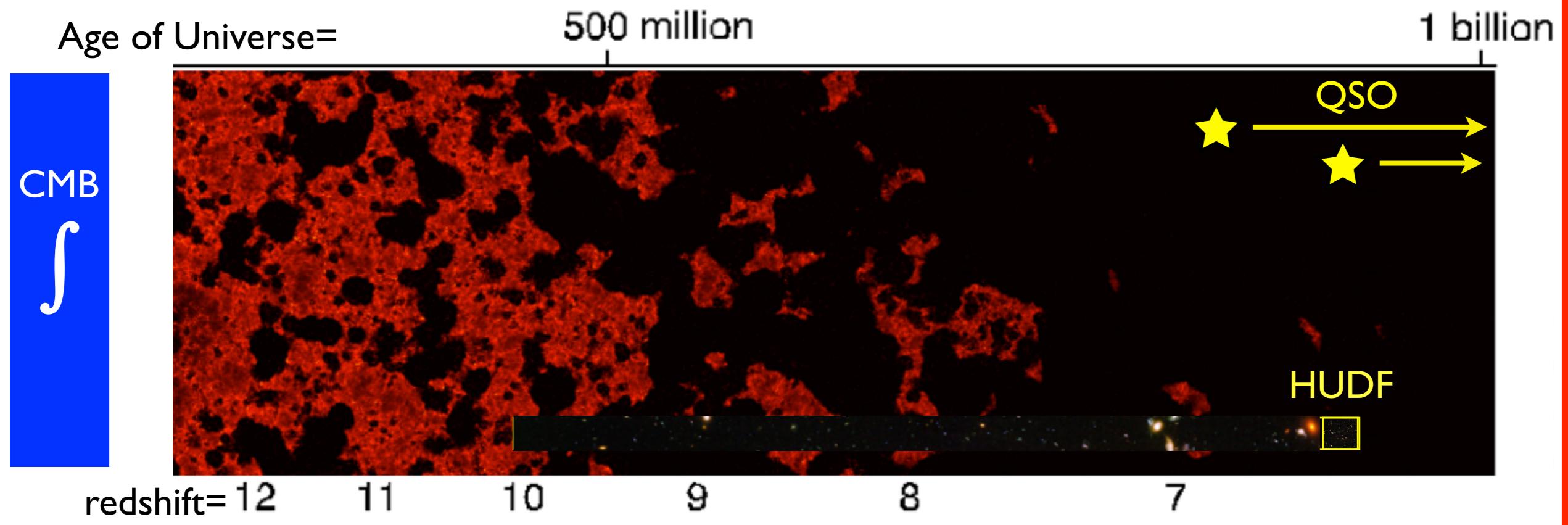


Pourtsidou+

Preliminary calculation



# More needed...



Existing observations leaves much unanswered:

- 1) Lyman-alpha forest: end point  $z > 6.5$
- 2) CMB optical depth: mid point  $z \sim 11$  (Revised down by Planck to  $z \sim 8.8 \pm 1.5$ )
- 3) kSZ amplitude: duration  $z < 4.4$  ?

HST probes skewer much smaller than scale of ionized regions + only brightest sources

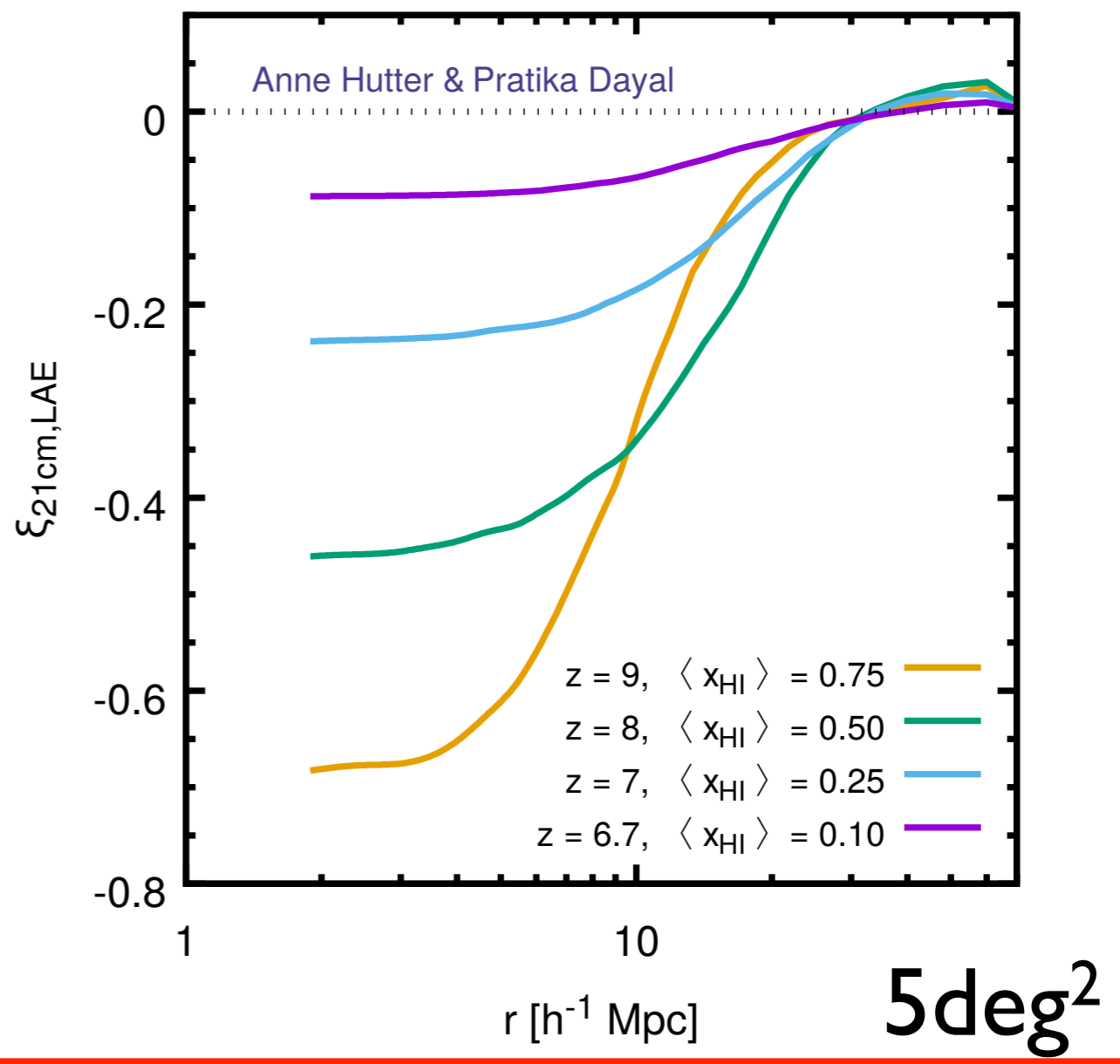
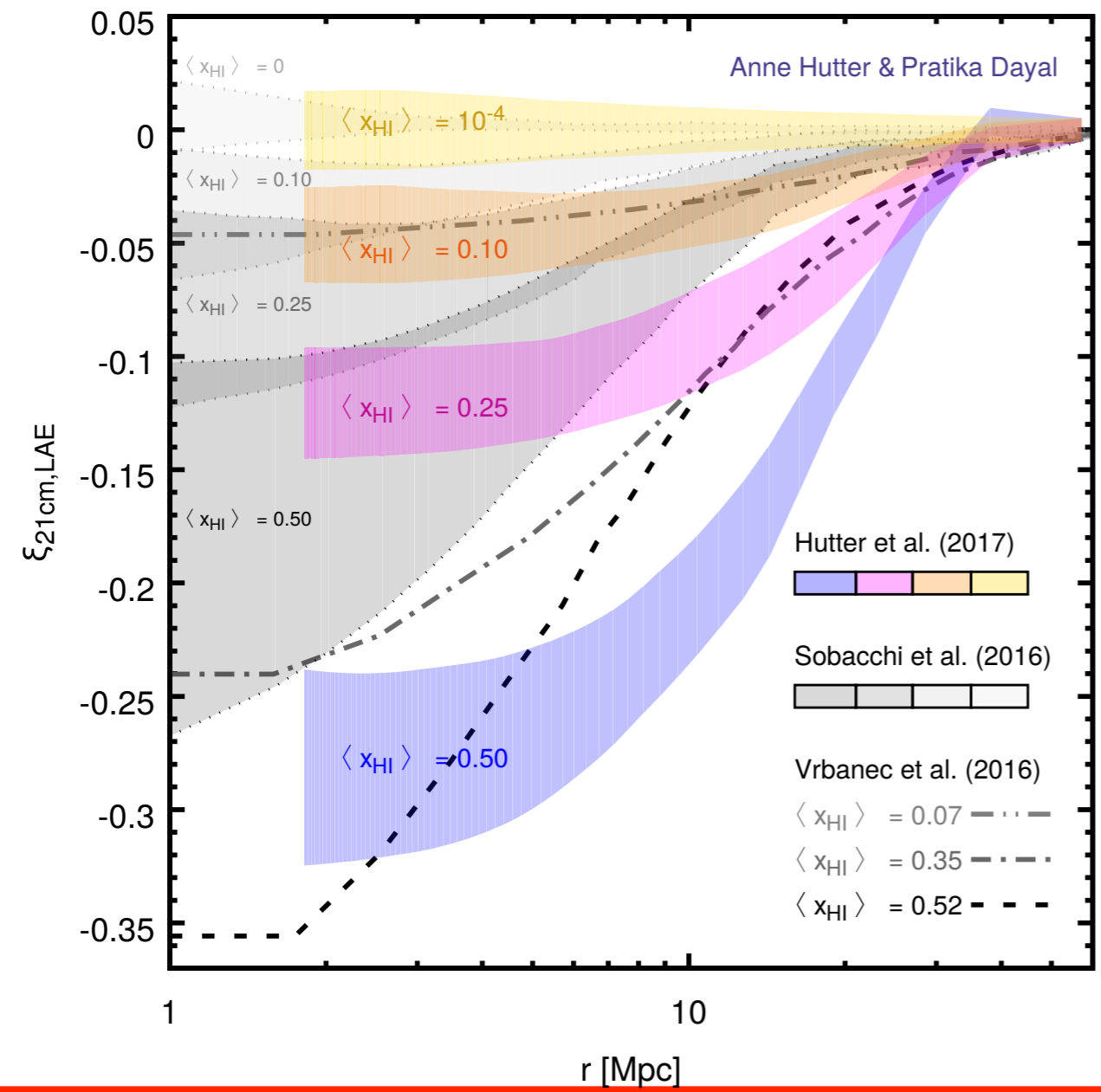
Large galaxy samples with LAE surveys or Euclid possible to  $z \sim 8$

Fundamental need for new types of observation to understand details of reionization



# Euclid synergies?

- $z=8$  QSO to find those that are radio loud
- Bright galaxies for stacking
- LAE - 21 cm cross-correlation as probe of HII region sizes
- ???







# Conclusions

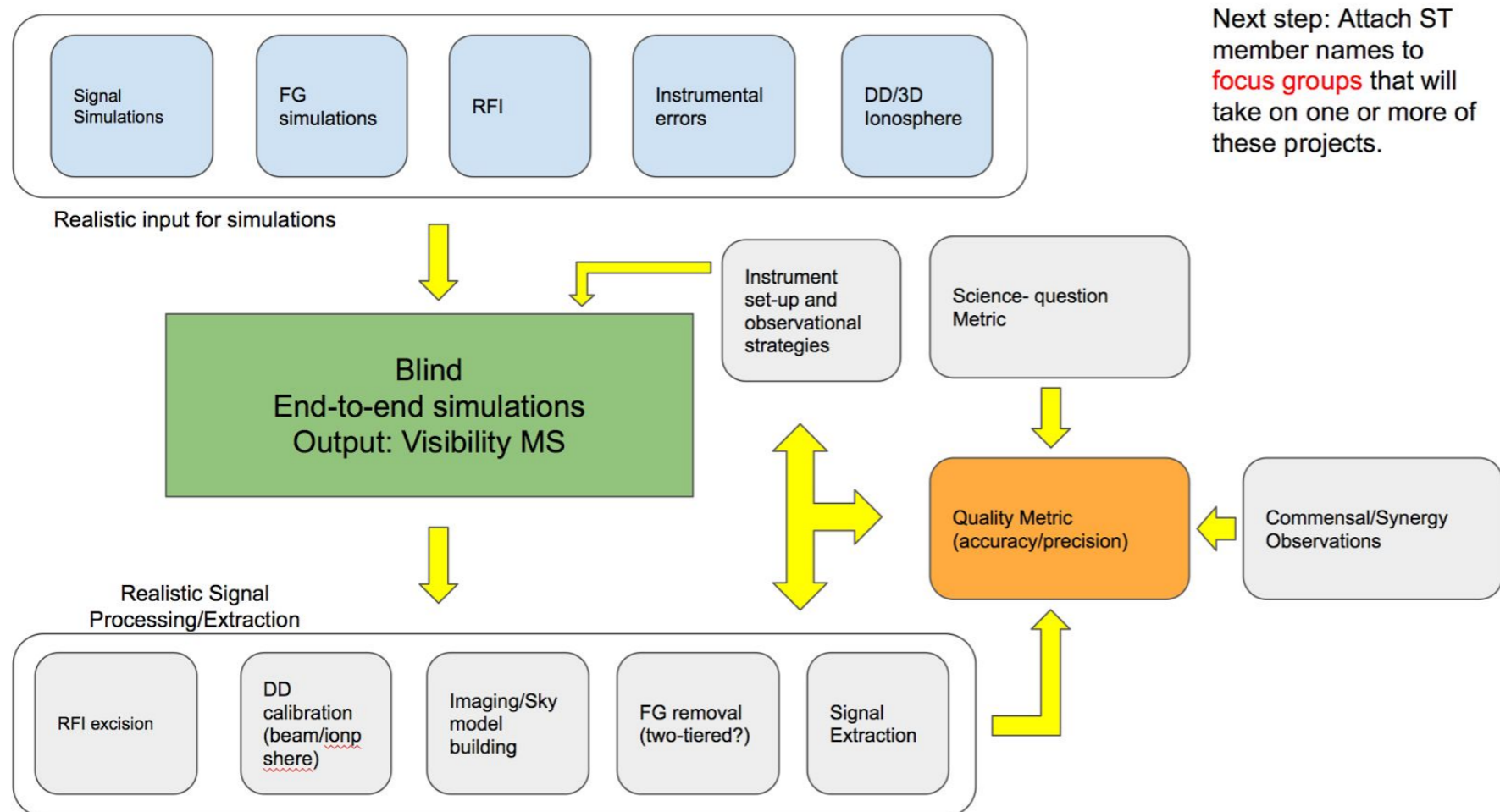
- SKA1 should begin commissioning/early science in 2021 with full operations in ~2024. (c.f. Euclid 2021-27)
- Taking shape now - cost control exercise, IGO, ...
- EoR plans HI surveys at  $z = 3 - 27$ 
  - SHALLOW - 10,000 deg<sup>2</sup> at LOFAR like sensitivity,  $z \sim 7-15$
  - MEDIUM + IM - 5000 deg<sup>2</sup>  $z \sim 3-20$
  - DEEP - 100 deg<sup>2</sup>,  $z \sim 6-27$
- Synergies with Euclid from both MID and LOW
  - MID better matched to low redshifts  $z < 3$  (Pourtsidou talk)
  - LOW for  $3 < z < 27$
- For reionisation:
  - LAE-21 cm cross correlations; Stack on LBGs?
  - High- $z$  quasars for radio follow up
  - OmegaHI
  - ???
- SKA-EoR Science Team preparing for KSP bid in ~2019  
Synergy focus group leads: Pratika Dayal, Erik Zackrisson

# SKA EoR Science Team

Leon Koopmans (NL, Chair ST), Gianni Bernardi (SA), Garrelt Mellema (SE),  
Andrei Mesinger (IT), Jonathan Pritchard (UK, Chair SWG), Cath Trott (AU)  
Abhi Datta (IN)

Various focus groups studying aspects of doing 21cm with SKA

<https://sites.google.com/site/skacdeorscienceteam/home>



Focus on pipelines at present

KSP bid in ~2019

Interest in synergy

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Figure 1: Flow-diagram for End-to-End data simulations.



# Other SKA-Euclid Synergies

- **Cosmology (MID)**
  - galaxy surveys - SKA1: Continuum, HI IM; SKA2: HI
  - weak lensing with SKA2 - different systematics  
(think 5000 deg<sup>2</sup> survey)
- **Reionization (LOW)**
  - 21 cm - LAE cross correlation
  - stack on bright galaxies at high-z
  - Radio loud quasars at  $z > 6$  (especially  $z \sim 8$ )
  - HI intensity mapping at  $3 < z < 6$
- **General**
  - LOW (50-350 MHz),
  - MID - Band 1 (580-1015MHz), Band 2 (0.9 - 1.67 GHz),  
Band 5 (8-13.8GHz)



# $z \sim 8$ quasars

21cm Forest requires radio bright sources at  $z > 7$

- QSO
- GRB

Euclid will be key for providing  $z \sim 8$  QSOs (hopefully some radio loud)

